Sample Calculations

Sample Calculations, Stack Outlet, Method 5B/202, Run 1

Area of Sample Location

$$A_s = \pi \times \left(\frac{d_n}{2 \times 12} \right)^2$$

$$A_s = \pi \times \left(\frac{180}{2 \times 12} \right)^2$$

$$A_s = 177 ft^2$$

where:

A_s	= area of sample location (ft^2)
d_s	= diameter of sample location (in)
12	= conversion factor (in/ft)
2	= conversion factor (diameter to radius)

Stack Pressure Absolute

$$P_a = P_b + \frac{P_s}{13.6}$$

$$P_a = 29.56 + \frac{-0.1}{13.6}$$

$$P_a = 29.55 in.Hg$$

where:

P_a	= stack pressure absolute (in. Hg)
P_b	= barometric pressure (in. Hg)
P_s	= static pressure (in. H_2O)
13.6	= conversion factor (in. H_2O/in. Hg)

Volume of Dry Gas Collected Corrected to Standard Temperature and Pressure

$$V_{m(std)} = \frac{17.64(V_m)(Y_d)\left(P_b + \frac{\Delta H}{13.6}\right)}{(T_m + 460)}$$

$$V_{m(std)} = \frac{17.64(60.01)(1.0034)\left(29.56 + \frac{1.73}{13.6}\right)}{(91.9 + 460)}$$

$$V_{m(std)} = 60.01 scf$$

where:

$V_{m(std)}$	= volume of gas collected at standard temperature and pressure (scf)
V_m	= volume of gas sampled at meter conditions (ft^3)
Y_d	= gas meter correction factor (dimensionless)
P_b	= barometric pressure (in. Hg)
ΔH	= average sample pressure (in. H_2O)
T_m	= average gas meter temperature (^oF)
13.6	= conversion factor (in. H_2O/in. Hg)
17.64	= ratio of standard temperature over standard pressure (^oR/in.Hg)
460	= conversion (^oF to ^oR)

Volume of Water Vapor Collected Corrected to Standard Temperature and Pressure

$$V_{w(std)} = 0.04715 \times (V_{wc} + V_{wsg})$$

$$V_{w(std)} = 0.04715 \times (175.8 + 11.0)$$

$$V_{w(std)} = 8.81 scf$$

where:

$V_{w(std)}$	= volume of water vapor at standard conditions (scf)
V_{wc}	= weight of liquid collected (g)
V_{wsg}	= weight gain of silica gel (g)
0.04715	= volume occupied by one gram of water at standard temperature and pressure (ft^3/g)

Percent Moisture[2]

$$B_{ws} = 100 \times \left[\frac{V_{w(std)}}{\left(V_{m(std)} + V_{w(std)}\right)} \right]$$

$$B_{ws} = 100 \times \left[\frac{8.81}{(60.01 + 8.81)} \right]$$

$$B_{ws} = 12.8\%$$

where:

B_{ws}	= moisture content of the gas stream (%)
$V_{m(std)}$	= volume of gas collected at standard temperature and pressure (scf)
$V_{w(std)}$	= volume of water vapor at standard conditions (scf)
100	= conversion factor

Molecular Weight of Dry Gas Stream[3]

$$M_d = \left(44 \times \frac{\%CO_2}{100}\right) + \left(32 \times \frac{\%O_2}{100}\right) + \left(28 \times \frac{(\%N_2)}{100}\right)$$

$$M_d = \left(44 \times \frac{11.6}{100}\right) + \left(32 \times \frac{7.72}{100}\right) + \left(28 \times \frac{(80.7)}{100}\right)$$

$$M_d = 30.16 lb/lbmole$$

where:

M_d	= molecular weight of the dry gas stream (lb/lb-mole)
$\%CO_2$	= carbon dioxide content of the dry gas stream (%)
44	= molecular weight of carbon dioxide (lb/lb-mole)
$\%O_2$	= oxygen content of the dry gas stream (%)
32	= molecular weight of oxygen (lb/lb-mole)
$\%N_2$	= nitrogen content of the dry gas stream (%)
28	= molecular weight of nitrogen and carbon monoxide (lb/lb-mole)
100	= conversion factor

[2] The moisture saturation point is used for all calculations if it is exceeded by the actual moisture content.
[3] The remainder of the gas stream after subtracting carbon dioxide and oxygen is assumed to be nitrogen.

Molecular Weight of Wet Gas Stream

$$M_s = \left(M_d \times \left(1 - \frac{B_{ws}}{100}\right)\right) + \left(18 \times \frac{B_{ws}}{100}\right)$$

$$M_s = \left(30.16 \times \left(1 - \frac{12.8}{100}\right)\right) + \left(18 \times \frac{12.8}{100}\right)$$

$$M_s = 28.61 lb / lbmole$$

where:

M_s	= molecular weight of the wet gas stream (lb/lb-mole)
M_d	= molecular weight of the dry gas stream (lb/lb-mole)
B_{ws}	= moisture content of the gas stream (%)
18	= molecular weight of water (lb/lb-mole)
100	= conversion factor

Velocity of Gas Stream

$$V_s = 85.49 (C_p)(\sqrt{\Delta P}) \sqrt{\frac{(T_s + 460)}{(M_s)\left(P_b + \frac{P_s}{13.6}\right)}}$$

$$V_s = 85.49 (0.84)(1.39) \sqrt{\frac{(128 + 460)}{(28.61)\left(29.56 + \frac{-0.1}{13.6}\right)}}$$

$$V_s = 83.2 ft / \sec$$

where:

V_s	= average velocity of the gas stream (ft/sec)
C_p	= pitot tube coefficient dimensionless
$\sqrt{\Delta P}$	= average square root of velocity pressures (in. H_2O)$^{1/2}$
T_s	= average stack temperature (°F)
M_s	= molecular weight of the wet gas stream (lb/lb-mole)
P_b	= barometric pressure (in. Hg)
P_s	= static pressure of gas stream (in. H_2O)
85.49	= pitot tube constant (ft/sec)([(lb/lb-mole)(in. Hg)]/[(°R)(in. H_2O)])$^{1/2}$
460	= conversion (°F to °R)
13.6	= conversion factor (in. H_2O/in. Hg)

Volumetric Flow of Gas Stream - Actual Conditions

$$Q_a = 60(V_s)(A_s)$$
$$Q_a = 60(83.2)(177)$$
$$Q_a = 882{,}234 acfm$$

where:

Q_a	= volumetric flow rate of the gas stream at actual conditions (acfm)
V_s	= average velocity of the gas stream (ft/sec)
A_s	= area of duct or stack (ft^2)
60	= conversion factor (min/hr)

Volumetric Flow of Gas Stream - Standard Conditions

$$Q_{std} = \frac{17.64(Q_a)\left(P_b + \frac{P_s}{13.6}\right)}{(T_s + 460)}$$

$$Q_{std} = \frac{17.64(882{,}234)\left(29.56 + \frac{-0.1}{13.6}\right)}{(128 + 460)}$$

$$Q_{std} = 782{,}725 scfm$$

where:

Q_{std}	= volumetric flow rate of the gas stream at standard conditions (scfm)
Q_a	= volumetric flow rate of the gas stream at actual conditions (acfm)
T_s	= average stack temperature (^oF)
P_b	= barometric pressure (in. Hg)
P_s	= static pressure of gas stream (in. H_2O)
13.6	= conversion factor (in. H_2O/in. Hg)
17.64	= ratio of standard temperature over standard pressure (^oR/in. Hg)
460	= conversion (^oF to ^oR)

Volumetric Flow of Gas Stream - Standard Conditions - Dry Basis

$$Q_{dstd} = Q_{std}\left(1 - \frac{B_{ws}}{100}\right)$$

$$Q_{dstd} = 782{,}715\left(1 - \frac{12.8}{100}\right)$$

$$Q_{dstd} = 682{,}820\,dscfm$$

where:

Q_{dstd}	= volumetric flow rate of the gas stream at standard conditions, on a dry basis (dscfm)
Q_{std}	= volumetric flow rate of the gas stream at standard conditions (scfm)
B_{ws}	= moisture content of the gas stream (%)
100	= conversion factor

Area of Nozzle

$$A_n = \pi \times \left(\frac{d_n}{2\times12}\right)^2$$

$$A_n = \pi \times \left(\frac{0.184}{2\times12}\right)^2$$

$$A_n = 0.000185\,ft^2$$

where:

A_n	= area of nozzle (ft^2)
d_n	= diameter of nozzle (in)
12	= conversion factor (in/ft)
2	= conversion factor (diameter to radius)

Percent Isokinetic

$$I = \frac{0.0945(T_s + 460)(V_{m(std)})}{\left(P_b + \frac{P_s}{13.6}\right)(v_s)(A_n)(\Theta)\left(1 - \frac{B_{ws}}{100}\right)}$$

$$I = \frac{0.0945(128 + 460)(60.01)}{\left(29.56 + \frac{-0.1}{13.6}\right)(83.2)(1.85 \times 10^{-4})(90)\left(1 - \frac{12.8}{100}\right)}$$

$$I = 93.5\%$$

where:

I	= percent isokinetic (%)
T_s	= average stack temperature (°F)
$V_{m(std)}$	= volume of gas collected at standard temperature and pressure (scf)
P_b	= barometric pressure (in. Hg)
P_s	= static pressure of gas stream (in. H_2O)
V_s	= average velocity of the gas stream (ft/sec)
A_n	= cross sectional area of nozzle (ft^2)
Θ	= sample time (min)
B_{ws}	= moisture content of the gas stream (%)
0.0945	= constant (^{0}R/in. Hg)
460	= conversion (°F to °R)
13.6	= conversion factor (in. H_2O/in Hg)
100	= conversion factor

Acetone Wash Blank-Particulate

$$W_a = \frac{(m_{ab})(v_{aw})}{v_{awb}}$$

$$W_a = \frac{(0.0000)(75)}{200}$$

$$W_a = 0.0000g$$

where:

W_a	= particulate mass in acetone wash, blank corrected (g)
m_{ab}	= mass collected, acetone wash blank (g)
v_{aw}	= volume of acetone wash (ml)
v_{awb}	= volume of acetone wash blank (ml)

Mass in Front Half, Acetone Blank Corrected

$$m_f = m_{fil} + (m_a - W_a)$$

$$m_f = 0.0026 + (0.0058 - 0.0000)$$

$$m_f = 0.0083g$$

where:

m_f	= mass in front half filter, and acetone wash, blank corrected (g)
m_{fil}	= mass in front half filter (g)
m_a	= mass in acetone wash (g)
W_a	= particulate mass in acetone wash blank (g)

Total Particulate Catch

$$M_n = m_f + m_b$$

$$M_n = 0.0083 + 0.0137$$

$$M_n = 0.0220g$$

where:

M_n	= total mass catch (g)
m_f	= mass in front half filter, and acetone wash, blank corrected (g)
m_b	= mass in back half organic fraction, and inorganic fraction, blank corrected (g)

Total Particulate Concentration, grains/dscf

$$C_{gr/dscf} = \frac{(M_n)(15.43)}{V_{m,std}}$$

$$C_{gr/dscf} = \frac{(0.0220)(15.43)}{60.01}$$

$$C_{gr/dscf} = 0.00566\, grains/dscf$$

where:

$C_{gr/dscf}$	= particulate concentration (grains/dscf)
M_n	= total particulate catch (g)
$V_{m(std)}$	= volume of gas collected at standard conditions (scf)
15.43	= conversion factor (grains/g)

Calculated F_d Factor, dscf/mmBtu

$$F_d = K((K_{hd} \times H) + (K_c \times C) + (K_s \times S) + (K_n \times N) - (K_o \times O_2))/GCV_w$$

$$F_d = 10^6((3.64 \times 4.83) + (1.53 \times 73.83) + (0.57 \times 3.59) + (0.14 \times 1.51) - (0.46 \times 8.24))/13{,}080$$

$$F_d = 9{,}863$$

where:

F_d	= calculated fuel factor (dscf/mmBtu)
K	= conversion factor (Btu/million Btu)
K_{hd}	= constant (scf/lb)
H	= weight percent hydrogen in coal (%)
K_c	= constant (scf/lb)
C	= weight percent carbon in coal (%)
K_s	= constant (scf/lb)
S	= weight percent sulfur in coal (%)
K_n	= constant (scf/lb)
N	= weight percent nitrogen in coal (%)
K_o	= constant (scf/lb)
O_2	= weight percent oxygen in coal (%)
GCV_w	= gross calorific value of fuel, wet (Btu/lb)

Total Particulate Emission Rate, lb/mmBtu [4]

$$E_{PM} = \frac{(M_n)(F_d)(20.9)}{(V_{m(std)})(453.6)(20.9 - O_2)}$$

$$E_{PM} = \frac{(0.0220)(9{,}863)(20.9)}{(60.27)(453.6)(20.9 - 7.72)}$$

$$E_{PM} = 0.0126 lb / mmBtu$$

where:

E_{PM}	= toal particulate matter emission rate, (lb/mmBtu)
M_n	= total particulate catch (g)
F_d	=fuel factor (dcsf/mmBtu)
20.9	= oxygen content of ambient air (%)
$V_{m(std)}$	= volume of gas collected at standard temperature and pressure (scf)
453.6	= conversion factor (g/lb)
$\%O_2$	= oxygen content of the dry gas stream (%)

Total Particulate Emission Rate, lb/hr

$$E_{lb/hr} = \frac{(M_n)(Q_{dstd})(60)}{(V_{m,std})(453.6)}$$

$$E_{lb/hr} = \frac{(0.0220)(682{,}820)(60)}{(60.01)(453.6)}$$

$$E_{lb/hr} = 33.1 lb / hr$$

where:

$E_{lb/hr}$	= particulate emission rate (lb/hr)
M_n	= total particulate catch (g)
$V_{m(std)}$	= volume of gas collected at standard conditions (scf)
Q_{dstd}	= volumetric flow rate of the dry gas stream at standard conditions (dscfm)
60	= conversion factor (min/hr)
453.6	= conversion factor (g/lb)

[4] All particulate emission rates are calculated in a similar manner.

Sample Calculations, Method 26A, Run 1

Concentration of Hydrogen Chloride in Flue Gas (lb/dscf)[5]

$$C_{HCL} = \frac{(M_{HCl})}{(V_{m(std)})(10^3)(453.6)}$$

$$C_{HCl} = \frac{(1.15)}{(94.71)(10^3)(453.6)}$$

$$C_{HCl} = 2.68 \times 10^{-8}\, lb/dscf$$

where:

C_{HCl} = concentration of hydrogen chloride in flue gas (lb/dscf)
M_{HCl} = mass of hydrogen chloride collected in sample (mg)
$V_{m(std)}$ = volume of gas collected at standard temperature and pressure (scf)
10^3 = conversion factor (mg/g)
453.6 = conversion factor (g/lb)

Concentration of Hydrogen Chloride in Flue Gas (ppmdv)[6]

$$C_{ppmv} = \frac{(M_{HCl})(385.3)(10^6)}{(MW_{HCl})(V_{m(std)})(10^3)(453.6)}$$

$$C_{ppmv} = \frac{(1.15)(385.3)(10^6)}{(36.458)(94.71)(10^3)(453.6)}$$

$$C_{ppmv} = 0.283\, ppmdv$$

where:

C_{ppmv} = concentration of hydrogen chloride in flue gas (ppmv)
M_{HCl} = mass of hydrogen chloride collected in sample (mg)
385.3 = = volume occupied by one pound gas at standard conditions (dscf/lbmole)
10^6 = conversion factor (fraction to ppm)
MW_{HCl} = molecular weight of hydrogen chloride (lb/lb-mole)
$V_{m(std)}$ = volume of gas collected at standard temperature and pressure (scf)
10^3 = conversion factor (mg/g)
453.6 = conversion factor (g/lb)

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[5] The HF concentration was calculated in a similar manner.
[6] The HF concentration was calculated in a similar manner.

Hydrogen Chloride Emission Rate, lb/mmBtu[7]

$$E_{HCl} = \frac{(C_{HCl})(F_d)(20.9)}{(20.9 - O_2)}$$

$$E_{HCl} = \frac{(2.68 \times 10^{-8})(9{,}863)(20.9)}{(20.9 - 7.72)}$$

$$E_{HCl} = 0.000419 lb / mmBtu$$

where:

E_{HCl}	= hydrogen chloride emission rate, (lb/mmBtu)
C_{HCl}	= hydrogen chloride concentration, (lb/dscf)
F_d	=fuel factor (dcsf/mmBtu)
20.9	= oxygen content of ambient air (%)
$\%O_2$	= oxygen content of the dry gas stream (%)

Hydrogen Chloride Emission Rate

$$E_{HCl} = C_{HCl} \times Q_{dstd} \times 60$$

$$E_{HCl} = 2.68 \times 10^{-8} \times 654{,}404 \times 60$$

$$E_{HCl} = 1.05 lb / hr$$

where:

E_{HCl}	= hydrogen chloride emission rate, (lb/hr)
C_{ppmdv}	= hydrogen chloride concentration, dry basis, (ppmdv)
Q_{dstd}	= volumetric flow rate of the dry gas stream at standard conditions (dscfm)
MW	= molecular weight of hydrogen chloride (lb/lbmole)
60	= conversion factor (min/hr)
385.3	= volume occupied by one pound gas at standard conditions (dscf/lbmole)
10^6	= conversion factor (fraction to ppm)

[7] The HF emission rate was calculated in a similar manner.

Sample Calculations, Method 29, Run 1

Concentration of Lead in Flue Gas, ug/dscm[8]

$$C_{ug/dscm} = \frac{(M_C)}{(V_{m(std)})}(35.31)$$

$$C_{ug/dscm} = \frac{(4.79)}{(66.01)}(35.31)$$

$$C_{ug/dscm} = 2.56 ug/dscm$$

where:

$C_{ug/dscm}$	= concentration of lead in flue gas (ug/dscm)
M_C	= mass of lead in sample (ug)
$V_{m(std)}$	= volume of gas collected at standard temperature and pressure(scf)
35.31	= conversion factor (ft^3/m^3)

Emission Rate of Lead in Flue Gas, lb/mmBtu[9]

$$E = \frac{(C_{ug/dscm})(F_d)(20.9)}{(35.315)(20.9 - \%O_2)(453.6)(10^6)}$$

$$E = \frac{(2.56)(9,863)(20.9)}{(35.315)(20.9 - 7.72)(453.6)(10^6)}$$

$$E = 2.50 \times 10^{-6} lb/mmBtu$$

where:

E	= lead emission rate (lb/mmBtu)
$C_{ug/dscm}$	= lead concentration (ug/dscm)
F_d	=fuel factor (dcsf/mmBtu)
35.31	=conversion factor (ft^3/m^3)
20.9	= oxygen content of ambient air (%)
$\%O_2$	= oxygen content of the dry gas stream (%)
453.6	= conversion factor (g/lb)
10^6	= conversion factor (ug/g)

[8] The concentrations of all MHs and mercury are calculated in a similar manner.
[9] The emission rates of all MHs and mercury are calculated in a similar manner.

Lead Emission Rate, lb/hr

$$E_{lb/hr} = \frac{(C_{ug/dscm})(Q_{dstd})(60)}{(35.31)(10^6)(453.6)}$$

$$E_{lb/hr} = \frac{(2.56)(684{,}896)(60)}{(35.31)(10^3)(10^3)(453.6)}$$

$$E_{lb/hr} = 0.00657 lb/hr$$

where:

$E_{lb/hr}$	= lead emission rate (lb/hr)
$C_{ug/dscm}$	= lead concentration (ug/dscm)
Q_{dstd}	= volumetric flow rate of dry gas stream at standard conditions (dscfm)
10^3	= conversion factor (ug/mg)
10^3	= conversion factor (mg/g)
35.31	= conversion factor (ft^3/m^3)
60.0	= conversion factor (min/hr)
453.59	= conversion factor (g/lb)