Case No. 2016-00281 Commission Staff's First Set of Data Requests Order Dated September 12, 2016 Item No. 4 Attachment 1 Page 1 of 33

## KENTUCKY POWER COMPANY

2011 Analysis of System Losses

April 2013

Prepared by:



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MANAGEMENT APPLICATIONS CONSULTING, INC.<sup>Page 2 of 33</sup>

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April 17, 2013

Mr. David M. Roush Director Regulatory Pricing & Analysis American Electric Power 1 Riverside Plaza Columbus, OH 43215

Mr. Mark P. Gilbert Director Economic Forecasting American Electric Power 212 East 6<sup>th</sup> Street Tulsa, OK 74119

#### RE: 2011 LOSS ANALYSIS

Dear Messrs. Roush and Gilbert:

Transmitted herewith are the results of the 2011 Analysis of System Losses for the Kentucky Power Company's (KPCO) power system. Our analysis develops cumulative expansion factors (loss factors) for both demand (peak/kW) and energy (average/kWh) losses by discrete voltage levels applicable to metered sales data. Our analysis considers only technical losses in arriving at our final recommendations.

On behalf of MAC, we appreciate the opportunity to assist you in performing the loss analysis contained herein. The level of detailed load research and sales data by voltage level, coupled with a summary of power flow data and power system model, forms the foundation for determining reasonable and representative power losses on the KPCO system. Our review of these data and calculated loss results support the proposed loss factors as presented herein for your use in various cost of service, rate studies, and demand analyses.

Should you require any additional information, please let us know at your earliest convenience.

Sincerely,

concer

Paul M. Normand Principal

Enclosure PMN/rjp

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## **1.0 EXECUTIVE SUMMARY**

This report presents Kentucky Power Company's (KPCO) 2011 Analysis of System Losses for the power systems as performed by Management Applications Consulting, Inc. (MAC). The study developed separate demand (kW) and energy (kWh) loss factors for each voltage level of service in the power system for KPCO. The cumulative loss factor results by voltage level, as presented herein, can be used to adjust metered kW and kWh sales data for losses in performing cost of service studies, determining voltage discounts, and other analyses which may require a loss adjustment.

The procedures used in the overall loss study were similar to prior studies and emphasized the use of "in house" resources where possible. To this end, extensive use was made of the Company's peak hour power flow data and transformer plant investments in the model. In addition, measured and estimated load data provided a means of calculating reasonable estimates of losses by using a "top-down" and "bottom-up" procedure. In the "top-down" approach, losses from the high voltage system, through and including distribution substations, were calculated along with power flow data, conductor and transformer loss estimates, and metered sales.

At this point in the analysis, system loads and losses at the input into the distribution substation system are known with reasonable accuracy. However, it is the remaining loads and losses on the distribution substations, primary system, secondary circuits, and services which are generally difficult to estimate. Estimated and actual Company load data provided the starting point for performing a "bottom-up" approach for calculating the remaining distribution losses. Basically, this "bottom-up" approach develops line loadings by first determining loads and losses at each level beginning at a customer's meter service entrance and then going through secondary lines, line transformers, primary lines and finally distribution substation. These distribution system loads and associated losses are then compared to the initial calculated input into Distribution Substation loadings for reasonableness prior to finalizing the loss factors. An overview of the loss study is shown on Figure 1.

Table 1, below, provides the final results from Appendix A for the 2011 calendar year. Exhibits 8 and 9 of Appendix A present a more detailed analysis of the final calculated summary results of losses by segments and delivery voltage of the power system. The following Table 1 cumulative loss expansion factors are applicable only to metered sales at the point of receipt for adjustment to the power system's input level.



Loss Factors at Sales Level, Calendar Year 2011

Voltage Level <u>of Service</u>	Total <u>KPCO</u>	Distribution <u>Only</u>		
Demand (kW)				
Transmission <sup>1</sup>	1.04223	_		
Subtransmission	1.06139	1.01838		
Primary Lines	1.07358	1.03008		
Secondary	1.10354	1.05883		
Energy (kWh)				
Transmission <sup>1</sup>	1.03482	_		
Subtransmission	1.04720	1.01197		
Primary Lines	1.05535	1.01985		
Secondary	1.08761	1.05102		
Losses – Net System Input <sup>2</sup>	6.31%MWh			
	8.20%MW			
Losses – Net System Output <sup>3</sup>	6.73%MWh			
	8.93%MW			

Composite Loss Factors at Metered Sales Level

	MW	<b>MWH</b>
Retail	1.08990	1.06774
Wholesale	1.04797	1.03845

The loss factors presented in the Delivery Only column of Table 1 are the Total KPCO loss factors divided by the transmission loss factor in order to remove these losses from each service level loss factor. For example, the secondary distribution demand loss factor of 1.05883 includes the recovery of all remaining non-transmission losses from the subtransmission, distribution substation, primary lines, line transformers, secondary conductors and services.

The net system input shown in Table 1 represents the MWh losses of 6.31% for the total KPCO load using calculated losses divided by the associated input energy to the system. The 6.73% represents the same losses using system output instead of input as a reference. The net system output reference shown in Table 1 represents MWh losses of 6.73% and MW losses of 8.93%. These results use the appropriate total losses for each but are divided by system output or sales. These calculations are all based on the data and results shown on Exhibits 1, 7 and 9 of the study.

<sup>&</sup>lt;sup>3</sup> Net system output uses losses divided by output or sales data as a reference.



<sup>&</sup>lt;sup>1</sup> Reflects results for 765 kV, 345 kV 161 kV, and 138 kV.

<sup>&</sup>lt;sup>2</sup> Net system input equals firm sales plus losses, Company use less non-requirement sales and related losses. See Appendix A, Exhibit 1, for their calculations.

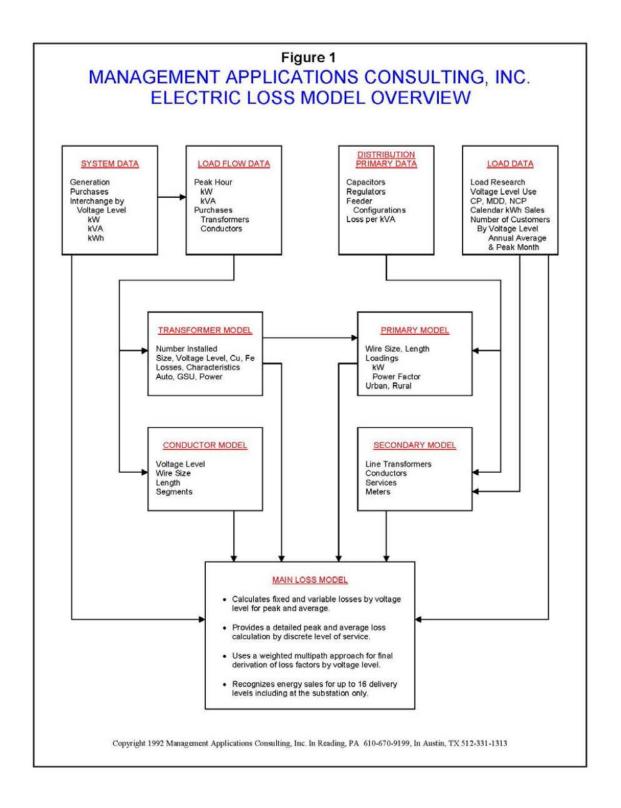
Due to the very nature of losses being primarily a function of equipment loadings, the loss factor derivations for any voltage level must consider both the load at that level plus the loads from lower voltages and their associated losses. As a result, cumulative losses on losses equates to additional load at higher levels along with future changes (+ or -) in loads throughout the power system. It is therefore important to recognize that losses are multiplicative in nature (future) and not additive (test year only) for all future years to ensure total recovery based on prospective fixed loss factors for each service voltage.

The derivation of the cumulative loss factors shown in Table 1 have been detailed for all electrical facilities in Exhibit 9, page 1 for demand and page 2 for energy. Beginning on line 1 of page 1 (demand) under the secondary column, metered sales are adjusted for service losses on lines 3 and 4. This new total load (with losses) becomes the load amount for the next higher facilities of secondary conductors and their loss calculations. This process is repeated for all the installed facilities until the secondary sales are at the input level (line 45). The final loss factor for all delivery voltages using this same process is shown on line 46 and Table 1 for demand. This procedure is repeated in Exhibit 9, page 2, for the energy loss factors.

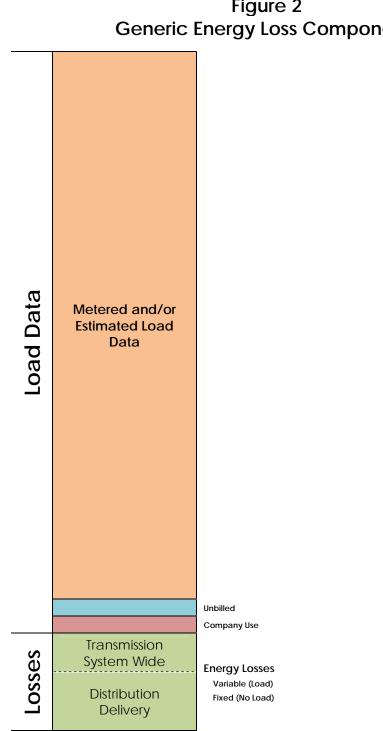
The loss factor calculation is simply the input required (line 45) divided by the metered sales (line 43).

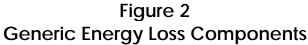
An overview of the loss study is shown on Figure 1 on the next page. Figure 2 simply illustrates the major components that must be considered in a loss analysis.













#### 2.0 INTRODUCTION

This report of the 2011 Analysis of System Losses for the Kentucky Power Company provides a summary of results, conceptual background or methodology, description of the analyses, and input information related to the study.

#### 2.1 **Conduct of Study**

Typically, between five to ten percent of the total kWh requirements of an electric utility is lost or unaccounted for in the delivery of power to customers. Investments must be made in facilities which support the total load which includes losses or unaccounted for load. Revenue requirements associated with load losses are an important concern to utilities and regulators in that customers must equitably share in all of these cost responsibilities. Loss expansion factors are the mechanism by which customers' metered demand and energy data are mathematically adjusted to the generation or input level (point of reference) when performing cost and revenue calculations.

An acceptable accounting of losses can be determined for any given time period using available engineering, system, and customer data along with empirical relationships. This loss analysis for the delivery of demand and energy utilizes such an approach. A microcomputer loss model<sup>4</sup> is utilized as the vehicle to organize the available data, develop the relationships, calculate the losses, and provide an efficient and timely avenue for future updates and sensitivity analyses. Our procedures and calculations are similar with prior loss studies, and they rely on numerous databases that include customer statistics and power system investments.

Company personnel performed most of the data gathering and data processing efforts and checked for reasonableness. MAC provided assistance as necessary to construct databases, transfer files, perform calculations, and check the reasonableness of results. A review of the preliminary results provided for additions to the database and modifications to certain initial assumptions based on available data. Efforts in determining the data required to perform the loss analysis centered on information which was available from existing studies or reports within the Company. From an overall perspective, our efforts concentrated on five major areas:

- 1. System information concerning peak demand and annual energy requirements by voltage level,
- 2. High voltage power system power flow data and associated loss calculations,
- 3. Distribution system primary and secondary loss calculations,
- 4. Derivation of fixed and variable losses by voltage level, and
- 5. Development of final cumulative expansion factors at each voltage for peak demand (kW) and annual energy (kWh) requirements at the point of delivery (meter).

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#### 2.2 Electric Power Losses

Losses in power systems consist of primarily technical losses with a much smaller level of non-technical losses.

#### **Technical Losses**

Electrical losses result from the transmission of energy over various electrical equipment. The largest component of these losses is power dissipation as a result of varying loading conditions and are oftentimes called load losses which are proportional to the square of the current ( $I^2R$ ). These losses can be as high as 75% of all technical losses. The remaining losses are called no-load and represent essentially fixed (constant) energy losses throughout the year. These no-load losses represent energy required by a power system to energize various electrical equipment regardless of their loading levels. The major portion of no-load losses consists of core or magnetizing energy related to installed transformers throughout the power system.

#### Non-Technical Losses

These are unaccounted for energy losses that are related to energy theft, metering, non-payment by customers, and accounting errors. Losses related to these areas are generally very small and can be extremely difficult and subjective to quantify. Our efforts generally do not develop any meaningful level as appropriate because we assume that improving technology and utility practices have minimized these amounts.

#### 2.3 Description of Model

The loss model is a customized applications model, constructed using the Excel software program. Documentation consists primarily of the model equations at each cell location. A significant advantage of such a model is that the actual formulas and their corresponding computed values at each cell of the model are immediately available to the analyst.

A brief description of the three (3) major categories of effort for the preparation of each loss model is as follows:

• Main sheet which contains calculations for all primary and secondary losses, summaries of all conductor and transformer calculations from other sheets discussed below, output reports and supporting results.



- Transformer sheet which contains data input and loss calculations for each distribution substation and high voltage transformer. Separate iron and copper losses are calculated for each transformer by identified type.
- Conductor sheet containing summary data by major voltage level as to circuit miles, loading assumptions, and kW and kWh loss calculations. Separate loss calculations for each line segment were made using the Company's power flow data by line segment and summarized by voltage level in this model.

Appendix A presents a detailed loss study result which derives the loss factors for the Company's system-wide power system. Appendix A, Exhibits 8 and 9, presents the final detailed summary results of the demand and energy losses for each major portion of the total KPCO power system.



#### 3.0 METHODOLOGY

#### 3.1 Background

The objective of a Loss Study is to provide a reasonable set of energy (average) and demand (peak) loss expansion factors which account for system losses associated with the transmission and delivery of power to each voltage level over a designated period of time. The focus of this study is to identify the difference between total energy inputs and the associated sales with the difference being equitably allocated to all delivery levels. Several key elements are important in establishing the methodology for calculating and reporting the Company's losses. These elements are:

- Selection of voltage level of services,
- Recognition of losses associated with conductors, transformations, and other electrical equipment/components within voltage levels,
- Identification of customers and loads at various voltage levels of service,
- Review of generation or net power supply input at each level for the test period studied, and
- Analysis of kW and kWh sales by voltage levels within the test period.

The three major areas of data gathering and calculations in the loss analysis were as follows:

- 1. System Information (monthly and annual)
  - MWH generation and MWH sales.
  - Coincident peak estimates and net power supply input from all sources and voltage levels.
  - Customer load data estimates from available load research information, adjusted MWH sales, and number of customers in the customer groupings and voltage levels identified in the model.
  - System default values, such as power factor, loading factors, and load factors by voltage level.



- 2. High Voltage System
  - Conductor information was summarized from a database by the Company which reflects the transmission system by voltage level. Extensive use was made of the Company's power flow data with the losses calculated and incorporated into the final loss calculations.
  - Transformer information was developed in a database to model transformation at each voltage level. Substation power, step-up, and auto transformers were individually identified along with any operating data related to loads and losses.
  - Power flow data of peak condition was the primary source of equipment loadings and derivation of load losses in the high voltage loss calculations.
- 3. Distribution System
  - Distribution Substations Data was developed for modeling each substation as to its size and loading. Loss calculations were performed from this data to determine load and no load losses separately for each transformer.
  - Primary lines Line loading and loss characteristics for several representative primary circuits were obtained from the Company. These loss results developed kW loss per MW of load and a composite average was calculated to derive the primary loss estimate.
  - Line transformers Losses in line transformers were based on each customer service group's size, as well as the number of customers per transformer. Accounting and load data provided the foundation with which to model the transformer loadings and to calculate load and no load losses.
  - Secondary network Typical secondary networks were estimated for conductor sizes, lengths, loadings, and customer penetration for residential and small general service customers.
  - Services Typical services were estimated for each secondary service class of customers identified in the study with respect to type, length, and loading.



The loss analysis was thus performed by constructing the model in segments and subsequently calculating the composite until the constraints of peak demand and energy were met:

- Information as to the physical characteristics and loading of each transformer and conductor segment was modeled.
- Conductors, transformers, and distribution were grouped by voltage level, and unadjusted losses were calculated.
- The loss factors calculated at each voltage level were determined by "compounding" the per-unit losses. Equivalent sales at the supply point were obtained by dividing sales at a specific level by the compounded loss factor to determine losses by voltage level.
- The resulting demand and energy loss expansion factors were then used to adjust all sales to the generation or input level in order to estimate the difference.
- Reconciliation of kW and kWh sales by voltage level using the reported system kW and kWh was accomplished by adjusting the initial loss factor estimates until the mismatch or difference was eliminated.

#### **3.2** Calculations and Analysis

This section provides a discussion of the input data, assumptions, and calculations performed in the loss analysis. Specific appendices have been included in order to provide documentation of the input data utilized in the model.

#### 3.2.1 Bulk, Transmission and Subtransmission Lines

The transmission and subtransmission line losses were calculated based on a modeling of unique voltage levels identified by the Company's power flow data and configuration for the entire integrated KPCO Power System. Specific information as to length of line, type of conductor, voltage level, peak load, maximum load, etc., were provided based on Company records and utilized as data input in the loss model.

Actual MW and MVA line loadings were based on KPCO's peak loading conditions. Calculations of line losses were performed for each line segment separately and combined by voltage levels for reporting purposes as shown in the Discussion of Results (Section 4.0) of this report. The loss calculations consisted of determining a circuit current value based on MVA line loadings and evaluating the  $I^2R$  results for each line segment.



After system coincident peak hour losses were identified for each voltage level, a separate calculation was then made to develop annual average energy losses based on a loss factor approach. Load factors were determined for each voltage level based on system and customer load information. An estimate of the Hoebel coefficient (see Appendix B) was then used to calculate energy losses for the entire period being analyzed. The results are presented in Section 4.0 of this report.

#### 3.2.2 Transformers

The transformer loss analysis required several steps in order to properly consider the characteristics associated with various transformer types; such as, step-up, auto transformers, distribution substations, and line transformers. In addition, further efforts were required to identify both iron and copper losses within each of these transformer types in order to obtain reasonable peak (kW) and average energy (kWh) losses. While iron losses were considered essentially constant for each hour, recognition had to be made for the varying degree of copper losses due to hourly equipment loadings.

Standardized test data tables were used to represent no load (fixed) and full load losses for different types and sizes of transformers. This test data was incorporated into the loss model to develop relationships representing copper and iron losses for the transformer loss calculation. These results were then totaled by various groups, as identified and discussed in Section 4.0.

The remaining miscellaneous losses considered in the loss study consisted of several areas which do not lend themselves to any reasonable level of modeling for estimating their respective losses and were therefore lumped together into a single loss factor of 0.10%. The typical range of values for these losses is from 0.10% to 0.25%, and we have assumed the lower value to be conservative at this time. The losses associated with this loss factor include bus bars, unmetered station use, and grounding transformers.



#### 3.2.3 Distribution System

The load data at the substation and customer level, coupled with primary and secondary network information, was sufficient to model the distribution system in adequate detail to calculate losses.

#### Primary Lines

Primary line loadings take into consideration the available distribution load along with the actual customer loads including losses. Primary line loss estimates were prepared by the Company for use in this loss study. These estimates considered loads per substation, voltage levels, loadings, total circuit miles, wire size, and single- to three-phase investment estimates. All of these factors were considered in calculating the actual demand (kW) and energy (kWh) for the primary system.

#### Line Transformers

Losses in line transformers were determined based on typical transformer sizes for each secondary customer service group and an estimated or calculated number of customers per transformer. Accounting records and estimates of load data provided the necessary database with which to model the loadings. These calculations also made it possible to determine separate copper and iron losses for distribution line transformers, based on a table of representative losses for various transformer sizes.

#### Secondary Line Circuits

A calculation of secondary line circuit losses was performed for loads served through these secondary line investments. Estimates of typical conductor sizes, lengths, loadings and customer class penetrations were made to obtain total circuit miles and losses for the secondary network. Customer loads which do not have secondary line requirements were also identified so that a reasonable estimate of losses and circuit miles of these investments could be made.

#### Service Drops and Meters

Service drops were estimated for each secondary customer reflecting conductor size, length and loadings to obtain demand losses. A separate calculation was also performed using customer maximum demands to obtain kWh losses. Meter loss estimates were also made for each customer and incorporated into the calculations of kW and kWh losses included in the Summary Results.



## 4.0 DISCUSSION OF RESULTS

A brief description of each Exhibit provided in Appendix A follows:

#### Exhibit 1 - Summary of Company Data

This exhibit reflects system information used to determine percent losses and a detailed summary of kW and kWh losses by voltage level. The loss factors developed in Exhibit 7 are also summarized by voltage level.

#### Exhibit 2 - Summary of Conductor Information

A summary of MW and MWH load and no load losses for conductors by voltage levels is presented. The sum of all calculated losses by voltage level is based on input data information provided in Appendix A. Percent losses are based on equipment loadings.

#### Exhibit 3 - Summary of Transformer Information

This exhibit summarizes transformer losses by various types and voltage levels throughout the system. Load losses reflect the copper portion of transformer losses while iron losses reflect the no load or constant losses. MWH losses are estimated using a calculated loss factor for copper and the test year hours times no load losses.

#### Exhibit 4 - Summary of Losses Diagram (2 Pages)

This loss diagram represents the inputs and output of power at system peak conditions. Page 1 details information from all points of the power system and what is provided to the distribution system for primary loads. This portion of the summary can be viewed as a "top down" summary into the distribution system.

Page 2 represents a summary of the development of primary line loads and distribution substations based on a "bottom up" approach. Basically, loadings are developed from the customer meter through the Company's physical investments based on load research and other metered information by voltage level to arrive at MW and MVA requirements during peak load conditions by voltage levels.

#### Exhibit 5 - Summary of Sales and Calculated Losses

Summary of Calculated Losses represents a tabular summary of MW and MWH load and no load losses by discrete areas of delivery within each voltage level. Losses have been identified and are derived based on summaries obtained from Exhibits 2 and 3 and losses associated with meters, capacitors and regulators.



#### Exhibit 6 - Development of Loss Factors, Unadjusted

This exhibit calculates demand and energy losses and loss factors by specific voltage levels based on sales level requirements. The actual results reflect loads by level and summary totals of losses at that level, or up to that level, based on the results as shown in Exhibit 5. Finally, the estimated values at generation are developed and compared to actual generation to obtain any difference or mismatch.

#### Exhibit 7 - Development of Loss Factors, Adjusted

The adjusted loss factors are the results of adjusting Exhibit 6 for any difference. All differences between estimated and actual are prorated to each level based on the ratio of each level's total load plus losses to the system total. These new loss factors reflect an adjustment in losses due only to the kW and kWh mismatch.

#### Exhibit 8 – Adjusted Losses and Loss Factors by Facility

These calculations present an expanded summary detail of Exhibit 7 for each segment of the power system with respect to the flow of power and associated losses from the receipt of energy at the meter to the generation for the KPCO power system.

#### Exhibit 9 – Summary of Losses by Delivery Voltage

These calculations present a reformatted summary of losses presented in Exhibits 7 and 8 by power system delivery segment as calculated by voltage level of service based on reported metered sales.



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## Kentucky Power Company 2011 Analysis of System Losses

# **Appendix A**

# Results of 2011 KPCO Integrated Power System Loss Analysis



#### KENTUCKY POWER

#### SUMMARY OF COMPANY DATA

ANNUAL PEAK	1,531 MW
ANNUAL SYSTEM INPUT	7,591,389 MWH
ANNUAL SALES OUTPUT	7,112,397 MWH
SYSTEM LOSSES @ INPUT SYSTEM LOSSES @ OUTPUT	478,992 or 6.31% 478,992 or 6.73%
SYSTEM LOAD FACTOR	56.6%

#### SUMMARY OF LOSSES - OUTPUT RESULTS

SERVICE	KV	M	IW Input	% TOTAL	MWH Input	% TOTAL
TRANS	765,345	52.9		42.15%	211,400	44.13%
	161,138		3.45%		2.78%	
SUBTRANS	69,46,34	20.8		16.54%	68,753	14.35%
			1.36%		0.91%	
PRIMARY	34,12,1	22.2		17.67%	57,725	12.05%
	- , ,		1.45%		0.76%	
SECONDARY	120/240,to,477	29.7		23.64%	141,114	29.46%
			1.94%		1.86%	
TOTAL		125.5		100.00%	478,992	100.00%
			8.20%		6.31%	

#### SUMMARY OF LOSS FACTORS

SERVICE	KV		LATIVE SALES D (Peak) 1/d	EXPANSION F ENERGY e	
TOT TRANS	765,345	1.04223	0.95948	1.03482	0.96636
SUBTRAN	161,138 69,46,34	1.06139	0.94216	1.04720	0.95492
PRIMARY	34,12,1	1.07358	0.93146	1.05535	0.94755
SECONDARY	120/240,to,477	1.10354	0.90617	1.08761	0.91944

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#### KENTUCKY POWER 2011 LOSS ANALYSIS

#### SUMMARY OF CONDUCTOR INFORMATION

DESCRIPTION			CIRCUIT LOADING			M\	MW LOSSES				MWH LOSSES	
			MILES	% R	ATING	LOAD	NO LOAD	TOTAL	L	LOAD	NO LOAD	TOTAL
BULK	765 KV O	R GREATE	ER						·			
TIE LINES			0.0		0.00%	0.000	0.000	0.000		0	0	0
BULK TRANS SUBTOT			<u>257.5</u> 257.5		0.00%	<u>11.777</u> 11.777	<u>2.844</u> 2.844	<u>14.621</u> 14.621		<u>71,988</u> 71,988	<u>24,912</u> 24,912	<u>96,900</u> 96,900
TRANS	138 KV	то	765.00	κv								
TIE LINES			C	)	0.00%	0.000	0.000	0.000		0	0	0
TRANS1 TRANS2	161 KV <u>138 KV</u>		56.5 <u>338.0</u>		0.00% 0.00%	4.361 <u>27.416</u>	0.040 <u>0.166</u>	4.402 <u>27.582</u>		14,202 <u>80,948</u>	352 <u>1,458</u>	14,553 <u>82,406</u>
SUBTOT			394.6			31.777	0.207	31.984		95,150	1,810	96,960
SUBTRANS	35 KV	то	138	KV					·			
	00 1 <i>0 1</i>		0	-	0.00%	0.000	0.000	0.000		0	0	0
SUBTRANS1 SUBTRANS2	69 KV 46 KV		425.0 167.3		0.00% 0.00%	13.669 3.794	0.000 0.000	13.669 3.794		40,500 11,243	0 0	40,500 11,243
SUBTRANS3	<u>35 KV</u>		<u>3.2</u>		0.00%	<u>0.010</u>	0.006	0.016		<u>30</u>		<u>83</u>
SUBTOT			595.4			17.473	0.006	17.479		51,772	<u>54</u> 54	51,8 <mark>26</mark>
PRIMARY LINES			8,180			13.136	0.000	13.136		25,107	0	25,107
SECONDARY LINES			2,367			4.736	0.000	4.736		9,354	0	9,354
SERVICES			3,147			5.622	0.364	5.985		11,969	3,184	15,153
TOTAL			14,941			84.521	3.420	87.941	-	265,340	29,960	295,300

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#### KENTUCKY POWER 2011 LOSS ANALYSIS

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SUMMARY OF TRANSFORMER INFORMATION
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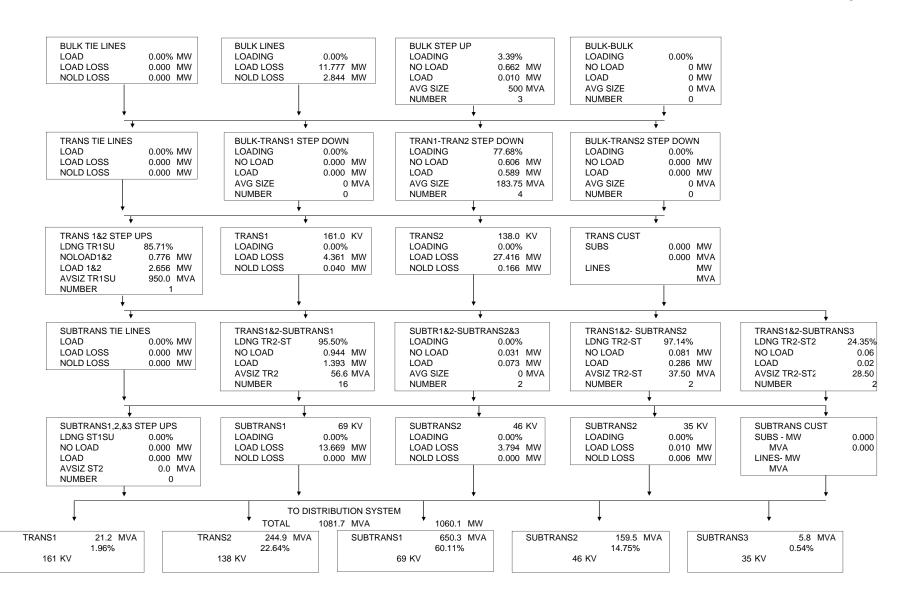
						RANSFORMER						L	*19/2019 22 of
DESCRIPTION		KV CAPA VOLTAGE	CITY MVA	NUMBER TRANSFMR	AVERAGE SIZE	LOADING %	MVA LOAD	LOAD	MW LOSSES - NO LOAD	TOTAL	LOAD	MWH LOSSES NO LOAD	 TOTAL
BULK STEP-UP		765	1,500.0	3	500.0	3.39%	51	0.010	0.662	0.672	30	5,795	5,824
BULK - BULK			0.0	0	0.0	0.00%	0	0	0.000	0.000	0		0
BULK - TRANS1		161	0.0	0	0.0	0.00%	0	0.000	0.000	0.000	0		0
BULK - TRANS2		138	0.0	0	0.0	0.00%	0	0.000	0.000	0.000	0		0
TRANS1 STEP-UP		161	950.0	1	950.0	85.71%	814	1.599	0.448	2.047	4,433	3,672	8,105
TRANS1 - TRANS2		138	735.0	4	183.8	77.68%	571	0.589	0.606	1.195	1,745		7,058
TRANS1-SUBTRANS1		69	54.0	1	54.0	116.02%	63	0.131	0.056	0.187	716		1,204
TRANS1-SUBTRANS2		46	0.0	0	0.0	0.00%	0	0.000	0.000	0.000	0		1,204
													-
TRANS1-SUBTRANS3		35	0.0	0	0.0	0.00%	0	0.000	0.000	0.000	0	0	0
TRANS2 STEP-UP		138	354.0	3	118.0	87.60%	310	1.057	0.328	1.385	3,004	2,743	5,747
TRANS2-SUBTRANS1		69	849.0	15	56.6	95.50%	811	1.262	0.888	2.150	8,326		16,107
TRANS2-SUBTRANS2		46	75.0	2	37.5	97.14%	73	0.286	0.081	0.367	815	708	1,524
TRANS2-SUBTRANS3		35	57.0	2	28.5	24.35%	14	0.021	0.062	0.083	42	544	586
SUBTRAN1 STEP-UP		69	0.0	0	0.0	0.00%	0	0.000	0.000	0.000	0	0	0
SUBTRAN2 STEP-UP		46	0.0	0	0.0	0.00%	0	0.000	0.000	0.000	0	0	0
SUBTRAN3 STEP-UP		35	0.0	0	0.0	0.00%	0	0.000	0.000	0.000	0	-	0
SUBTRAN1-SUBTRAN	,	46	24.0	2	12.0	82.91%	20	0.073	0.031	0.104	221	275	496
SUBTRAN1-SUBTRAN		35	0.0	0	0.0	0.00%	20	0.000	0.000	0.000	0		490
													-
SUBTRAN2-SUBTRAN	3	35	0.0	0	0.0	0.00%	0	0.000	0.000	0.000	0	0	0
						DI	ISTRIBUTION S	UBSTATIONS					
TRANS1 -	161	33	24.0	2	12.0	88.25%	21	0.084	0.031	0.116	175	275	451
TRANS1 -	161	12	0.0	0	0.0	0.00%	0	0.000	0.000	0.000	0	0	0
TRANS1 -	161	1	0.0	0	0.0	0.00%	0	0.000	0.000	0.000	0	0	0
TRANS2 -	138	33	285.0	12	23.8	66.92%	191	0.534	0.332	0.865	1,113	2,906	4,019
TRANS2 -	138	12	67.0	4	16.8	80.87%	54	0.179	0.083	0.261	373		1,097
TRANS2 -	138	1	0.0	0	0.0	0.00%	0	0.000	0.000	0.000	0		0
SUBTRAN1-	69	33	209.0	12	17.4	82.33%	172	0.558	0.257	0.816	1,165	2,252	3,417
SUBTRAN1-	69	12	620.5	54	11.5	76.80%	477	1.786	0.825	2.611	3,725		10,955
SUBTRAN1-	69	1	15.0	2	7.5	10.79%	2	0.001	0.023	0.025	2		211
	46	20	07.0	4	01.0	80.820/	70	0.007	0.400	0.200	400	802	1 205
SUBTRAN2-	46	33	87.0	4	21.8	80.83%	70	0.207	0.102	0.309	432		1,325
SUBTRAN2-	46	12	139.3	13	10.7	63.91%	89	0.335	0.191	0.526	699	/	2,375
SUBTRAN2-	46	1	1.0	1	1.0	23.98%	0	0.000	0.002	0.002	1	18	18
SUBTRAN3-	35	33	0.0	0	0.0	0.00%	0	0.000	0.000	0.000	0	0	0
SUBTRAN3-	35	12	5.0	1	5.0	116.20%	6	0.042	0.009	0.051	88	77	165
SUBTRAN3-	35	1	0.0	0	0.0	0.00%	0	0.000	0.000	0.000	0	0	0
PRIMARY - PRIMARY			21.3	4	5.3	54.60%	12	0.042	0.037	0.079	88	321	408
LINE TRANSFRMR			3,179.4	98,137	32.4	33.22%	1,056	4.227	10.149	14.376	6,931	88,902	95,833
TOTAL		=	9,251	98,279			=	13.024		28.228	 34,123	=======================================	======= 166,925
			3,20 I	30,213				13.024	10.204	20.220	34,123	102,001	100,920

Case No. 2016-00281 Commission Staff's First Set of Data Requests Order Dated September 12, 2016 Item No. 4 Attachment 1 EXHIBIT 4 P#Age ⊈3 of 33

#### KENTUCKY POWER 2011 LOSS ANALYSIS

1530.76 MW

SUMMARY OF LOSSES DIAGRAM - DEMAND MODEL - SYSTEM PEAK



Case No. 2016-00281

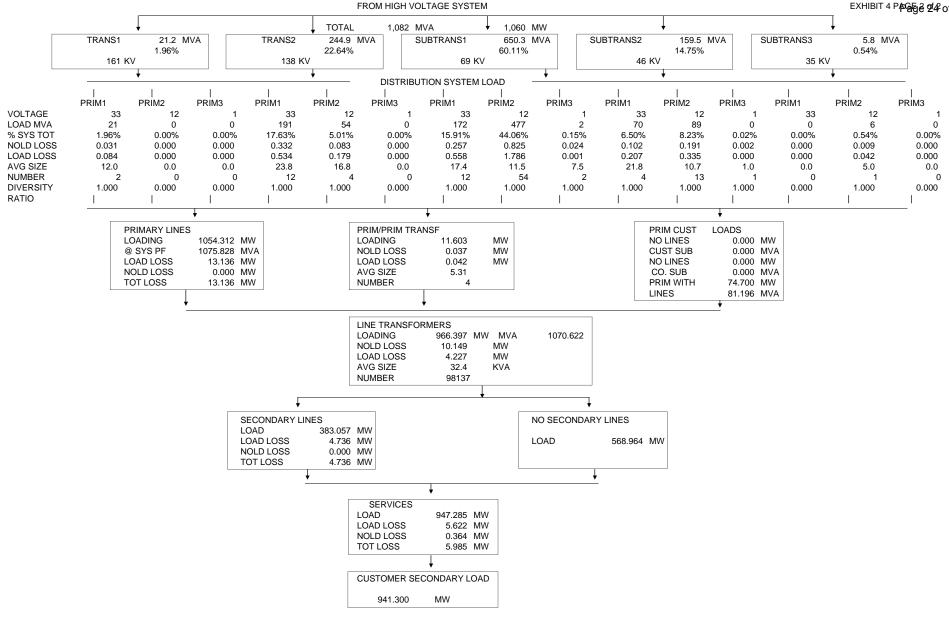
Commission Staff's First Set of Data Requests Order Dated September 12, 2016

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#### Attachment 1

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#### KENTUCKY POWER 2011 LOSS ANALYSIS



Case No. 2016-00281 Commission Staff's First Set of Data Requests Order Dated September 12, 2016 Item No. 4

#### Attachment 1 EXFHabe)∎ 25 of 33

#### KENTUCKY POWER 2011 LOSS ANALYSIS

#### SUMMARY of SALES and CALCULATED LOSSES

LOSS # AND LEVEL	MW LOAD	NO LOAD +	LOAD =	TOT LOSS	EXP FACTOR	CUM EXP FAC	MWH LOAD	NO LOAD +	LOAD =	TOT LOSS	EXP FACTOR	CUM EXP FAC
1 BULK XFMMR	0.0	0.00	0.00	0.00	0.000000	0.000000	0	0	0	0	0	0
2 BULK LINES	49.9	3.51	11.79	15.29	1.441882	1.441882	244,789	30,707	72,018	102,725	1.7230845	1.7230845
3 TRANS1 XFMR	0.0	0.00	0.00	0.00	0.000000	0.000000	0	0	0	0	0.0000000	0.0000000
4 TRANS1 LINES	798.0	0.49	5.96	6.45	1.008147	1.008147	4,562,176	4,024	18,634	22,658	1.0049913	1.0049913
5 TRANS2TR1 SD	559.5	0.61	0.59	1.20	1.002141	1.010305	2,744,683	5,313	1,745	7,058	1.0025780	1.0075822
6 TRANS2BLK SD	0.0	0.00	0.00	0.00	0.000000	0.000000	0	0	0	0	0.0000000	0.0000000
7 TRANS2 LINES	1,213.4	0.49	28.47	28.97	1.024457	1.029325	5,920,714	4,201	83,952	88,153	1.0151140	1.0186820
TOTAL TRAN	1,305.0	5.09	46.81	51.90	1.041421	1.041421	6,283,446	44,244	176,349	220,594	1.0363845	1.0363845
8 STR1BLK SD								·				
9 STR1T1 SD	61.4	0.06	0.13	0.19	1.003049	1.044596	301.204	487	716	1.204	1.0040123	1.0405428
10 SRT1T2 SD	794.6	0.89	1.26	2.15	1.002713	1.044247	3,897,990	7,781	8,326	16,107	1.0041494	1.0406848
11 SUBTRANS1 LINES	981.0	0.00	13.67	13.67	1.014130	1.056136	5,199,194	0	40,500	40,500	1.0078508	1.0445209
12 STR2T1 SD	0.0	0.00	0.00	0.00	0.000000	0.000000	0	0	0	0	0.0000000	0.0000000
13 STR2T2 SD	71.4	0.08	0.29	0.37	1.005164	1.046799	350,260	708	815	1,524	1.0043692	1.0409126
14 STR2S1 SD	19.5	0.03	0.07	0.10	1.005385	1.061823	95,659	275	221	496	1.0052158	1.0499690
15 SUBTRANS2 LINES	160.9	0.00	3.79	3.79	1.024152	1.066573	695,919	0	11,243	11,243	1.0164204	1.053402
16 STR3T1 SD	0.0	0.00	0.00	0.00	0.000000	0.000000	0	0	0	0	0.0000000	0.0000000
17 STR3T2 SD	13.6	0.06	0.02	0.08	1.006146	1.047821	66,716	544	42	586	1.0088600	1.0455668
18 STR3S1 SD	0.0	0.00	0.00	0.00	0.000000	0.000000	0	0	0	0	0.0000000	0.0000000
19 STR3S2 SD	0.0	0.00	0.00	0.00	0.000000	0.000000	0	0	0	0	0.0000000	0.0000000
20 SUBTRANS3 LINES	13.6	0.01	0.01	0.02	1.001187	1.042657	66,716	54	30	83	1.0012492	1.0376792
21 SUBTRANS TOTAL	1,150.0	1.12	19.25	20.37	1.018033	1.060201	5,811,708	9,850	61,893	71,743	1.0124989	1.049338
DISTRIBUTION SUBST												
TRANS1	20.8	0.03	0.08	0.12	1.005598	1.047251	83,968	275	175	451	1.0053984	1.0419793
TRANS2	240.0	0.41	0.71	1.13	1.004717	1.046333	970,949	3,630	1,486	5,116	1.0052971	1.0418743
SUBTR1	637.3	1.11	2.35	3.45	1.005446	1.061888	2,577,918	9,691	4,892	14,583	1.0056891	1.0504633
SUBTR2	156.4	0.30	0.54	0.84	1.005387	1.072319	632,521	2,587	1,132	3,718	1.0059134	1.0596314
SUBTR3	5.7	0.01	0.04	0.05	1.009001	1.052042	23,033	77	88	165	1.0072010	1.0451515
WEIGHTED AVERAGE	1,060.1	1.86	3.73	5.58	1.005294	1.059565	4,288,389	16,260	7,773	24,033	1.0056358	1.0496762
PRIMARY INTRCHNGE	0.0				0.000000		0				0.0000000	
PRIMARY LINES	1,054.3	0.00	13.18	13.18	1.012658	1.072977	4,264,267	0	25,194	25,194	1.0059434	1.0559148
LINE TRANSF	966.4	10.15	4.23	14.38	1.015101	1.089180	3,722,774	88,902	6,931	95,833	1.0264225	1.0838147
SECONDARY	952.0	0.00	4.74	4.74	1.004999	1.094625	3,626,941	0	9,354	9,354	1.0025858	1.0866172
SERVICES	947.3	0.36	5.62	5.99	1.006358	1.101585	3,617,587	3,184	11,969	15,153		1.0911879
	:	=======================================						=				
TOTAL SYSTEM		18.59	97.55	116.13				162,441	299,463	461,904		

#### DEVELOPMENT of LOSS FACTORS

UNADJUSTED DEMAND

LOSS FACTOR LEVEL	CUSTOMER SALES MW	CALC LOSS TO LEVEL	SALES MW @ GEN	CUM PEAK EX FACTORS	PANSION
	а	b	С	d	1/d
BULK LINES	0.0	0.0	0.0	0.00000	0.00000
TRANS SUBS	0.0	0.0	0.0	0.00000	0.00000
TRANS LINES	73.0	3.0	76.0	1.04142	0.96023
TOTAL TRANS	0.0	0.0	0.0	0.00000	0.00000
SUBTRANS	316.3	19.0	335.3	1.06020	0.94322
PRIM SUBS	0.0	0.0	0.0	0.00000	0.00000
PRIM LINES	74.7	5.5	80.2	1.07298	0.93199
SECONDARY	<u>941.3</u>	<u>95.6</u>	<u>1,036.9</u>	1.10158	0.90778
TOTALS	1,405.3	123.1	1,528.4		

#### DEVELOPMENT of LOSS FACTORS UNADJUSTED ENERGY

LOSS FACTOR LEVEL		CALC LOSS	SALES MWH @ GEN	CUM ANNUAL FACTORS	EXPANSION
	а	b	С	d	1/d
BULK LINES	0	0	0	0.00000	0.00000
TRANS SUBS	0	0	0	0.00000	0.00000
TRANS LINES	526,918	19,172	546,090	1.03638	0.96489
TOTAL TRANS	0	0	0	0.00000	0.00000
SUBTRANS	2,466,746	121,705	2,588,451	1.04934	0.95298
PRIM SUBS	0	0	0	0.00000	0.00000
PRIM LINES	516,299	28,869	545,168	1.05591	0.94705
SECONDARY	<u>3,602,434</u>	<u>328,498</u>	<u>3,930,932</u>	1.09119	0.91643
TOTALS	7,112,397	498,243	7,610,640		

#### ESTIMATED VALUES AT GENERATION

LOSS FACTOR AT		
VOLTAGE LEVEL	MW	MWH
BULK LINES	0.00	0
TRANS SUBS	0.00	0
TRANS LINES	76.02	546,090
SUBTRANS SUBS	0.00	0
SUBTRANS LINES	335.34	2,588,451
PRIM SUBS	0.00	0
PRIM LINES	80.15	545,168
SECONDARY	1,036.92	3,930,932
SUBTOTAL	1,528.44	7,610,640
ACTUAL ENERGY	1,530.76	7,591,389
MISSMATCH	(2.32)	19,251
% MISSMATCH	-0.15%	0.25%

KPCO 2011 LOSS B

#### DEVELOPMENT of LOSS FACTORS

ADJUSTED DEMAND

LOSS FACTOR LEVEL	CUSTOMER SALES MW	SALES ADJUST	CALC LOSS TO LEVEL	SALES MW @ GEN	CUM PEAK EXP FACTORS	ANSION
	a	b	C	d	e	f=1/e
BULK LINES	0.0	0.0	0.0	0.0	0.00000	0.00000
TRANS SUBS	0.0	0.0	0.0	0.0	0.00000	0.00000
TRANS LINES	73.0	0.0	3.1	76.1	1.04223	0.95948
TOTAL TRANS	0.0	0.0	0.0	0.0	0.00000	0.00000
SUBTRANS	316.3	0.0	19.4	335.7	1.06139	0.94216
PRIM SUBS	0.0	0.0	0.0	0.0	0.00000	0.00000
PRIM LINES	74.7	0.0	5.5	80.2	1.07358	0.93146
SECONDARY	941.3	<u>0.0</u>	97.5	<u>1,038.8</u>	1.10354	0.90617
			125.5			
TOTALS	1,405.3	0.0	125.5	1,530.8		

#### DEVELOPMENT of LOSS FACTORS ADJUSTED ENERGY

LOSS FACTOR LEVEL	CUSTOMER SALES MWH	SALES ADJUST		CALC LOSS TO LEVEL	SALES MWH @ GEN	CUM ANNUAL E FACTORS	XPANSION
	а	b		C	d	e	f=1/e
			•				
BULK LINES	0		0	0	0	0.00000	0.00000
TRANS SUBS	0		0	0	0	0.00000	0.00000
TRANS LINES	526,918		0	18,345	545,263	1.03482	0.96636
TOTAL TRANS	0		0	0	0	0.00000	0.00000
SUBTRANS	2,466,746		0	116,440	2,583,186	1.04720	0.95492
PRIM SUBS	0		0	0	0	0.00000	0.00000
PRIM LINES	516,299		0	28,579	544,878	1.05535	0.94755
SECONDARY	3,602,434		<u>0</u>	315,620	<u>3,918,054</u>	1.08761	0.91944
				478,983			
TOTALS	7,112,397		0	478,992	7,591,380		

#### ESTIMATED VALUES AT GENERATION

LOSS FACTOR AT		
VOLTAGE LEVEL	MW	MWH
BULK LINES	0.00	0
TRANS SUBS	0.00	0
TRANS LINES	76.08	545,263
SUBTRANS SUBS	0.00	0
SUBTRANS LINES	335.72	2,583,186
PRIM SUBS	0.00	0
PRIM LINES	80.20	544,878
SECONDARY	1,038.77	3,918,054
	1,530.76	7,591,380
ACTUAL ENERGY	1,530.76	7,591,389
MISSMATCH	0.00	(9)
	0.000/	
% MISSMATCH	0.00%	0.00%

#### KENTUCKY POWER 2011 LOSS ANALYSIS

EXHIBIT	8
	0

Adjusted Losses and Loss Fa	actors by Facilit	у			EXHIBIT 8
Unadjusted Los	sses by Segmer	ht			
	MW	Unadjusted	MWH	Unadjusted	
Service Drop Losses	5.99	6.94	15,153	18,400	
Secondary Losses	4.74	5.49	9,354	11,359	
Line Transformer Losses	14.38	16.67	95,833	116,370	
Primary Line Losses	13.18	15.28	25,194	30,594	
Distribution Substation Losses	5.58	6.47	24,033	29,183	
Subtransmission Losses	20.37	20.37	71,743	71,743	
Transmission System Losses	51.90	51.90	220,594	220,594	
Total	116.13	123.14	461,904	498,243	
			- ,	, -	
Mismatch Alloca		nt	<b>N</b> (1)		N
Service Drop Losses	MW -0.13		MWH 632		Note adjusting 632
Secondary Losses	-0.10		390		390
Line Transformer Losses	-0.31		3,994		3,994
Primary Line Losses	-0.29		1,050		1,050
Distribution Substation Losses	-0.12		1,002		1,000
Subtransmission Losses	-0.38		2,990		2,990
Transmission System Losses	-0.98		9,194		9,194
Total	-2.32		19,251		19,251
			-, -		19,251
Adjusted Loss	ses by Segment			o/ ( <b>T</b> )	
Convice Dren Lesson	MW	% of Total	MWH	% of Total	
Service Drop Losses	7.07	5.6%	17,769	3.7%	
Secondary Losses	5.60	4.5%	10,969	2.3%	
Line Transformer Losses	16.99	13.5%	112,376	23.5%	
Primary Line Losses	15.57	12.4%	29,544	6.2%	
Distribution Substation Losses	6.60	5.3%	28,182	5.9%	
Subtransmission Losses	20.75	16.5%	68,753	14.4%	
<u>Transmission System Losses</u> Total	52.88 125.46	42.2%	211,400	44.1%	
TOTAL	125.40	100.0%	478,992	100.0%	
Loss Factors by Segment	MW		мwн		
Retail Sales from Service Drops	941.30		3,602,434		
Adjusted Service Drop Losses	7.07		17,769		
Input to Service Drops	948.37		3,620,203		
Service Drop Loss Factor	1.00751		1.00493		
Output from Secondary	948.37		3,620,203		
Adjusted Secondary Losses	5.60		<u>10,969</u>		
Input to Secondary Secondary Conductor Loss Factor	953.97 <b>1.00590</b>		3,631,172 <b>1.00303</b>		
Output from Line Transformers	953.97		3,631,172		
Adjusted Line Transformer Losses	<u>16.99</u>		<u>112,376</u>		
Input to Line Transformers	970.95		3,743,548		
Line Transformer Loss Factor	1.01781		1.03095		
Secondary Composite	1.03150		1.03917		
Retail Sales from Primary	74.70		516,299		
Req. Whis Sales from Primary	0.00		0		
Input to Line Transformers	<u>970.95</u>		<u>3,743,548</u>		
Output from Primary Lines	1045.65		4,259,847		
Adjusted Primary Line Losses	<u>15.57</u>		29,544		
Input to Primary Lines	1061.23		4,289,391		
Primary Line Loss Factor	1.01489		1.00694		
Out TO PR from Distribution Substations	1061.23		4,289,391		
Req. Whis Sales from Substations	0.00		0		
Retail Sales from Substations	0.00		0		
TotalOutput from Distribution Substations	1061.23		4,289,391		
Adjusted Distribution Substation Losses	6.60		28,182		
Input to Distribution Substations	1067.82		4,317,572		
Distribution Substation Loss Factor	1.00622		1.00657		
Retail Sales at from SubTransmission	310.10		2,438,725		
Req. Whis Sales from SubTransmission	6.20		28,021		
Input to Distribution Substations	<u>799.30</u>		<u>3,233,472</u>		
Output from SubTransmission	1129.25		5,742,955		
Adjusted SubTransmission System Losses	<u>20.75</u>		<u>68,753</u>		
Input to SubTransmission	1150.00 1 01838		5,811,708		
SubTransmission Loss Factor	1.01838		1.01197		
OUT DISTR SUBS	260.77		1,054,917		
Retail Sales at from Transmission	58.50		459,332		
Req. Whis Sales from Transmission Input Subtransmission	14.50		67,586 4,490,212		
Output from Transmission	918.35 1252.12		4,490,212 6,072,046		
Adjusted Transmission System Losses	52.88		211,400		
Input to Transmission	1305.00		6,283,446		
Transmission Loss Factor	1.04223		6,283,446 <b>1.03482</b>		
Tanomioor LUSS Faciul	1.04223		1.03402		

Adjusted Losses and Loss Factors by Facility

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	DEMAND MW		SUMMAF	Y OF LOSSES	AND LOSS	FACTORS BY	DELIVERY VO	LTAGE	EXHIBIT 9
	SERVICE LEVEL	SALES MW	LOSSES	SECONDARY	PRIMARY	SUBSTATION	SUBTRANS	TRANSMISSION	PAGE 1 of 2
1 2 3 4 5	SERVICES SALES LOSSES INPUT EXPANSION FACTOR	941.30 <b>1.00751</b>	7.1	941.3 7.1 948.4					
6 7 8 9 10	SECONDARY SALES LOSSES INPUT EXPANSION FACTOR	1.00590	5.6	5.6 954.0					
11 12 13 14 15	LINE TRANSFORMER SALES LOSSES INPUT EXPANSION FACTOR	1.01781	17.0	17.0 971.0					
16 17 18 19 20 21	PRIMARY SECONDARY SALES LOSSES INPUT EXPANSION FACTOR	74.70 <b>1.01489</b>	15.6	971.0 14.5	74.7 1.1				
22 23 24 25 26 27	SUBSTATION PRIMARY SALES LOSSES INPUT EXPANSION FACTOR	0.0 <b>1.00622</b>	6.6	985.4 6.1 991.5	75.8 0.5 76.3				
28 29 30 31 32 33	SUB-TRANSMISSION DISTRIBUTION SUBS SALES LOSSES INPUT EXPANSION FACTOR	316.30 <b>1.01838</b>	20.8	724.3 13.3 737.6	75.0 1.4 76.4		316.3 5.8 322.1		
34 35 36 37 38 39 40	TRANSMISSION SUBTRANSMISSION DISTRIBUTION SUBS SALES LOSSES INPUT EXPANSION FACTOR	73.00 <b>1.04223</b>	52.9	523.7 259.5 33.1 817.6	54.2 1.3 2.3 57.9		322.1 13.6 335.7	73. 3. 76.	1
41	TOTALS LOSSES	CALCULATED	125.5	96.6	5.3		19.4	3.	1
42	% OF TOTAL	SCALED	125.5 100%	97.5 77.69%	5.5 4.38%		19.4 15.48%	3. 2.46%	
43 44	SALES % OF TOTAL	1,405.3 100.00%		941.3 66.98%	74.7 5.32%		316.3 22.51%	73. 5.199	
45	INPUT	1,530.8		1,038.8	80.2		335.7	76.	1
46	CUMMULATIVE EXPANSIO (from meter to syst			1.10354	1.07358	NA	1.06139	1.0422	3

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	ENERGY MWH		SUMMARY	OF LOSSE	S AND LOSS	FACTORS B	Y DELIVERY V	OLTAGE	EXHIBIT 9
	SERVICE LEVEL	SALES	LOSSES S	ECONDARY	PRIMARY	SUBSTATION	SUBTRANS	TRANSMISSION	PAGE 2 of 2
1 2 3 4 5	SERVICES SALES LOSSES INPUT EXPANSION FACTOR	3,602,434 <b>1.00493</b>	17,769	3,602,434 17,769 3,620,203					
6 7 8 9 10	SECONDARY SALES LOSSES INPUT EXPANSION FACTOR	1.00303	10,969	10,969 3,631,172					
11 12 13 14 15	LINE TRANSFORMER SALES LOSSES INPUT EXPANSION FACTOR	1.03095	112,376	112,376 3,743,548					
16 17 18 19 20 21	PRIMARY SECONDARY SALES LOSSES INPUT EXPANSION FACTOR	516,299.000 <b>1.00694</b>	29,544	3,743,548 25,963	516,299				
22 23 24 25 26 27	SUBSTATION PRIMARY SALES LOSSES INPUT EXPANSION FACTOR	0 <b>1.00657</b>	28,182	3,769,511 24,766 3,794,277	3,416				
28 29 30 31 32 33	SUB-TRANSMISSION DISTRIBUTION SUBS SALES LOSSES INPUT EXPANSION FACTOR	2,466,746	68,753	3,173,472 37,992 3,211,464	718		2,466,746 29,531 2,496,277		
34 35 36 37 38 39 40	TRANSMISSION SUBTRANSMISSION DISTRIBUTION SUBS SALES LOSSES INPUT EXPANSION FACTOR	526,918 <b>1.03482</b>	211,400	1,926,879 591,621 87,682 2,606,182	463,295 16,130		2,496,277 86,908 2,583,186	526,918 18,345	5
41 42	TOTALS LOSSES % OF TOTAL	Calculated Scaled	478,992 478,983 100%	317,517 315,620 66.29%	28,579		116,440 116,440		5
42 43 44	SALES % OF TOTAL	7,112,397 100.00%	10076	3,602,434 50.65%	516,299		2,466,746 34.68%	526,91	3
45	INPUT	7,591,380		3,918,054	544,878		2,583,186	545,263	3
46	CUMMULATIVE EXPANSION (from meter to syste			1.08761	1.05535	NA	1.04720	1.0348	2

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## Kentucky Power Company 2011 Analysis of System Losses

# **Appendix B**

# **Discussion of Hoebel Coefficient**



#### COMMENTS ON THE HOEBEL COEFFICIENT

The Hoebel coefficient represents an established industry standard relationship between peak losses and average losses and is used in a loss study to estimate energy losses from peak demand losses. H. F. Hoebel described this relationship in his article, "Cost of Electric Distribution Losses," <u>Electric Light and Power</u>, March 15, 1959. A copy of this article is attached.

Within any loss evaluation study, peak demand losses can readily be calculated given equipment resistance and approximate loading. Energy losses, however, are much more difficult to determine given their time-varying nature. This difficulty can be reduced by the use of an equation which relates peak load losses (demand) to average losses (energy). Once the relationship between peak and average losses is known, average losses can be estimated from the known peak load losses.

Within the electric utility industry, the relationship between peak and average losses is known as the loss factor. For definitional purposes, loss factor is the ratio of the average power loss to the peak load power loss, during a specified period of time. This relationship is expressed mathematically as follows:

(1) E A ) D	where: F <sub>LS</sub>	=	Loss Factor
(1) $F_{LS}$ . $A_{LS}$ ) $P_{LS}$	$A_{LS}$	=	Average Losses
	P <sub>LS</sub>	=	Peak Losses

The loss factor provides an estimate of the degree to which the load loss is maintained throughout the period in which the loss is being considered. In other words, loss factor is the ratio of the actual kWh losses incurred to the kWh losses which would have occurred if full load had continued throughout the period under study.

Examining the loss factor expression in light of a similar expression for load factor indicates a high degree of similarity. The mathematical expression for load factor is as follows:

	where: $F_{LD}$ =	Load Factor
(2) $F_{LD}$ . $A_{LD}$ ) $P_{LD}$	$A_{LD} =$	Average Load
	$P_{LD}$ =	Peak Load

This load factor result provides an estimate of the degree to which the load loss is maintained throughout the period in which the load is being considered. Because of the similarities in definition, the loss factor is sometimes called the "load factor of losses." While the definitions are similar, a strict equating of the two factors cannot be made. There does exist, however, a relationship between these two factors which is dependent upon the shape of the load duration curve. Since resistive losses vary as the square of the load, it can be shown mathematically that the loss factor can vary between the extreme limits of load factor and load factor squared. The relationship between load factor and loss factor has become an industry standard and is as follows:



2	where: $F_{LS}$ = Loss Factor
(3) $F_{LS}$ . $H^*F_{LD}^2$ + (1-H)* $F_{LD}$	$F_{LD}$ = Load Factor
	H = Hoebel Coeff

As noted in the attached article, the suggested value for H (the Hoebel coefficient) is 0.7. The exact value of H will vary as a function of the shape of the utility's load duration curve. In recent years, values of H have been computed directly for a number of utilities based on EEI load data. It appears on this basis, the suggested value of 0.7 should be considered a lower bound and that values approaching unity may be considered a reasonable upper bound. Based on experience, values of H have ranged from approximately 0.85 to 0.95. The standard default value of 0.9 is generally used.

Inserting the Hoebel coefficient estimate gives the following loss factor relationship using Equation (3):

(4)  $F_{LS}$ .  $0.90*F_{LD}^2 + 0.10*F_{LD}$ 

Once the Hoebel constant has been estimated and the load factor and peak losses associated with a piece of equipment have been estimated, one can calculate the average, or energy losses as follows:

(5) 
$$A_{LS} \cdot P_{LS} * [H*F_{LD}^2 + (1-H)*F_{LD}]$$
 where:  $A_{LS} = Average Losses$   
 $P_{LS} = Peak Losses$   
 $H = Hoebel Coefficient$   
 $F_{LD} = Load Factor$ 

Loss studies use this equation to calculate energy losses at each major voltage level in the analysis.

