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KENTUCKY POWER COMPANY

2011 Analysis of System Losses

April 2013

Prepared by:



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April 17, 2013

Mr. David M. Roush Director Regulatory Pricing & Analysis American Electric Power 1 Riverside Plaza Columbus, OH 43215

Mr. Mark P. Gilbert Director Economic Forecasting American Electric Power 212 East 6th Street Tulsa, OK 74119

RE: 2011 LOSS ANALYSIS

Dear Messrs. Roush and Gilbert:

Transmitted herewith are the results of the 2011 Analysis of System Losses for the Kentucky Power Company's (KPCO) power system. Our analysis develops cumulative expansion factors (loss factors) for both demand (peak/kW) and energy (average/kWh) losses by discrete voltage levels applicable to metered sales data. Our analysis considers only technical losses in arriving at our final recommendations.

On behalf of MAC, we appreciate the opportunity to assist you in performing the loss analysis contained herein. The level of detailed load research and sales data by voltage level, coupled with a summary of power flow data and power system model, forms the foundation for determining reasonable and representative power losses on the KPCO system. Our review of these data and calculated loss results support the proposed loss factors as presented herein for your use in various cost of service, rate studies, and demand analyses.

Should you require any additional information, please let us know at your earliest convenience.

Sincerely,

concer

Paul M. Normand Principal

Enclosure PMN/rjp

Kentucky Power Company 2011 Analysis of System Losses

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1.0 EXECUTIVE SUMMARY

This report presents Kentucky Power Company's (KPCO) 2011 Analysis of System Losses for the power systems as performed by Management Applications Consulting, Inc. (MAC). The study developed separate demand (kW) and energy (kWh) loss factors for each voltage level of service in the power system for KPCO. The cumulative loss factor results by voltage level, as presented herein, can be used to adjust metered kW and kWh sales data for losses in performing cost of service studies, determining voltage discounts, and other analyses which may require a loss adjustment.

The procedures used in the overall loss study were similar to prior studies and emphasized the use of "in house" resources where possible. To this end, extensive use was made of the Company's peak hour power flow data and transformer plant investments in the model. In addition, measured and estimated load data provided a means of calculating reasonable estimates of losses by using a "top-down" and "bottom-up" procedure. In the "top-down" approach, losses from the high voltage system, through and including distribution substations, were calculated along with power flow data, conductor and transformer loss estimates, and metered sales.

At this point in the analysis, system loads and losses at the input into the distribution substation system are known with reasonable accuracy. However, it is the remaining loads and losses on the distribution substations, primary system, secondary circuits, and services which are generally difficult to estimate. Estimated and actual Company load data provided the starting point for performing a "bottom-up" approach for calculating the remaining distribution losses. Basically, this "bottom-up" approach develops line loadings by first determining loads and losses at each level beginning at a customer's meter service entrance and then going through secondary lines, line transformers, primary lines and finally distribution substation. These distribution system loads and associated losses are then compared to the initial calculated input into Distribution Substation loadings for reasonableness prior to finalizing the loss factors. An overview of the loss study is shown on Figure 1.

Table 1, below, provides the final results from Appendix A for the 2011 calendar year. Exhibits 8 and 9 of Appendix A present a more detailed analysis of the final calculated summary results of losses by segments and delivery voltage of the power system. The following Table 1 cumulative loss expansion factors are applicable only to metered sales at the point of receipt for adjustment to the power system's input level.



Kentucky Power Company 2011 Analysis of System Losses

Loss Factors at Sales Level, Calendar Year 2011

Voltage Level <u>of Service</u>	Total <u>KPCO</u>	Distribution <u>Only</u>
Demand (kW)		
Transmission ¹	1.04223	_
Subtransmission	1.06139	1.01838
Primary Lines	1.07358	1.03008
Secondary	1.10354	1.05883
Energy (kWh)		
Transmission ¹	1.03482	_
Subtransmission	1.04720	1.01197
Primary Lines	1.05535	1.01985
Secondary	1.08761	1.05102
Losses – Net System Input ²	6.31%MWh	
- 1	8.20%MW	
Losses – Net System Output ³	6.73%MWh	
	8.93%MW	

Composite Loss Factors at Metered Sales Level

	MW	MWH
Retail	1.08990	1.06774
Wholesale	1.04797	1.03845

The loss factors presented in the Delivery Only column of Table 1 are the Total KPCO loss factors divided by the transmission loss factor in order to remove these losses from each service level loss factor. For example, the secondary distribution demand loss factor of 1.05883 includes the recovery of all remaining non-transmission losses from the subtransmission, distribution substation, primary lines, line transformers, secondary conductors and services.

The net system input shown in Table 1 represents the MWh losses of 6.31% for the total KPCO load using calculated losses divided by the associated input energy to the system. The 6.73% represents the same losses using system output instead of input as a reference. The net system output reference shown in Table 1 represents MWh losses of 6.73% and MW losses of 8.93%. These results use the appropriate total losses for each but are divided by system output or sales. These calculations are all based on the data and results shown on Exhibits 1, 7 and 9 of the study.

³ Net system output uses losses divided by output or sales data as a reference.



¹ Reflects results for 765 kV, 345 kV 161 kV, and 138 kV.

² Net system input equals firm sales plus losses, Company use less non-requirement sales and related losses. See Appendix A, Exhibit 1, for their calculations.

Due to the very nature of losses being primarily a function of equipment loadings, the loss factor derivations for any voltage level must consider both the load at that level plus the loads from lower voltages and their associated losses. As a result, cumulative losses on losses equates to additional load at higher levels along with future changes (+ or -) in loads throughout the power system. It is therefore important to recognize that losses are multiplicative in nature (future) and not additive (test year only) for all future years to ensure total recovery based on prospective fixed loss factors for each service voltage.

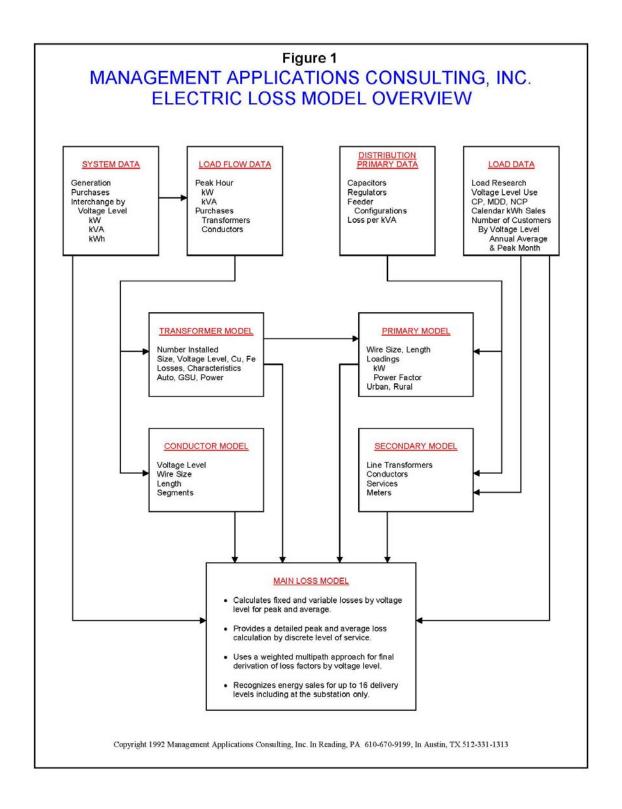
The derivation of the cumulative loss factors shown in Table 1 have been detailed for all electrical facilities in Exhibit 9, page 1 for demand and page 2 for energy. Beginning on line 1 of page 1 (demand) under the secondary column, metered sales are adjusted for service losses on lines 3 and 4. This new total load (with losses) becomes the load amount for the next higher facilities of secondary conductors and their loss calculations. This process is repeated for all the installed facilities until the secondary sales are at the input level (line 45). The final loss factor for all delivery voltages using this same process is shown on line 46 and Table 1 for demand. This procedure is repeated in Exhibit 9, page 2, for the energy loss factors.

The loss factor calculation is simply the input required (line 45) divided by the metered sales (line 43).

An overview of the loss study is shown on Figure 1 on the next page. Figure 2 simply illustrates the major components that must be considered in a loss analysis.

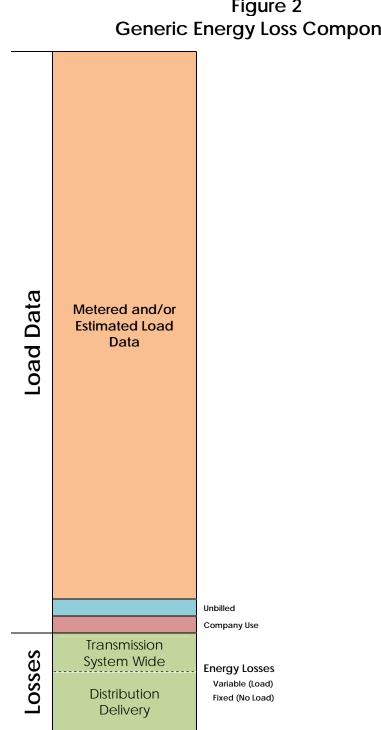


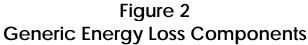
Kentucky Power Company 2011 Analysis of System Losses





Kentucky Power Company 2011 Analysis of System Losses







2.0 INTRODUCTION

This report of the 2011 Analysis of System Losses for the Kentucky Power Company provides a summary of results, conceptual background or methodology, description of the analyses, and input information related to the study.

2.1 **Conduct of Study**

Typically, between five to ten percent of the total kWh requirements of an electric utility is lost or unaccounted for in the delivery of power to customers. Investments must be made in facilities which support the total load which includes losses or unaccounted for load. Revenue requirements associated with load losses are an important concern to utilities and regulators in that customers must equitably share in all of these cost responsibilities. Loss expansion factors are the mechanism by which customers' metered demand and energy data are mathematically adjusted to the generation or input level (point of reference) when performing cost and revenue calculations.

An acceptable accounting of losses can be determined for any given time period using available engineering, system, and customer data along with empirical relationships. This loss analysis for the delivery of demand and energy utilizes such an approach. A microcomputer loss model⁴ is utilized as the vehicle to organize the available data, develop the relationships, calculate the losses, and provide an efficient and timely avenue for future updates and sensitivity analyses. Our procedures and calculations are similar with prior loss studies, and they rely on numerous databases that include customer statistics and power system investments.

Company personnel performed most of the data gathering and data processing efforts and checked for reasonableness. MAC provided assistance as necessary to construct databases, transfer files, perform calculations, and check the reasonableness of results. A review of the preliminary results provided for additions to the database and modifications to certain initial assumptions based on available data. Efforts in determining the data required to perform the loss analysis centered on information which was available from existing studies or reports within the Company. From an overall perspective, our efforts concentrated on five major areas:

- 1. System information concerning peak demand and annual energy requirements by voltage level,
- 2. High voltage power system power flow data and associated loss calculations,
- 3. Distribution system primary and secondary loss calculations,
- 4. Derivation of fixed and variable losses by voltage level, and
- 5. Development of final cumulative expansion factors at each voltage for peak demand (kW) and annual energy (kWh) requirements at the point of delivery (meter).

⁴Copyright by Management Applications Consulting, Inc.



2.2 Electric Power Losses

Losses in power systems consist of primarily technical losses with a much smaller level of non-technical losses.

Technical Losses

Electrical losses result from the transmission of energy over various electrical equipment. The largest component of these losses is power dissipation as a result of varying loading conditions and are oftentimes called load losses which are proportional to the square of the current (I^2R). These losses can be as high as 75% of all technical losses. The remaining losses are called no-load and represent essentially fixed (constant) energy losses throughout the year. These no-load losses represent energy required by a power system to energize various electrical equipment regardless of their loading levels. The major portion of no-load losses consists of core or magnetizing energy related to installed transformers throughout the power system.

Non-Technical Losses

These are unaccounted for energy losses that are related to energy theft, metering, non-payment by customers, and accounting errors. Losses related to these areas are generally very small and can be extremely difficult and subjective to quantify. Our efforts generally do not develop any meaningful level as appropriate because we assume that improving technology and utility practices have minimized these amounts.

2.3 Description of Model

The loss model is a customized applications model, constructed using the Excel software program. Documentation consists primarily of the model equations at each cell location. A significant advantage of such a model is that the actual formulas and their corresponding computed values at each cell of the model are immediately available to the analyst.

A brief description of the three (3) major categories of effort for the preparation of each loss model is as follows:

• Main sheet which contains calculations for all primary and secondary losses, summaries of all conductor and transformer calculations from other sheets discussed below, output reports and supporting results.



- Transformer sheet which contains data input and loss calculations for each distribution substation and high voltage transformer. Separate iron and copper losses are calculated for each transformer by identified type.
- Conductor sheet containing summary data by major voltage level as to circuit miles, loading assumptions, and kW and kWh loss calculations. Separate loss calculations for each line segment were made using the Company's power flow data by line segment and summarized by voltage level in this model.

Appendix A presents a detailed loss study result which derives the loss factors for the Company's system-wide power system. Appendix A, Exhibits 8 and 9, presents the final detailed summary results of the demand and energy losses for each major portion of the total KPCO power system.



3.0 METHODOLOGY

3.1 Background

The objective of a Loss Study is to provide a reasonable set of energy (average) and demand (peak) loss expansion factors which account for system losses associated with the transmission and delivery of power to each voltage level over a designated period of time. The focus of this study is to identify the difference between total energy inputs and the associated sales with the difference being equitably allocated to all delivery levels. Several key elements are important in establishing the methodology for calculating and reporting the Company's losses. These elements are:

- Selection of voltage level of services,
- Recognition of losses associated with conductors, transformations, and other electrical equipment/components within voltage levels,
- Identification of customers and loads at various voltage levels of service,
- Review of generation or net power supply input at each level for the test period studied, and
- Analysis of kW and kWh sales by voltage levels within the test period.

The three major areas of data gathering and calculations in the loss analysis were as follows:

- 1. System Information (monthly and annual)
 - MWH generation and MWH sales.
 - Coincident peak estimates and net power supply input from all sources and voltage levels.
 - Customer load data estimates from available load research information, adjusted MWH sales, and number of customers in the customer groupings and voltage levels identified in the model.
 - System default values, such as power factor, loading factors, and load factors by voltage level.



- 2. High Voltage System
 - Conductor information was summarized from a database by the Company which reflects the transmission system by voltage level. Extensive use was made of the Company's power flow data with the losses calculated and incorporated into the final loss calculations.
 - Transformer information was developed in a database to model transformation at each voltage level. Substation power, step-up, and auto transformers were individually identified along with any operating data related to loads and losses.
 - Power flow data of peak condition was the primary source of equipment loadings and derivation of load losses in the high voltage loss calculations.
- 3. Distribution System
 - Distribution Substations Data was developed for modeling each substation as to its size and loading. Loss calculations were performed from this data to determine load and no load losses separately for each transformer.
 - Primary lines Line loading and loss characteristics for several representative primary circuits were obtained from the Company. These loss results developed kW loss per MW of load and a composite average was calculated to derive the primary loss estimate.
 - Line transformers Losses in line transformers were based on each customer service group's size, as well as the number of customers per transformer. Accounting and load data provided the foundation with which to model the transformer loadings and to calculate load and no load losses.
 - Secondary network Typical secondary networks were estimated for conductor sizes, lengths, loadings, and customer penetration for residential and small general service customers.
 - Services Typical services were estimated for each secondary service class of customers identified in the study with respect to type, length, and loading.



The loss analysis was thus performed by constructing the model in segments and subsequently calculating the composite until the constraints of peak demand and energy were met:

- Information as to the physical characteristics and loading of each transformer and conductor segment was modeled.
- Conductors, transformers, and distribution were grouped by voltage level, and unadjusted losses were calculated.
- The loss factors calculated at each voltage level were determined by "compounding" the per-unit losses. Equivalent sales at the supply point were obtained by dividing sales at a specific level by the compounded loss factor to determine losses by voltage level.
- The resulting demand and energy loss expansion factors were then used to adjust all sales to the generation or input level in order to estimate the difference.
- Reconciliation of kW and kWh sales by voltage level using the reported system kW and kWh was accomplished by adjusting the initial loss factor estimates until the mismatch or difference was eliminated.

3.2 Calculations and Analysis

This section provides a discussion of the input data, assumptions, and calculations performed in the loss analysis. Specific appendices have been included in order to provide documentation of the input data utilized in the model.

3.2.1 Bulk, Transmission and Subtransmission Lines

The transmission and subtransmission line losses were calculated based on a modeling of unique voltage levels identified by the Company's power flow data and configuration for the entire integrated KPCO Power System. Specific information as to length of line, type of conductor, voltage level, peak load, maximum load, etc., were provided based on Company records and utilized as data input in the loss model.

Actual MW and MVA line loadings were based on KPCO's peak loading conditions. Calculations of line losses were performed for each line segment separately and combined by voltage levels for reporting purposes as shown in the Discussion of Results (Section 4.0) of this report. The loss calculations consisted of determining a circuit current value based on MVA line loadings and evaluating the I^2R results for each line segment.



After system coincident peak hour losses were identified for each voltage level, a separate calculation was then made to develop annual average energy losses based on a loss factor approach. Load factors were determined for each voltage level based on system and customer load information. An estimate of the Hoebel coefficient (see Appendix B) was then used to calculate energy losses for the entire period being analyzed. The results are presented in Section 4.0 of this report.

3.2.2 Transformers

The transformer loss analysis required several steps in order to properly consider the characteristics associated with various transformer types; such as, step-up, auto transformers, distribution substations, and line transformers. In addition, further efforts were required to identify both iron and copper losses within each of these transformer types in order to obtain reasonable peak (kW) and average energy (kWh) losses. While iron losses were considered essentially constant for each hour, recognition had to be made for the varying degree of copper losses due to hourly equipment loadings.

Standardized test data tables were used to represent no load (fixed) and full load losses for different types and sizes of transformers. This test data was incorporated into the loss model to develop relationships representing copper and iron losses for the transformer loss calculation. These results were then totaled by various groups, as identified and discussed in Section 4.0.

The remaining miscellaneous losses considered in the loss study consisted of several areas which do not lend themselves to any reasonable level of modeling for estimating their respective losses and were therefore lumped together into a single loss factor of 0.10%. The typical range of values for these losses is from 0.10% to 0.25%, and we have assumed the lower value to be conservative at this time. The losses associated with this loss factor include bus bars, unmetered station use, and grounding transformers.



3.2.3 Distribution System

The load data at the substation and customer level, coupled with primary and secondary network information, was sufficient to model the distribution system in adequate detail to calculate losses.

Primary Lines

Primary line loadings take into consideration the available distribution load along with the actual customer loads including losses. Primary line loss estimates were prepared by the Company for use in this loss study. These estimates considered loads per substation, voltage levels, loadings, total circuit miles, wire size, and single- to three-phase investment estimates. All of these factors were considered in calculating the actual demand (kW) and energy (kWh) for the primary system.

Line Transformers

Losses in line transformers were determined based on typical transformer sizes for each secondary customer service group and an estimated or calculated number of customers per transformer. Accounting records and estimates of load data provided the necessary database with which to model the loadings. These calculations also made it possible to determine separate copper and iron losses for distribution line transformers, based on a table of representative losses for various transformer sizes.

Secondary Line Circuits

A calculation of secondary line circuit losses was performed for loads served through these secondary line investments. Estimates of typical conductor sizes, lengths, loadings and customer class penetrations were made to obtain total circuit miles and losses for the secondary network. Customer loads which do not have secondary line requirements were also identified so that a reasonable estimate of losses and circuit miles of these investments could be made.

Service Drops and Meters

Service drops were estimated for each secondary customer reflecting conductor size, length and loadings to obtain demand losses. A separate calculation was also performed using customer maximum demands to obtain kWh losses. Meter loss estimates were also made for each customer and incorporated into the calculations of kW and kWh losses included in the Summary Results.



Kentucky Power Company 2011 Analysis of System Losses

4.0 DISCUSSION OF RESULTS

A brief description of each Exhibit provided in Appendix A follows:

Exhibit 1 - Summary of Company Data

This exhibit reflects system information used to determine percent losses and a detailed summary of kW and kWh losses by voltage level. The loss factors developed in Exhibit 7 are also summarized by voltage level.

Exhibit 2 - Summary of Conductor Information

A summary of MW and MWH load and no load losses for conductors by voltage levels is presented. The sum of all calculated losses by voltage level is based on input data information provided in Appendix A. Percent losses are based on equipment loadings.

Exhibit 3 - Summary of Transformer Information

This exhibit summarizes transformer losses by various types and voltage levels throughout the system. Load losses reflect the copper portion of transformer losses while iron losses reflect the no load or constant losses. MWH losses are estimated using a calculated loss factor for copper and the test year hours times no load losses.

Exhibit 4 - Summary of Losses Diagram (2 Pages)

This loss diagram represents the inputs and output of power at system peak conditions. Page 1 details information from all points of the power system and what is provided to the distribution system for primary loads. This portion of the summary can be viewed as a "top down" summary into the distribution system.

Page 2 represents a summary of the development of primary line loads and distribution substations based on a "bottom up" approach. Basically, loadings are developed from the customer meter through the Company's physical investments based on load research and other metered information by voltage level to arrive at MW and MVA requirements during peak load conditions by voltage levels.

Exhibit 5 - Summary of Sales and Calculated Losses

Summary of Calculated Losses represents a tabular summary of MW and MWH load and no load losses by discrete areas of delivery within each voltage level. Losses have been identified and are derived based on summaries obtained from Exhibits 2 and 3 and losses associated with meters, capacitors and regulators.



Kentucky Power Company 2011 Analysis of System Losses

Exhibit 6 - Development of Loss Factors, Unadjusted

This exhibit calculates demand and energy losses and loss factors by specific voltage levels based on sales level requirements. The actual results reflect loads by level and summary totals of losses at that level, or up to that level, based on the results as shown in Exhibit 5. Finally, the estimated values at generation are developed and compared to actual generation to obtain any difference or mismatch.

Exhibit 7 - Development of Loss Factors, Adjusted

The adjusted loss factors are the results of adjusting Exhibit 6 for any difference. All differences between estimated and actual are prorated to each level based on the ratio of each level's total load plus losses to the system total. These new loss factors reflect an adjustment in losses due only to the kW and kWh mismatch.

Exhibit 8 – Adjusted Losses and Loss Factors by Facility

These calculations present an expanded summary detail of Exhibit 7 for each segment of the power system with respect to the flow of power and associated losses from the receipt of energy at the meter to the generation for the KPCO power system.

Exhibit 9 – Summary of Losses by Delivery Voltage

These calculations present a reformatted summary of losses presented in Exhibits 7 and 8 by power system delivery segment as calculated by voltage level of service based on reported metered sales.



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Kentucky Power Company 2011 Analysis of System Losses

Appendix A

Results of 2011 KPCO Integrated Power System Loss Analysis



KENTUCKY POWER

EXHIBIT 1

SUMMARY OF COMPANY DATA

ANNUAL PEAK	1,531 MW
ANNUAL SYSTEM INPUT	7,591,389 MWH
ANNUAL SALES OUTPUT	7,112,397 MWH
SYSTEM LOSSES @ INPUT SYSTEM LOSSES @ OUTPUT	478,992 or 6.31% 478,992 or 6.73%
SYSTEM LOAD FACTOR	56.6%

SUMMARY OF LOSSES - OUTPUT RESULTS

SERVICE	KV	N	IW Input	% TOTAL	MWH Input	% TOTAL
TRANS	765,345	52.9		42.15%	211,400	44.13%
	161,138		3.45%		2.78%	
		~~~~			00 750	44.050/
SUBTRANS	69,46,34	20.8	1.36%	16.54%	68,753 0.91%	14.35%
			1.30%		0.91%	
PRIMARY	34,12,1	22.2		17.67%	57,725	12.05%
			1.45%		0.76%	
SECONDARY	120/240,to,477	29.7	1 0 4 9 /	23.64%	141,114	29.46%
			1.94%		1.86%	
TOTAL		125.5		100.00%	478,992	100.00%
			8.20%		6.31%	

#### SUMMARY OF LOSS FACTORS

SERVICE	KV	CUMMUI DEMAN d	EXPANSION F ENERGY e	N FACTORS RGY (Annual) 1/e		
TOT TRANS	765,345 161,138	1.04223	0.95948	1.03482	0.96636	
SUBTRAN	69,46,34	1.06139	0.94216	1.04720	0.95492	
PRIMARY	34,12,1	1.07358	0.93146	1.05535	0.94755	
SECONDARY	120/240,to,477	1.10354	0.90617	1.08761	0.91944	

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#### KENTUCKY POWER 2011 LOSS ANALYSIS

#### SUMMARY OF CONDUCTOR INFORMATION

DESCRIPTION		С	IRCUIT	LOA	DING	M\	VLOSSES				MWH LOSSES	
		1	MILES	% RA	TING	LOAD	NO LOAD	TOTAL		LOAD	NO LOAD	TOTAL
BULK	765 KV C	R GREATER							[			
TIE LINES			0.0		0.00%	0.000	0.000	0.000		0	0	0
BULK TRANS			<u>257.5</u>		0.00%	<u>11.777</u>	<u>2.844</u>	<u>14.621</u>		<u>71,988</u>	<u>24,912</u>	<u>96,900</u>
SUBTOT			257.5			11.777	2.844	14.621		71,988	24,912	96,900
TRANS	138 KV	то 7	765.00	KV								
TIE LINES			0	)	0.00%	0.000	0.000	0.000		0	0	0
TRANS1	161 KV		56.5		0.00%	4.361	0.040	4.402		14,202	352	14,553
TRANS2	<u>138 KV</u>		<u>338.0</u>		0.00%	<u>27.416</u>	<u>0.166</u>	27.582		80,948	<u>1,458</u>	82,406
SUBTOT	100 111		<u>394.6</u>		0.0070	31.777	0.207	31.984		95,150	1,810	<u>96,960</u>
SUBTRANS	35 KV	то	138	KV								
TIE LINES			0	)	0.00%	0.000	0.000	0.000		0	0	0
SUBTRANS1	69 KV		425.0		0.00%	13.669	0.000	13.669		40,500	0	40,500
SUBTRANS2	46 KV		167.3		0.00%	3.794	0.000	3.794		11,243	0	11,243
SUBTRANS3	<u>35 KV</u>		<u>3.2</u>		<u>0.00%</u>	<u>0.010</u>	<u>0.006</u>	<u>0.016</u>		<u>30</u>	<u>54</u> 54	<u>83</u>
SUBTOT			595.4			17.473	0.006	17.479		51,772	54	51,826
PRIMARY LINES			8,180			13.136	0.000	13.136		25,107	0	25,107
SECONDARY LINES			2,367			4.736	0.000	4.736		9,354	0	9,354
SERVICES			3,147			5.622	0.364	5.985		11,969	3,184	15,153
TOTAL			14,941			84.521	3.420	87.941		265,340	29,960	295,300

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#### KENTUCKY POWER 2011 LOSS ANALYSIS

IMMARY	OF TRANS	SFORMER	INFORMATIO	ON

DESCRIPTION							N 4) / A						
DESCRIPTION		KV CAPA VOLTAGE	MVA	NUMBER TRANSFMR	AVERAGE SIZE	LOADING %	MVA LOAD	LOAD	MW LOSSES - NO LOAD	TOTAL	LOAD	MWH LOSSES NO LOAD	TOTAL
BULK STEP-UP		765	1,500.0	3	500.0	3.39%	51	0.010	0.662	0.672	30	5,795	5,824
BULK - BULK			0.0	0	0.0	0.00%	0	0	0.000	0.000	0	0	0
BULK - TRANS1		161	0.0	0	0.0	0.00%	0	0.000	0.000	0.000	0	0	0
BULK - TRANS2		138	0.0	0	0.0	0.00%	0	0.000	0.000	0.000	0	0	0
RANS1 STEP-UP		161	950.0	1	950.0	85.71%	814	1.599	0.448	2.047	4,433	3,672	8,105
RANS1 - TRANS2		138	735.0	4	183.8	77.68%	571	0.589	0.606	1.195	1,745	5,313	7,058
RANS1-SUBTRANS1		69	54.0	1	54.0	116.02%	63	0.131	0.056	0.187	716	487	1,204
FRANS1-SUBTRANS2		46	0.0	0	0.0	0.00%	0	0.000	0.000	0.000	0	0	0
TRANS1-SUBTRANS3		35	0.0	0	0.0	0.00%	0	0.000	0.000	0.000	0	0	0
TRANS2 STEP-UP		138	354.0	3	118.0	87.60%	310	1.057	0.328	1.385	3,004	2,743	5,747
TRANS2-SUBTRANS1		69	849.0	15	56.6	95.50%	811	1.262	0.888	2.150	8,326	7,781	16,107
TRANS2-SUBTRANS2		46	75.0	2	37.5	97.14%	73	0.286	0.081	0.367	815	708	1,524
TRANS2-SUBTRANS3		35	57.0	2	28.5	24.35%	14	0.021	0.062	0.083	42	544	586
SUBTRAN1 STEP-UP		69	0.0	0	0.0	0.00%	0	0.000	0.000	0.000	0	0	0
SUBTRAN2 STEP-UP		46	0.0	0	0.0	0.00%	0	0.000	0.000	0.000	0	0	0
SUBTRAN3 STEP-UP		35	0.0	0	0.0	0.00%	0	0.000	0.000	0.000	0	0	0
SUBTRAN1-SUBTRAN		46	24.0	2	12.0	82.91%	20	0.073	0.031	0.104	221	275	496
SUBTRAN1-SUBTRAN		35	0.0	0	0.0	0.00%	0	0.000	0.000	0.000	0	0	0
SUBTRAN2-SUBTRAN	3	35	0.0	0	0.0	0.00%	0	0.000	0.000	0.000	0	0	0
	—					D	ISTRIBUTION S	UBSTATIONS					
TRANS1 -	161	33	24.0	2	12.0	88.25%	21	0.084	0.031	0.116	175	275	451
TRANS1 -	161	12	0.0	0	0.0	0.00%	0	0.000	0.000	0.000	0	0	0
TRANS1 -	161	1	0.0	0	0.0	0.00%	0	0.000	0.000	0.000	0	0	0
FRANS2 -	138	33	285.0	12	23.8	66.92%	191	0.534	0.332	0.865	1,113	2,906	4,019
FRANS2 -	138	12	67.0	4	16.8	80.87%	54	0.179	0.083	0.261	373	724	1,097
FRANS2 -	138	1	0.0	0	0.0	0.00%	0	0.000	0.000	0.000	0	0	0
SUBTRAN1-	69	33	209.0	12	17.4	82.33%	172	0.558	0.257	0.816	1,165	2,252	3,417
SUBTRAN1-	69	12	620.5	54	11.5	76.80%	477	1.786	0.825	2.611	3,725	7,230	10,955
SUBTRAN1-	69	1	15.0	2	7.5	10.79%	2	0.001	0.024	0.025	2	209	211
SUBTRAN2-	46	33	87.0	4	21.8	80.83%	70	0.207	0.102	0.309	432	893	1,325
SUBTRAN2-	46	12	139.3	13	10.7	63.91%	89	0.335	0.191	0.526	699	1,676	2,375
SUBTRAN2-	46	1	1.0	1	1.0	23.98%	0	0.000	0.002	0.002	1	18	18

35

35

35

33

12

1

0.0

5.0

0.0

21.3

3,179.4

9,251

0

1

0

4

98,137

98,279

0.0

5.0

0.0

5.3

32.4

SUBTRAN3-

SUBTRAN3-

SUBTRAN3-

TOTAL

PRIMARY - PRIMARY

LINE TRANSFRMR

0.00%

0.00%

54.60%

33.22%

116.20%

0

6

0

12

1,056

0.000

0.042

0.000

0.042

4.227

13.024

0.000

0.009

0.000

0.037

10.149

15.204

0.000

0.051

0.000

0.079

14.376

28.228

______ _____

0

0

88

88

6,931

34,123

0

77

321

88,902

132,801

0

0

0

165

408

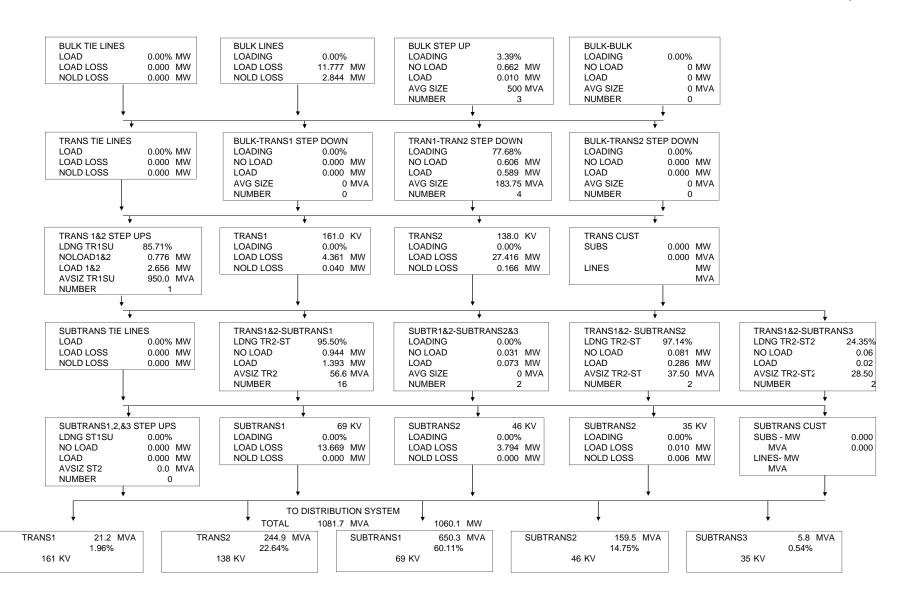
95,833

166,925

#### KENTUCKY POWER 2011 LOSS ANALYSIS

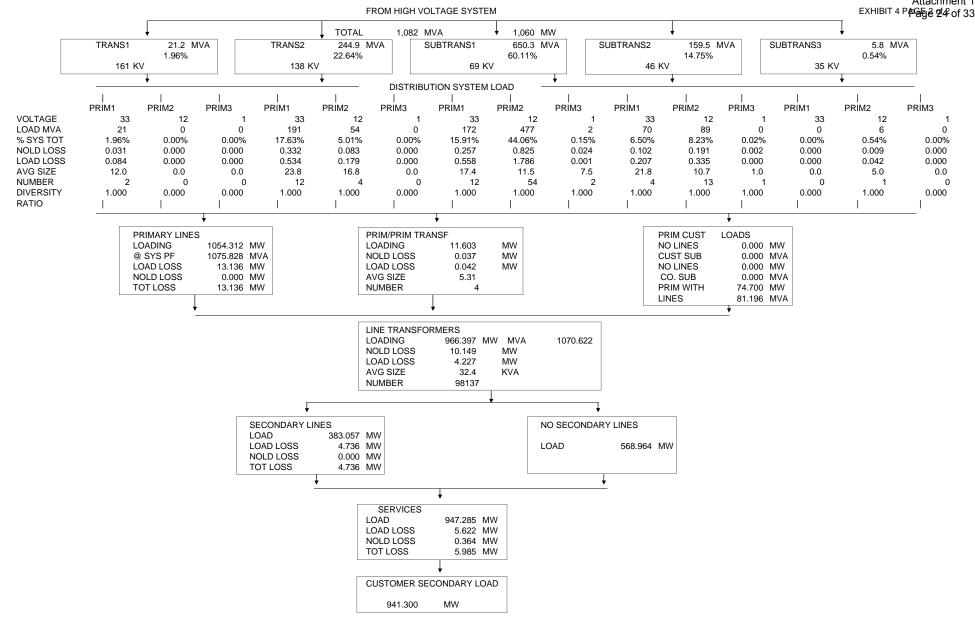
1530.76 MW

SUMMARY OF LOSSES DIAGRAM - DEMAND MODEL - SYSTEM PEAK



KPSC Case No. 2015-00271 Sierra Club's Initial Data Requests Dated October 28, 2015 Item No. 9 Attachment 1

#### KENTUCKY POWER 2011 LOSS ANALYSIS



KPSC Case No. 2015-00271 Sierra Club's Initial Data Requests Dated October 28, 2015 Item No. 9 Attachment 1 EX**Plage** 25 of 33

#### KENTUCKY POWER 2011 LOSS ANALYSIS

#### SUMMARY of SALES and CALCULATED LOSSES

LOSS # AND LEVEL	MW LOAD	NO LOAD +	LOAD =	TOT LOSS	EXP FACTOR	CUM EXP FAC	MWH LOAD	NO LOAD +	LOAD =	TOT LOSS	EXP FACTOR	CUM EXP FAC
1 BULK XFMMR	0.0	0.00	0.00	0.00	0.000000	0.000000	0	0	0	0	0	0
2 BULK LINES	49.9	3.51	11.79	15.29	1.441882	1.441882	244,789	30,707	72,018	102,725	1.7230845	1.7230845
3 TRANS1 XFMR	0.0	0.00	0.00	0.00	0.000000	0.000000	0	0	0	0	0.0000000	0.0000000
4 TRANS1 LINES	798.0	0.49	5.96	6.45	1.008147	1.008147	4,562,176	4,024	18,634	22,658	1.0049913	1.0049913
5 TRANS2TR1 SD	559.5	0.61	0.59	1.20	1.002141	1.010305	2,744,683	5,313	1.745	7,058	1.0025780	1.0075822
6 TRANS2BLK SD	0.0	0.00	0.00	0.00	0.000000	0.000000	0	0	0	0	0.0000000	0.0000000
7 TRANS2 LINES	1.213.4	0.49	28.47	28.97	1.024457	1.029325	5,920,714	4.201	83.952	88.153	1.0151140	1.0186820
TOTAL TRAN	1,305.0	5.09	46.81	51.90	1.041421	1.041421	6,283,446	44,244	176,349	220,594	1.0363845	1.0363845
8 STR1BLK SD	,						-,, -	,	-,	-,		
9 STR1T1 SD	61.4	0.06	0.13	0.19	1.003049	1.044596	301.204	487	716	1.204	1.0040123	1.0405428
10 SRT1T2 SD	794.6	0.89	1.26	2.15	1.002713	1.044247	3,897,990	7,781	8,326	16,107	1.0041494	1.0406848
11 SUBTRANS1 LINES	981.0	0.00	13.67	13.67	1.014130	1.056136	5,199,194	0	40,500	40,500	1.0078508	1.0445209
	00110	0.00					0,100,101	Ū	10,000	.0,000		
12 STR2T1 SD	0.0	0.00	0.00	0.00	0.000000	0.000000	0	0	0	0	0.0000000	0.0000000
13 STR2T2 SD	71.4	0.08	0.29	0.37	1.005164	1.046799	350,260	708	815	1,524	1.0043692	1.0409126
14 STR2S1 SD	19.5	0.03	0.07	0.10	1.005385	1.061823	95,659	275	221	496	1.0052158	1.0499690
15 SUBTRANS2 LINES	160.9	0.00	3.79	3.79	1.024152	1.066573	695,919	0	11,243	11,243	1.0164204	1.053402
	100.0	0.00	0.10	0.10	1.02 1102	1.000010	000,010	Ŭ	11,210	11,210	1.0101201	1.000 102
16 STR3T1 SD	0.0	0.00	0.00	0.00	0.000000	0.000000	0	0	0	0	0.0000000	0.0000000
17 STR3T2 SD	13.6	0.06	0.02	0.08	1.006146	1.047821	66,716	544	42	586	1.0088600	1.0455668
18 STR3S1 SD	0.0	0.00	0.00	0.00	0.000000	0.000000	0	0	0	0	0.0000000	0.0000000
19 STR3S2 SD	0.0	0.00	0.00	0.00	0.000000	0.000000	0	0	0	0	0.0000000	0.0000000
20 SUBTRANS3 LINES	13.6	0.01	0.01	0.02	1.001187	1.042657	66,716	54	30	83	1.0012492	1.0376792
21 SUBTRANS TOTAL	1,150.0	1.12	19.25	20.37	1.018033	1.060201	5,811,708	9,850	61,893	71,743	1.0124989	1.049338
DISTRIBUTION SUBST												
TRANS1	20.8	0.03	0.08	0.12	1.005598	1.047251	83,968	275	175	451	1.0053984	1.0419793
TRANS2	240.0	0.41	0.71	1.13	1.004717	1.046333	970,949	3,630	1,486		1.0052971	1.0418743
SUBTR1	637.3	1.11	2.35	3.45	1.005446	1.061888	2,577,918	9,691	4,892	,		1.0504633
SUBTR2	156.4	0.30	0.54	0.84	1.005387	1.072319	632,521	2,587	1,132	,	1.0059134	1.0596314
SUBTR3	5.7	0.01	0.04	0.05	1.009001	1.052042	23,033	2,007	88	,	1.0072010	1.0451515
WEIGHTED AVERAGE	1,060.1	1.86	3.73	5.58	1.005294	1.059565	4,288,389	16,260	7,773		1.0056358	1.0496762
PRIMARY INTRCHNGE	0.0	1.00	0.10	0.00	0.000000	1.000000	1,200,000	10,200	1,110	21,000	0.0000000	1.0 1001 02
PRIMARY LINES	1,054.3	0.00	13.18	13.18	1.012658	1.072977	4,264,267	0	25,194	25 194	1.0059434	1.0559148
LINE TRANSF	966.4	10.15	4.23	14.38	1.012000	1.089180	3,722,774	88,902	6,931	95,833		1.0838147
SECONDARY	952.0	0.00	4.23	4.74	1.004999	1.094625	3,626,941	00,902	9,354	9,354	1.0025858	1.0866172
SERVICES	932.0	0.36	5.62	5.99	1.006358	1.101585	3,617,587	3,184	11,969	15,153	1.0023858	1.0911879
	341.3	0.30	5.02	5.55	1.000330	1.101303	5,017,507	5,104	11,909	10,100	1.0042003	1.03110/9
	:	=======================================						=======================================				
TOTAL SYSTEM		18.59	97.55	116.13				162,441	299,463	461,904		

#### DEVELOPMENT of LOSS FACTORS

UNADJUSTED DEMAND

LOSS FACTOR LEVEL	CUSTOMER SALES MW	CALC LOSS TO LEVEL	SALES MW @ GEN	CUM PEAK EX FACTORS	PANSION
	а	b	С	d	1/d
BULK LINES	0.0	0.0	0.0	0.00000	0.00000
TRANS SUBS	0.0	0.0	0.0	0.00000	0.00000
TRANS LINES	73.0	3.0	76.0	1.04142	0.96023
TOTAL TRANS	0.0	0.0	0.0	0.00000	0.00000
SUBTRANS	316.3	19.0	335.3	1.06020	0.94322
PRIM SUBS	0.0	0.0	0.0	0.00000	0.00000
PRIM LINES	74.7	5.5	80.2	1.07298	0.93199
SECONDARY	<u>941.3</u>	<u>95.6</u>	<u>1,036.9</u>	1.10158	0.90778
TOTALS	1,405.3	123.1	1,528.4		

#### DEVELOPMENT of LOSS FACTORS UNADJUSTED ENERGY

LOSS FACTOR LEVEL		CALC LOSS	SALES MWH @ GEN	CUM ANNUAL FACTORS	EXPANSION
	а	b	С	d	1/d
BULK LINES	0	0	0	0.00000	0.00000
TRANS SUBS	0	0	0	0.00000	0.00000
TRANS LINES	526,918	19,172	546,090	1.03638	0.96489
TOTAL TRANS	0	0	0	0.00000	0.00000
SUBTRANS	2,466,746	121,705	2,588,451	1.04934	0.95298
PRIM SUBS	0	0	0	0.00000	0.00000
PRIM LINES	516,299	28,869	545,168	1.05591	0.94705
SECONDARY	<u>3,602,434</u>	<u>328,498</u>	<u>3,930,932</u>	1.09119	0.91643
TOTALS	7,112,397	498,243	7,610,640		

#### ESTIMATED VALUES AT GENERATION

		-
LOSS FACTOR AT		
VOLTAGE LEVEL	MW	MWH
BULK LINES	0.00	0
TRANS SUBS	0.00	0
TRANS LINES	76.02	546,090
SUBTRANS SUBS	0.00	0
SUBTRANS LINES	335.34	2,588,451
PRIM SUBS	0.00	0
PRIM LINES	80.15	545,168
SECONDARY	1,036.92	3,930,932
SUBTOTAL	1,528.44	7,610,640
ACTUAL ENERGY	1,530.76	7,591,389
MISSMATCH	(2.32)	19,251
% MISSMATCH	-0.15%	0.25%

KPCO 2011 LOSS B

#### KENTUCKY POWER 2011 LOSS ANALYSIS

#### DEVELOPMENT of LOSS FACTORS

ADJUSTED DEMAND

LOSS FACTOR LEVEL	CUSTOMER SALES MW	SALES ADJUST	CALC LOSS TO LEVEL	SALES MW @ GEN	CUM PEAK EXP FACTORS	ANSION
	a	b	C	d	e	f=1/e
BULK LINES	0.0	0.0	0.0	0.0	0.00000	0.00000
TRANS SUBS	0.0	0.0	0.0	0.0	0.00000	0.00000
TRANS LINES	73.0	0.0	3.1	76.1	1.04223	0.95948
TOTAL TRANS	0.0	0.0	0.0	0.0	0.00000	0.00000
SUBTRANS	316.3	0.0	19.4	335.7	1.06139	0.94216
PRIM SUBS	0.0	0.0	0.0	0.0	0.00000	0.00000
PRIM LINES	74.7	0.0	5.5	80.2	1.07358	0.93146
SECONDARY	941.3	0.0	97.5	1,038.8	1.10354	0.90617
			125.5			
TOTALS	1,405.3	0.0	125.5	1,530.8		

#### DEVELOPMENT of LOSS FACTORS ADJUSTED ENERGY

LOSS FACTOR LEVEL	CUSTOMER SALES MWH	SALES ADJUST		CALC LOSS TO LEVEL	SALES MWH @ GEN	CUM ANNUAL E FACTORS	XPANSION
	a	b		C	d	e	f=1/e
			•	•	2	0.00000	
BULK LINES	0		0	0	0	0.00000	0.00000
TRANS SUBS	0		0	0	0	0.00000	0.00000
TRANS LINES	526,918		0	18,345	545,263	1.03482	0.96636
TOTAL TRANS	0		0	0	0	0.00000	0.00000
SUBTRANS	2,466,746		0	116,440	2,583,186	1.04720	0.95492
PRIM SUBS	0		0	0	0	0.00000	0.00000
PRIM LINES	516,299		0	28,579	544,878	1.05535	0.94755
SECONDARY	3,602,434		<u>0</u>	315,620	<u>3,918,054</u>	1.08761	0.91944
				478,983			
TOTALS	7,112,397		0	478,992	7,591,380		

#### ESTIMATED VALUES AT GENERATION

LOSS FACTOR AT		
VOLTAGE LEVEL	MW	MWH
BULK LINES	0.00	0
TRANS SUBS	0.00	0
TRANS LINES	76.08	545,263
SUBTRANS SUBS	0.00	0
SUBTRANS LINES	335.72	2,583,186
PRIM SUBS	0.00	0
PRIM LINES	80.20	544,878
SECONDARY	1,038.77	3,918,054
	1,530.76	7,591,380
ACTUAL ENERGY	1,530.76	7,591,389
MISSMATCH	0.00	(9)
% MISSMATCH	0.00%	0.00%

EXHIBIT 8

Note adjusting 632 390 3,994

1,050 1,002 2,990 9,194 19,251 19,251

	MW	Unadjusted	MWH	Unadjusted
Service Drop Losses	5.99	6.94	15,153	18,400
Secondary Losses Line Transformer Losses	4.74 14.38	5.49 16.67	9,354 95,833	11,359 116,370
Primary Line Losses	14.30	15.28	25,194	30,594
Distribution Substation Losses	5.58	6.47	24,033	29,183
Subtransmission Losses	20.37	20.37	71,743	71,743
Transmission System Losses	<u>51.90</u>	51.90	<u>220,594</u>	220,594
Total	116.13	123.14	461,904	498,243
Mismatch Allocation	on by Segme	nt		
	MW		MWH	1
Service Drop Losses	-0.13		632	
Secondary Losses Line Transformer Losses	-0.10 -0.31		390 3,994	
Primary Line Losses	-0.29		1,050	
Distribution Substation Losses	-0.12		1,002	
Subtransmission Losses	-0.38		2,990	
Transmission System Losses	-0.98		9,194	
Total	-2.32		19,251	
Adjusted Losses	by Segment			
	MW	% of Total	MWH	% of Total
Service Drop Losses	7.07	5.6%	17,769	3.7%
Secondary Losses Line Transformer Losses	5.60 16.99	4.5% 13.5%	10,969 112,376	2.3% 23.5%
Primary Line Losses	15.57	12.4%	29,544	6.2%
Distribution Substation Losses	6.60	5.3%	28,182	5.9%
Subtransmission Losses	20.75	16.5%	68,753	14.4%
Transmission System Losses	52.88	42.2%	211,400	44.1%
Total	125.46	100.0%	478,992	100.0%
Loss Factors by Segment	MW		мwн	
Retail Sales from Service Drops	941.30		3,602,434	
Adjusted Service Drop Losses	<u>7.07</u>		<u>17,769</u>	
Input to Service Drops	948.37 <b>1.00751</b>		3,620,203	
Service Drop Loss Factor	1.00/51		1.00493	
Output from Secondary	948.37		3,620,203	
Adjusted Secondary Losses	<u>5.60</u>		<u>10,969</u>	
Input to Secondary	953.97		3,631,172	
Secondary Conductor Loss Factor	1.00590		1.00303	
Output from Line Transformers	953.97		3,631,172	
Adjusted Line Transformer Losses	<u>16.99</u>		<u>112,376</u>	
Input to Line Transformers	970.95		3,743,548	
Line Transformer Loss Factor Secondary Composite	<b>1.01781</b> 1.03150		1.03095 1.03917	
Retail Sales from Primary	74.70		516,299	
Req. Whis Sales from Primary	0.00		010,200	
Input to Line Transformers	<u>970.95</u>		<u>3,743,548</u>	
Output from Primary Lines	1045.65		4,259,847	
Adjusted Primary Line Losses	<u>15.57</u>		<u>29,544</u>	
Input to Primary Lines Primary Line Loss Factor	1061.23 <b>1.01489</b>		4,289,391 <b>1.00694</b>	
Out TO PR from Distribution Substations	1061.23		4,289,391	
Req. Whis Sales from Substations	0.00		0	
Retail Sales from Substations TotalOutput from Distribution Substations	0.00 1061.23		0 4,289,391	
Adjusted Distribution Substation Losses	6.60		<u>28,182</u>	
Input to Distribution Substations	1067.82		4,317,572	
Distribution Substation Loss Factor	1.00622		1.00657	
Retail Sales at from SubTransmission	310.10		2,438,725	
Req. Whis Sales from SubTransmission	6.20		28,021	
Input to Distribution Substations	<u>799.30</u>		<u>3,233,472</u>	
Output from SubTransmission	1129.25		5,742,955	
Adjusted SubTransmission System Losses	<u>20.75</u>		<u>68,753</u> 5 811 708	
SubTransmission Loss Factor	1150.00 <b>1.01838</b>		5,811,708 <b>1.01197</b>	
OUT DISTR SUBS	260.77		1,054,917	
Retail Sales at from Transmission	58.50		459,332	
Req. Whis Sales from Transmission	14.50		67,586	
Input Subtransmission	918.35		4,490,212	
Output from Transmission Adjusted Transmission System Losses	1252.12 52.88		6,072,046 211,400	

52.88 1305.00

1.04223

Adjusted Losses and Loss Factors by Facility

Unadjusted Losses by Segment

**Transmission Loss Factor** 

Adjusted Transmission System Losses Input to Transmission

211,400 6,283,446

1.03482

EXHIBIT 9

SUMMARY OF LOSSES AND LOSS FACTORS BY DELIVERY VOLTAGE

			••••						PAGE 1 of 2
	SERVICE LEVEL	SALES MW	LOSSES	SECONDARY	PRIMARY	SUBSTATION	SUBTRANS	TRANSMISSION	
1	SERVICES								
2	SALES	941.30		941.3					
3	LOSSES		7.1	7.1					
4		4 00754		948.4					
5	EXPANSION FACTOR	1.00751							
6	SECONDARY								
7	SALES								
8	LOSSES		5.6	5.6					
9	INPUT			954.0					
10	EXPANSION FACTOR	1.00590							
11	LINE TRANSFORMER								
12	SALES								
13	LOSSES		17.0	17.0					
14	INPUT			971.0					
15	EXPANSION FACTOR	1.01781							
40	PRIMARY								
16 17	SECONDARY			971.0					
18	SALES	74.70		571.0	74.7				
19	LOSSES		15.6	14.5	1.1				
20	INPUT								
21	EXPANSION FACTOR	1.01489							
22	SUBSTATION								
23	PRIMARY			985.4	75.8				
24	SALES	0.0		00011	10.0				
25	LOSSES		6.6	6.1	0.5				
26	INPUT			991.5	76.3				
27	EXPANSION FACTOR	1.00622							
28	SUB-TRANSMISSION								
29	DISTRIBUTION SUBS			724.3	75.0				
30	SALES	316.30					316.3		
31	LOSSES		20.8	13.3	1.4		5.8		
32	INPUT			737.6	76.4		322.1		
33	EXPANSION FACTOR	1.01838							
34	TRANSMISSION								
35	SUBTRANSMISSION			523.7	54.2		322.1		
36	DISTRIBUTION SUBS			259.5	1.3				
37	SALES	73.00						73.	
38	LOSSES		52.9	33.1	2.3		13.6	3.	
39		4 0 4 0 0 0		817.6	57.9		335.7	76.	1
40	EXPANSION FACTOR	1.04223							
41	TOTALS LOSSES	CALCULATED	125.5	96.6	5.3		19.4	3.	1
		SCALED	125.5	97.5	5.5		19.4	3.	
42	% OF TOTAL		100%	77.69%	4.38%		15.48%	2.46%	6
43	SALES	1,405.3		941.3	74.7		316.3	73.	n
43 44	% OF TOTAL	1,405.3		66.98%	5.32%		22.51%	73. 5.19%	
				50.0070	0.0270		12.0170		
45	INPUT	1,530.8		1,038.8	80.2		335.7	76.	1
46	CUMMULATIVE EXPANSIO (from meter to syst			1.10354	1.07358	NA	1.06139	1.0422	3

(from meter to system input)

	ENERGY MWH		SUMMARY	OF LOSSE	S AND LOSS	FACTORS B	Y DELIVERY V	OLTAGE	EXHIBIT 9
	SERVICE LEVEL	SALES	LOSSES S	ECONDARY	PRIMARY	SUBSTATION	SUBTRANS	TRANSMISSION	PAGE 2 of 2
1 2 3 4 5	SERVICES SALES LOSSES INPUT EXPANSION FACTOR	3,602,434 <b>1.00493</b>	17,769	3,602,434 17,769 3,620,203					
6 7 8 9 10	SECONDARY SALES LOSSES INPUT EXPANSION FACTOR	1.00303	10,969	10,969 3,631,172					
11 12 13 14 15	LINE TRANSFORMER SALES LOSSES INPUT EXPANSION FACTOR	1.03095	112,376	112,376 3,743,548					
16 17 18 19 20 21	PRIMARY SECONDARY SALES LOSSES INPUT EXPANSION FACTOR	516,299.000	29,544	3,743,548 25,963	516,299				
22 23 24 25 26 27	SUBSTATION PRIMARY SALES LOSSES INPUT EXPANSION FACTOR	0 <b>1.00657</b>	28,182	3,769,511 24,766 3,794,277					
28 29 30 31 32 33	SUB-TRANSMISSION DISTRIBUTION SUBS SALES LOSSES INPUT EXPANSION FACTOR	2,466,746	68,753	3,173,472 37,992 3,211,464	718		2,466,746 29,531 2,496,277		
34 35 36 37 38 39 40	TRANSMISSION SUBTRANSMISSION DISTRIBUTION SUBS SALES LOSSES INPUT EXPANSION FACTOR	526,918 <b>1.03482</b>	211,400	1,926,879 591,621 87,682 2,606,182	463,295 16,130		2,496,277 86,908 2,583,186	526,918 3 18,345	5
41	TOTALS LOSSES	Calculated Scaled	478,992 478,983	317,517 315,620			116,440 116,440		
42	% OF TOTAL		100%	66.29%	4.98%			3.83%	6
43 44	SALES % OF TOTAL	7,112,397 100.00%		3,602,434 50.65%			2,466,746 34.68%		
45	INPUT	7,591,380		3,918,054	544,878		2,583,186	545,26	3
46	CUMMULATIVE EXPANSION (from meter to syste			1.08761	1.05535	NA	1.04720	) 1.03482	2

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# Kentucky Power Company 2011 Analysis of System Losses

# Appendix B

# **Discussion of Hoebel Coefficient**



## COMMENTS ON THE HOEBEL COEFFICIENT

The Hoebel coefficient represents an established industry standard relationship between peak losses and average losses and is used in a loss study to estimate energy losses from peak demand losses. H. F. Hoebel described this relationship in his article, "Cost of Electric Distribution Losses," <u>Electric Light and Power</u>, March 15, 1959. A copy of this article is attached.

Within any loss evaluation study, peak demand losses can readily be calculated given equipment resistance and approximate loading. Energy losses, however, are much more difficult to determine given their time-varying nature. This difficulty can be reduced by the use of an equation which relates peak load losses (demand) to average losses (energy). Once the relationship between peak and average losses is known, average losses can be estimated from the known peak load losses.

Within the electric utility industry, the relationship between peak and average losses is known as the loss factor. For definitional purposes, loss factor is the ratio of the average power loss to the peak load power loss, during a specified period of time. This relationship is expressed mathematically as follows:

	where: $F_{LS} = Loss Factor$
(1) $F_{LS}$ . $A_{LS}$ ) $P_{LS}$	$A_{LS} = Average Losses$
	$P_{LS}$ = Peak Losses

The loss factor provides an estimate of the degree to which the load loss is maintained throughout the period in which the loss is being considered. In other words, loss factor is the ratio of the actual kWh losses incurred to the kWh losses which would have occurred if full load had continued throughout the period under study.

Examining the loss factor expression in light of a similar expression for load factor indicates a high degree of similarity. The mathematical expression for load factor is as follows:

	where: $F_{LD}$ =	Load Factor
(2) $F_{LD}$ . $A_{LD}$ ) $P_{LD}$	$A_{LD} =$	Average Load
	$P_{LD}$ =	Peak Load

This load factor result provides an estimate of the degree to which the load loss is maintained throughout the period in which the load is being considered. Because of the similarities in definition, the loss factor is sometimes called the "load factor of losses." While the definitions are similar, a strict equating of the two factors cannot be made. There does exist, however, a relationship between these two factors which is dependent upon the shape of the load duration curve. Since resistive losses vary as the square of the load, it can be shown mathematically that the loss factor can vary between the extreme limits of load factor and load factor squared. The relationship between load factor and loss factor has become an industry standard and is as follows:



(3) $F_{LS}$ . $H^*F_{LD}^2$ + (1-H)* $F_{LD}$
------------------------------------------------

where:  $F_{LS} = Loss Factor$   $F_{LD} = Load Factor$ H = Hoebel Coeff

As noted in the attached article, the suggested value for H (the Hoebel coefficient) is 0.7. The exact value of H will vary as a function of the shape of the utility's load duration curve. In recent years, values of H have been computed directly for a number of utilities based on EEI load data. It appears on this basis, the suggested value of 0.7 should be considered a lower bound and that values approaching unity may be considered a reasonable upper bound. Based on experience, values of H have ranged from approximately 0.85 to 0.95. The standard default value of 0.9 is generally used.

Inserting the Hoebel coefficient estimate gives the following loss factor relationship using Equation (3):

(4)  $F_{LS}$ .  $0.90*F_{LD}^2 + 0.10*F_{LD}$ 

Once the Hoebel constant has been estimated and the load factor and peak losses associated with a piece of equipment have been estimated, one can calculate the average, or energy losses as follows:

(5) 
$$A_{LS} \cdot P_{LS} * [H*F_{LD}^2 + (1-H)*F_{LD}]$$
 where:  $A_{LS} = Average Losses$   
 $P_{LS} = Peak Losses$   
 $H = Hoebel Coefficient$   
 $F_{LD} = Load Factor$ 

Loss studies use this equation to calculate energy losses at each major voltage level in the analysis.

