Self-Effectuating Enforcement Mechanism (SEEM)

BellSouth Proposed Changes to Kentucky SEEM

Issue Date: December 16, 2002



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Administrative Plan

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Administrative Plan

<u>1. Scope</u>

- 1.1 This Administrative Plan ("Plan") includes Service Quality Measurements ("SQM") with corresponding Self Effectuating Enforcement Mechanisms ("SEEM") to be implemented by BellSouth pursuant to the Orders issued by the Georgia Public Service Commission on January 12, 2001 and May 7, 2001, in Docket 7892-U, and adopted by the Kentucky Public Service Commission (the "Commission") in its Order dated October 19, 2001, Case No. 2001-105.
- 1.2 All exhibits referred to in this plan are located on the BellSouth Performance Measurement Reports website at:

https://pmap.bellsouth.com

2. Reporting

- 2.1 In providing services pursuant to the Interconnection Agreements between BellSouth and each CLEC,
 BellSouth will report its performance to each CLEC in accordance with BellSouth's SQMs and applicable
 SEEMs, which are posted on the Performance Measurement Reports website.
- 2.2 BellSouth will make performance reports available to each CLEC on a monthly basis. The reports will contain information collected in each performance category and will be available to each CLEC via the Performance Measurements Reports website. BellSouth will also provide electronic access to the CLEC specific raw data, when possible, underlying the SQMs via the Performance Measurements website.
- 2.3 Preliminary SQM reports will be posted on the Performance Measurements Reports website by 8:00 A.M.

 EST on the 21st day of each month, or the first business day after the 21st, for the previous month's performance. Final validated SQM reports will be posted by 8:00 A.M. EST on the last day of the month, or the first business day thereafter. Final validated SQM reports not posted within 24 hours of this time will be considered late for late penalty purposes.
- <u>2.4</u> <u>Final validated SEEM reports will be posted by 8:00 A.M. EST on the 15th day of the month, or the first business day thereafter, following the final validated SQM report.</u>
- 2.5 BellSouth shall pay penalties to the Commission, in the aggregate, for late and incomplete reports on the following progressive sliding scale: 1 -7 days \$5,000; 8-15 days \$10,000; 16-30 day \$40,000; 31+ days \$5,000 per day.
- 2.6 Such penalty shall be made to the Commission or its designee within fifteen (15) calendar days of the end of the reporting month in which the final publication date of the report or the report revision occurs.
- 2.7 <u>Tier-2 SEEMs payments and Administrative fines and penalties for late and incomplete reports will be sent electronically transferred, to the Commission on or before the 15th of the month.</u>
- 2.8 BellSouth shall retain the performance measurement raw data files for a period of 18 months and further retain the data used in PMAP to produce monthly reports for a period of three years.
- 2.9 BellSouth will provide documentation of late and incomplete occurrences during the reporting month that data is posted to the website. The notations may be viewed on the Performance Measurements website from the PMAP home page on the Current Month Site Updates link.



3. Review of Measurements

- Beginning in December 2002 and annually thereafter BellSouth will review the SQMs and the SEEMS. All modifications to the SQMs will be approved by the Commission. Each CLEC may provide input regarding any suggested additions, deletions or other modifications to the SQMs or the SEEMS. BellSouth will provide notice of all changes to the SQMs via the Performance Measurement Reports website.
- 3.2 BellSouth acknowledges that the Commission reserves the right to modify the SQMs or the SEEMS plan at any time it deems necessary upon Commission order.

4. Enforcement Mechanisms

4.1 Definitions

- 4.1.1 Enforcement Measurement Elements the performance measurements identified as SEEM measurements within the SOM.
- 4.1.2 <u>Enforcement Measurement Benchmark a competitive level of performance negotiated by BellSouth used to evaluate the performance of BellSouth and each CLEC where no analogous retail process, product or service is feasible.</u>
- <u>4.1.3</u> <u>Enforcement Measurement Compliance comparing performance levels provided to BellSouth retail customers with performance levels provided by BellSouth to the CLEC customer.</u>
- 4.1.4 <u>Test Statistic and Balancing Critical Value</u> the means by which enforcement will be determined using statistically valid equations. The Test Statistic and Balancing Critical Value are set forth in Exhibit C located on the Performance Measurements Reports website, incorporated herein by this reference.
- 4.1.5 Cell a grouping of transactions at which like-to-like comparisons are made. For example, all BellSouth retail POTS services, for residential customers, requiring a dispatch in a particular wire center, at a particular point in time will be compared directly to CLEC resold services for residential customers, requiring a dispatch, in the same wire center, at a particular point in time. When determining compliance, these cells can have a positive or negative Test Statistic. See Exhibit C located on the Performance Measurements Reports website, incorporated herein by this reference.
- 4.1.6 <u>Affected Volume</u> that proportion of the total impacted CLEC volume or CLEC Aggregate volume for which remedies will be paid.
- 4.1.7 <u>Delta a measure of the meaningful difference between BellSouth performance and CLEC performance. For individual CLECs the Delta value shall be .50 and for the CLEC aggregate the Delta value shall be .35.</u>
- 4.1.8 Parity Gap refers to the incremental departure from a compliant-level of service. This is also referred to as "diff" in the Statistical paper located at Exhibit C located on the Performance Measurements Reports website, incorporated herein by this reference.
- 4.1.9 <u>Tier-1 Enforcement Mechanisms self-executing liquidated damages paid directly to each impacted CLEC when BellSouth delivers non-compliant performance of any one of the Tier-1 Enforcement Measurement Elements for any month as calculated by BellSouth.</u>
- 4.1.10 Tier-2 Enforcement Mechanisms assessments paid directly to the Kentucky Public Service

 Commission or its designee. Tier 2 Enforcement Mechanisms are triggered by three consecutive
 monthly failures in which BellSouth performance is out of compliance or does not meet the
 benchmarks for the aggregate of all CLEC data as calculated by BellSouth for a particular Tier-2
 Enforcement Measurement Element.



4.1.11 Tier-3 Enforcement Mechanisms – the voluntary suspension of additional marketing and sales of long distance services triggered by excessive repeat failures of those specific submeasures as defined in Exhibit B located on the Performance Measurements Reports website, incorporated herein by this reference until BellSouth performance improves.

4.2 Application

- 4.2.1 The application of the Tier-1, Tier-2 and Tier-3 Enforcement Mechanisms does not foreclose other legal and regulatory claims and remedies available to each CLEC.
- 4.2.2 Payment of any Tier-1 or Tier-2 Enforcement Mechanisms shall not be considered as an admission against interest or an admission of liability or culpability in any legal, regulatory or other proceeding relating to BellSouth's performance. The payment of any Tier-1 Enforcement Mechanisms to each CLEC shall be credited against any liability associated with or related to BellSouth's service performance.
- 4.2.3 It is not the intent of the Parties that BellSouth be liable for both Tier-2 Enforcement Mechanisms and any other assessments or sanctions imposed by the Commission. CLECs will not oppose any effort by BellSouth to set off Tier-2 Enforcement Mechanisms from any additional assessment imposed by the Commission.
- 4.2.4 The Enforcement Mechanisms contained in this Plan have been provided by BellSouth in order to maintain compliance between BellSouth and each CLEC. Therefore, CLECs may not use the existence of this section or any payments of any Tier-1 or Tier-2 Enforcement Mechanisms under this section as evidence that BellSouth has not complied with or has violated any state or federal law or regulation.

4.3 Methodology

- 4.3.1 Tier-1 Enforcement Mechanisms will be triggered by BellSouth's failure to achieve applicable
 Enforcement Measurement Compliance or Enforcement Measurement Benchmarks for each CLEC
 for the State of Kentucky for a given Enforcement Measurement Element in a given month.
 Enforcement Measurement Compliance is based upon a Test Statistic and Balancing Critical Value
 calculated by BellSouth utilizing BellSouth generated data. The method of calculation is set forth in
 Exhibit D located on the Performance Measurements Reports website, incorporated herein by this
 reference.
 - 4.3.1.1 <u>Tier-1 Enforcement Mechanisms apply on a per transaction basis for each negative cell</u> and will escalate based upon the number of consecutive months that BellSouth has reported non-compliance.
 - 4.3.1.2 <u>Fee Schedule for Tier-1 Enforcement Mechanisms is shown on the Performance</u>

 <u>Measurement Reports website in Table-1 of Exhibit A, incorporated herein by this reference. Failures beyond Month 6 will be subject to Month 6 fees.</u>
- 4.3.2 Tier-2 Enforcement Mechanisms will be triggered by BellSouth's failure to achieve applicable

 Enforcement Measurement Compliance or Enforcement Measurement Benchmarks for the State
 for given Enforcement Measurement Elements for three consecutive months based upon a
 statistically valid equation calculated by BellSouth utilizing BellSouth generated data. The method
 of calculation is set forth in Exhibit D located on the Performance Measurements Reports website,
 incorporated herein by this reference.
 - 4.3.2.1 <u>Tier- 2 Enforcement Mechanisms apply, for an aggregate of all CLEC data generated by BellSouth, on a per transaction basis for each negative cell for a particular Enforcement Measurement Element.</u>
 - 4.3.2.2 Fee Schedule for Total Quarterly Tier-2 Enforcement Mechanisms is shown on the Performance Measurement Reports website in Table-2 of Exhibit A, incorporated herein by this reference.



4.3.3 Tier-3 Enforcement Mechanisms will be triggered by BellSouth's failure to achieve Enforcement
Measurement Compliance or Enforcement Measurement Benchmarks for the State for given
Enforcement Measurement Elements for three consecutive months. The method of calculation for
specified submeasures is identical to the method of calculation for Tier-2 Enforcement Mechanisms
as described above. The specific submeasures which are the mechanism for triggering and
removing a Tier-3 Enforcement Mechanisms are described in Exhibit B on the Performance
Measurement Reports website, incorporated herein by this reference.

4.4 Payment of Tier-1 and Tier-2 Amounts

- 4.4.1 If BellSouth performance triggers an obligation to pay Tier-1 Enforcement Mechanisms to a CLEC or an obligation to remit Tier-2 Enforcement Mechanisms to the Commission or its designee,

 BellSouth shall make payment in the required amount on the day upon which the final validated SEEM reports are posted on the Performance Measurements Reports website as set forth in Section 2.4 above.
- 4.4.2 For each day after the due date that BellSouth fails to pay a CLEC the required amount, BellSouth will pay the CLEC 6% simple interest per annum.
- 4.4.3 If a CLEC disputes the amount paid to for Tier-1 Enforcement Mechanisms, the CLEC shall submit a written claim to BellSouth within sixty (60) days after the date of the performance measurement report for which the obligation arose. BellSouth shall investigate all claims and provide the CLEC written findings within thirty (30) days after receipt of the claim. If BellSouth determines the CLEC is owed additional amounts, BellSouth shall pay the CLEC such additional amounts within thirty (30) days after its findings along with 6% simple interest per annum.
- 4.4.4 BellSouth may set off any SEEMS payment to a CLEC against undisputed amounts owed by a CLEC to BellSouth pursuant to the Interconnection Agreement between the parties which have not been paid to BellSouth within ninety (90) days past the Bill Due Date as set forth in the Billing Attachment of the Interconnection Agreement.
- 4.4.5 At the end of each calendar year, BellSouth will have its independent auditing and accounting firm certify that the results of all Tier-1 and Tier-2 Enforcement Mechanisms were paid and accounted for in accordance with Generally Accepted Account Principles (GAAP).

4.5 Limitations of Liability

- 4.5.1 BellSouth will not be responsible for CLEC acts or omissions that cause performance measures to be missed or fail, including but not limited to accumulation and submission of orders at unreasonable quantities or times or failure to submit accurate orders or inquiries. BellSouth shall provide each CLEC with reasonable notice of such acts or omissions and provide each CLEC any such supporting documentation.
- 4.5.2 BellSouth shall not be obligated for Tier-1 or Tier 2 Enforcement Mechanisms for non-compliance with a performance measure if such non-compliance was the result of an act or omission by a CLEC that is in bad faith.
- 4.5.3 BellSouth shall not be obligated to pay Tier-1 Enforcement Mechanisms or Tier-2 Enforcement
 Mechanism for non-compliance with a performance measurement if such non-compliance was the
 result of any of the following: a Force Majeure event as set forth in the General Terms and
 Conditions of the Interconnection Agreement between BellSouth and each CLEC; an act or
 omission by a CLEC that is contrary to any of its obligations under its Interconnection Agreement
 with BellSouth; an act or omission by a CLEC that is contrary to any of its obligations under the
 Act, Commission rule, or state law; an act or omission associated with third-party systems or
 equipment.



4.6 Enforcement Mechanism Cap

- 4.6.1 BellSouth's total liability for the payment of Tier-1 and Tier-2 Enforcement Mechanisms shall be collectively capped at 44% of net revenue per year for the state of Kentucky.
- 4.6.2 <u>If projected payments exceed the state cap, a proportional payment will be made to the respective parties.</u>
- 4.6.3 If BellSouth's payment of Tier-1 and Tier-2 Enforcement Mechanisms would have exceeded the cap referenced in this plan, a CLEC may commence a proceeding with the Commission to demonstrate why BellSouth should pay any amount in excess of the cap. Each CLEC shall have the burden of proof to demonstrate why, under the circumstances, BellSouth should have additional liability.

4.7 Audits

4.7.1 All auditing provisions of the Interconnection Agreement between BellSouth and each CLEC shall remain in full force and effect.

4.8 <u>Dispute Resolution</u>

4.8.1 Notwithstanding any other provision of the Interconnection Agreement between BellSouth and each CLEC, any dispute regarding BellSouth's performance or obligations pursuant to this Plan shall be resolved by the Commission.



Appendix A: Fee Schedule



1. Table-1: Liquidated Damages For Tier-1 Measures (Per Affected Item)

Performance Measurement	Month 1	Month 2	Month3	Month4	Month 5	Month 6
Pre-Ordering	\$20	\$30	\$40	\$50	\$60	\$70
Ordering	\$40	\$50	\$60	\$70	\$80	\$90
Provisioning	\$100	\$125	\$175	\$250	\$325	\$500
Provisioning UNE (Coordinated Customer Conversions)	\$400	\$450	\$500	\$550	\$650	\$800
Maintenance and Repair	\$100	\$125	\$175	\$250	\$325	\$500
Maintenance and Repair UNE	\$400	\$450	\$500	\$550	\$650	\$800
LNP	\$150	\$250	\$500	\$600	\$700	\$800
Billing	\$1.00	\$1.00	\$1.00	\$1.00	\$1.00	\$1.00
IC Trunks	\$100	\$125	\$175	\$250	\$325	\$500
Collocation	\$5,000	\$5,000	\$5,000	\$5,000	\$5,000	\$5,000

2. Table-2: Remedy Payments For Tier-2 Measures

Performance Measurement	Per Affected Item
OSS/Pre-Ordering	\$20
Ordering	\$60
Provisioning	\$300
Provisioning-UNE (Coordinated Customer Conversions)	\$875
Maintenance and Repair	\$300
Maintenance and Repair-UNE	\$875
Billing	\$1.00
LNP	\$500
IC Trunks	\$500
Collocation	\$15,000
Change Management	\$1,000
Service Order Accuracy	\$50



Appendix B: SEEM Submetrics



1. Tier 1 Submetrics

Table B-1 contains a list of Tier 1 submetrics.

Table B-1: Tier 1 Submetrics

Item	<u>SQM</u>	Submetric
No.	Ref	
1	<u>PO-1</u>	Loop Makeup - Response Time - Manual - Loops
2	<u>PO-2</u>	Loop Makeup - Response Time - Electronic - Loops
3	<u>O-1</u>	Acknowledgement Message Timeliness EDI
	<u>O-1</u>	Acknowledgement Message Timeliness TAG
4	<u>O-2</u>	Acknowledgement Message Completeness EDI
	<u>O-2</u>	Acknowledgement Message Completeness TAG
5	<u>O-4</u>	Percent Flow-Through Service Requests (Detail) - Residence
	<u>O-4</u>	Percent Flow-Through Service Requests (Detail) - Business
	<u>O-4</u>	Percent Flow-Through Service Requests (Detail) - UNE-P
	<u>O-4</u>	Percent Flow-Through Service Requests (Detail) - UNE-Other
	<u>O-4</u>	Percent Flow-Through Service Requests (Detail) - LNP
6	<u>O-8</u>	Reject Interval - Fully Mechanized
	<u>O-8</u>	Reject Interval - Partially Mechanized
	<u>O-8</u>	Reject Interval - Non-Mechanized
7	<u>O-9</u>	Firm Order Confirmation Timeliness <u>- Fully Mechanized</u>
	<u>O-9</u>	Firm Order Confirmation Timeliness - Partially Mechanized
	<u>O-9</u>	Firm Order Confirmation Timeliness - Non-Mechanized
	<u>O-9</u>	Firm Order Confirmation Timeliness - IC Trunks
8	<u>O-11</u>	Firm Order Confirmation and Reject Response Completeness - Fully Mechanized
9	<u>P-3</u>	Percent Missed Installation Appointments - Resale POTS
10	<u>P-3</u>	Percent Missed Installation Appointments - Resale Design
11	<u>P-3</u>	Percent Missed Installation Appointments - UNE Loop and Port Combinations
12	<u>P-3</u>	Percent Missed Installation Appointments - UNE Loops
13	<u>P-3</u>	Percent Missed Installation Appointments - UNE xDSL
14	<u>P-3</u>	Percent Missed Installation Appointments - UNE Line Sharing
15	<u>P-3</u>	Percent Missed Installation Appointments - Local IC <u>Interconnection</u> Trunks
	<u>P-3</u>	Percent Missed Installation Appointments - LNP
16	<u>P-4</u>	Average Completion Interval (OCI) & Order Completion Interval Distribution - Resale POTS
17	<u>P-4</u>	Average Completion Interval (OCI) & Order Completion Interval Distribution - Resale Design
18	<u>P-4</u>	Average Completion Interval (OCI) & Order Completion Interval Distribution - UNE Loop and Port Combinations
19	<u>P-4</u>	Average Completion Interval (OCI) & Order Completion Interval Distribution - UNE Loops_ Loop Design



Table B-1: Tier 1 Submetrics (Continued)

		Table B-1: Her 1 Submetrics (Continued)
Item No.	SQM Ref	Submetric
20	<u>P-4</u>	Average Completion Interval (OCI) & Order Completion Interval Distribution - UNE xDSL without conditioning
	<u>P-4</u>	Average Completion Interval (OCI) & Order Completion Interval Distribution - UNE xDSL with conditioning
	<u>P-4</u>	Average Completion Interval (OCI) & Order Completion Interval Distribution - UNE Enhanced Extended Links/Non-Switched Combinations
21	<u>P-4</u>	Average Completion Interval (OCI) & Order Completion Interval Distribution - UNE Line Sharing
22	<u>P-4</u>	Average Completion Interval (OCI) & Order Completion Interval Distribution - Local HCInterconnection Trunks
23	<u>P-7</u>	Coordinated Customer Conversions Interval - Unbundled Loops
24	<u>P-7A</u>	Coordinated Customer Conversions - Hot Cut Timeliness Percent within interval% Within Interval and Average Interval - UNE Loops
25	<u>P-7C</u>	Coordinated Customer Conversions Hot Cut Conversions - Percent Provisioning Troubles Received within 7 days of a completed service order - UNE Loops
26	<u>P-8</u>	Cooperative Acceptance Testing - Percent% of xDSL Loops TestedSuccessfully Passing Cooperative Testing - UNE xDSL
27	<u>P-9</u>	Percent Provisioning Troubles within 30 days of Service Order Completion - Resale POTS
28	<u>P-9</u>	Percent Provisioning Troubles within 30 days of Service Order Completion - Resale Design
29	<u>P-9</u>	Percent Provisioning Troubles within 30 days of Service Order Completion - UNE Loop and Port Combinations
30	<u>P-9</u>	Percent Provisioning Troubles within 30 days of Service Order Completion - UNE Loops
31	<u>P-9</u>	Percent Provisioning Troubles within 30 days of Service Order Completion - UNE xDSL
32	<u>P-9</u>	Percent Provisioning Troubles within 30 days of Service Order Completion - UNE Line Sharing
33	<u>P-9</u>	Percent Provisioning Troubles within 30 days of Service Order Completion - Local IC <u>Interconnection</u> Trunks
34		LNP - Percent Missed Installation Appointments - LNP
	<u>P-13A</u>	LNP - Percent Out of Service < 60 Minutes
	<u>P-13B</u>	LNP - Percentage of Time BellSouth Applies the 10-digit Trigger Prior to the LNP Order Due Date
	<u>P-13C</u>	LNP - Average Disconnect Timeliness Interval & Disconnect Timeliness Interval Distribution (Non Trigger)
35	<u>M&R-1</u>	Missed Repair Appointments - Resale POTS
36	<u>M&R-1</u>	Missed Repair Appointments - Resale Design
37	<u>M&R-1</u>	Missed Repair Appointments - UNE Loop and Port Combinations
38	<u>M&R-1</u>	Missed Repair Appointments - UNE Loops
39	<u>M&R-1</u>	Missed Repair Appointments - UNE xDSL
40	<u>M&R-1</u>	Missed Repair Appointments - UNE Line Sharing
41	<u>M&R-1</u>	Missed Repair Appointments - Local ICInterconnection Trunks



Table B-1: Tier 1 Submetrics (Continued)

Item No.	SQM Ref	Submetric
42	<u>M&R-2</u>	Customer Trouble Report Rate - Resale POTS
43	<u>M&R-2</u>	Customer Trouble Report Rate - Resale Design
44	<u>M&R-2</u>	Customer Trouble Report Rate - UNE Loop and Port Combinations
45	M&R-2	Customer Trouble Report Rate - UNE Loops
46	M&R-2	Customer Trouble Report Rate - UNE xDSL
47	M&R-2	Customer Trouble Report Rate - UNE Line Sharing
48	<u>M&R-2</u>	Customer Trouble Report Rate - Local ICInterconnection Trunks
49	<u>M&R-3</u>	Maintenance Average Duration - Resale POTS
50	M&R-3	Maintenance Average Duration - Resale Design
51	M&R-3	Maintenance Average Duration - UNE Loop and Port Combinations
52	M&R-3	Maintenance Average Duration - UNE Loops
53	M&R-3	Maintenance Average Duration - UNE xDSL
54	<u>M&R-3</u>	Maintenance Average Duration - UNE Line Sharing
55	M&R-3	Maintenance Average Duration - Local IC <u>Interconnection</u> Trunks
56	M&R-4	Percent Repeat Troubles within 30 days - Resale POTS
57	<u>M&R-4</u>	Percent Repeat Troubles within 30 days - Resale Design
58	<u>M&R-4</u>	Percent Repeat Troubles within 30 days - UNE Loop and Port Combinations
59	M&R-4	Percent Repeat Troubles within 30 days - UNE Loops
60	<u>M&R-4</u>	Percent Repeat Troubles within 30 days - UNE xDSL
61	<u>M&R-4</u>	Percent Repeat Troubles within 30 days - UNE Line Sharing
62	M&R-4	Percent Repeat Troubles within 30 days - Local IC <u>Interconnection</u> Trunks
63	<u>B-1</u>	Invoice Accuracy
64	<u>B-2</u>	Mean Time to Deliver Invoices - CRIS
	<u>B-2</u>	Mean Time to Deliver Invoices - CABS
65	<u>B-3</u>	Usage Data Delivery Accuracy
66	TGP-2	Trunk Group Performance - CLEC Specific - CLEC trunk group
67	<u>C-3</u>	Collocation Percent of Due Dates Missed - All Collocation Arrangements



2. Tier 2 Submetrics

Table B-2 contains a list of Tier 2 submetrics.

Table B-2: Tier 2 Submetrics

		Table B-2: Tier 2 Submetrics
Item No	SQM Ref	Submetric
1	<u>OSS-1</u>	Average Response Time Interval and Percent Within Interval (Pre-Ordering/Ordering) - LENS
	OSS-1	Average Response Interval and Percent Within Interval (Pre-Ordering/Ordering) - TAG
2	OSS-2	OSS Interface Availability (Pre-Ordering/Ordering) - Regional per OSS Interface
3	OSS-3	OSS Interface Availability (Maintenance & Repair) - Regional per OSS Interface
4	<u>PO-1</u>	Loop Makeup - Response Time - Manual <u>- Loops</u>
5	<u>PO-2</u>	Loop Makeup - Response Time - Electronic <u>- Loops</u>
6	<u>O-1</u>	Acknowledgement Message Timeliness - EDI
7	<u>O-1</u>	Acknowledgement Message Timeliness - TAG
8	<u>O-2</u>	Acknowledgement Message Completeness EDI
9	<u>O-2</u>	Acknowledgement Message Completeness TAG
10	<u>O-3</u>	Percent Flow-through Service Requests (Summary)- Residence
	<u>O-3</u>	Percent Flow-Through Service Requests (Summary)- Business
	<u>O-3</u>	Percent Flow-Through Service Requests (Summary)- UNE-P
	<u>O-3</u>	Percent Flow-Through Service Requests (Summary)- UNE-Other
	<u>O-3</u>	Percent Flow-Through Service Requests (Summary)- LNP
11	<u>O-8</u>	Reject Interval-Fully Mechanized
	<u>O-8</u>	Reject Interval- Partially Mechanized
	<u>O-8</u>	Reject Interval- Non-Mechanized
12	<u>O-9</u>	Firm Order Confirmation Timeliness-Fully Mechanized
	<u>O-9</u>	Firm Order Confirmation Timeliness- Partially Mechanized
	<u>O-9</u>	Firm Order Confirmation Timeliness- Non-Mechanized
	<u>O-9</u>	Firm Order Confirmation Timeliness- IC Trunks
13	<u>O-11</u>	Firm Order Confirmation and Reject Response Completeness - Fully Mechanized
14	<u>P-3</u>	Percent Missed Installation Appointments - Resale POTS
15	<u>P-3</u>	Percent Missed Installation Appointments - Resale Design
16	<u>P-3</u>	Percent Missed Installation Appointments - UNE Loop and Port Combinations
17	<u>P-3</u>	Percent Missed Installation Appointments - UNE Loops
18	<u>P-3</u>	Percent Missed Installation Appointments - UNE xDSL
19	<u>P-3</u>	Percent Missed Installation Appointments - UNE Line Sharing
20	<u>P-3</u>	Percent Missed Installation Appointments - Local 1 Interconnection Trunks
	<u>P-3</u>	Percent Missed Installation Appointments - LNP
27	<u>P-4</u>	Average Completion Interval (OCI) & Order Completion Interval Distribution - Local +CInterconnection Trunks



Table B-2: Tier 2 Submetrics (Continued)

		Table B-2: Her 2 Submetrics (Continued)
Item No	SQM Ref	Submetric
22	<u>P-4</u>	Average Completion Interval (OCI) & Order Completion Interval Distribution - Resale Design
21	<u>P-4</u>	Average Completion Interval (OCI) & Order Completion Interval Distribution - Resale POTS
26	<u>P-4</u>	Average Completion Interval (OCI) & Order Completion Interval Distribution - UNE Line Sharing
23	<u>P-4</u>	Average Completion Interval (OCI) & Order Completion Interval Distribution - UNE Loop and Port Combinations
24	<u>P-4</u>	Average Completion Interval (OCI) & Order Completion Interval Distribution - UNE Loop-sLoop Design
25	<u>P-4</u>	Average Completion Interval (OCI) & Order Completion Interval Distribution - UNE xDSL without conditioning
	<u>P-4</u>	Average Completion Interval (OCI) & Order Completion Interval Distribution - UNE xDSL with conditioning
	<u>P-4</u>	Average Completion Interval (OCI) & Order Completion Interval Distribution - UNE Enhanced Extended Links/Non-Switched Combinations
28	<u>P-7</u>	Coordinated Customer Conversions Interval - Unbundled Loops
29	<u>P-7A</u>	Coordinated Customer Conversions - Hot Cut Timeliness Percent within interval and Average Interval - UNE Loops
30	<u>P-7C</u>	Coordinated Customer Conversions Hot Cut Conversions - Percent Provisioning Troubles Received within 7 days of a completed service order - UNE Loops
31	<u>P-8</u>	Cooperative Acceptance Testing - Percent xDSL Loops <u>Successful Passing Cooperative Testing-Tested</u> - <u>UNE xDSL</u>
32	<u>P-9</u>	Percent Provisioning Troubles within 30 days of Service Order Completion - Resale POTS
33	<u>P-9</u>	Percent Provisioning Troubles within 30 days of Service Order Completion - Resale Design
34	<u>P-9</u>	Percent Provisioning Troubles within 30 days of Service Order Completion - UNE Loop and Port Combinations
35	<u>P-9</u>	Percent Provisioning Troubles within 30 days of Service Order Completion - UNE Loops
36	<u>P-9</u>	Percent Provisioning Troubles within 30 days of Service Order Completion - UNE xDSL
37	<u>P-9</u>	Percent Provisioning Troubles within 30 days of Service Order Completion - UNE Line Sharing
38	<u>P-9</u>	Percent Provisioning Troubles within 30 days of Service Order Completion - Local IC <u>Interconnection</u> Trunks
	<u>P-11</u>	Service Order Accuracy - Resale
	<u>P-11</u>	Service Order Accuracy - UNE
	<u>P-11</u>	Service Order Accuracy - UNE-P
78		Service Order Accuracy - Resale Residence
79		Service Order Accuracy Resale Business
80		Service Order Accuracy - Resale Design
81		Service Order Accuracy - UNE Specials/Design
82		Service Order Accuracy UNE/Non design
83		Service Order Accuracy - Local Interconnection Trunks



Table B-2: Tier 2 Submetrics (Continued)

Item	<u>SQM</u>	Submetric
No 39	Ref	LNP Percent Missed Installation Appointments
39	P-13A	LNP - Percent Out of Service < 60 Minutes
	P-13A P-13B	LNP - Percentage of Time BellSouth Applies the 10-digit Trigger Prior to the LNP Order Due
	<u>P-13B</u>	Date
	<u>P-13C</u>	LNP - Average Disconnect Timeliness Interval & Disconnect Timeliness Interval Distribution
		(Non Trigger)
40	<u>M&R-1</u>	Missed Repair Appointments - Resale POTS
41	<u>M&R-1</u>	Missed Repair Appointments - Resale Design
42	<u>M&R-1</u>	Missed Repair Appointments - UNE Loop and Port Combinations
43	<u>M&R-1</u>	Missed Repair Appointments - UNE Loops
44	<u>M&R-1</u>	Missed Repair Appointments - UNE xDSL
45	<u>M&R-1</u>	Missed Repair Appointments - UNE Line Sharing
46	<u>M&R-1</u>	Missed Repair Appointments - Local IC <u>Interconnection</u> Trunks
53	M&R-2	Customer Trouble Report Rate - Local IC <u>Interconnection</u> Trunks
48	<u>M&R-2</u>	Customer Trouble Report Rate - Resale Design
47	<u>M&R-2</u>	Customer Trouble Report Rate - Resale POTS
52	<u>M&R-2</u>	Customer Trouble Report Rate - UNE Line Sharing
49	<u>M&R-2</u>	Customer Trouble Report Rate - UNE Loop and Port Combinations
50	<u>M&R-2</u>	Customer Trouble Report Rate - UNE Loops
51	M&R-2	Customer Trouble Report Rate - UNE xDSL
54	<u>M&R-3</u>	Maintenance Average Duration - Resale POTS
55	<u>M&R-3</u>	Maintenance Average Duration - Resale Design
56	<u>M&R-3</u>	Maintenance Average Duration - UNE Loop and Port Combinations
57	<u>M&R-3</u>	Maintenance Average Duration - UNE Loops
58	<u>M&R-3</u>	Maintenance Average Duration - UNE xDSL
59	<u>M&R-3</u>	Maintenance Average Duration - UNE Line Sharing
60	<u>M&R-3</u>	Maintenance Average Duration - Local ICInterconnection Trunks
61	<u>M&R-4</u>	Percent Repeat Troubles within 30 days - Resale POTS
62	<u>M&R-4</u>	Percent Repeat Troubles within 30 days - Resale Design
63	<u>M&R-4</u>	Percent Repeat Troubles within 30 days - UNE Loop and Port Combinations
64	<u>M&R-4</u>	Percent Repeat Troubles within 30 days - UNE Loops
65	<u>M&R-4</u>	Percent Repeat Troubles within 30 days - UNE xDSL
66	<u>M&R-4</u>	Percent Repeat Troubles within 30 days - UNE Line Sharing
67	<u>M&R-4</u>	Percent Repeat Troubles within 30 days - Local IC <u>Interconnection</u> Trunks
68	<u>B-1</u>	Invoice Accuracy
69	<u>B-2</u>	Mean Time to Deliver Invoices-CRIS
	<u>B-2</u>	Mean Time to Deliver Invoices- CABS



Table B-2: Tier 2 Submetrics (Continued)

Item No	SQM Ref	Submetric
70	<u>B-3</u>	Usage Data Delivery Accuracy
71	TGP-1	Trunk Group Performance - <u>CLEC</u> Aggregate
72	<u>C-3</u>	Collocation Percent of Due Dates Missed - <u>All Collocation Arrangements</u>
73	<u>CM-1</u>	Timeliness of Change Management Notices - Region
74	<u>CM-3</u>	Timeliness of Documents Associated with Change - Region
75	<u>CM-6</u>	Percent of Software Errors Corrected in X (10, 30, 45) Business Days - Region
76	<u>CM-7</u>	Percent of Change Requests Accepted or Rejected Within 10 Days - Region
77	<u>CM-11</u>	Percent of Change Requests Implemented Within 60 Weeks of Prioritization - Region



3. Tier 3 Submetrics

Table B-3 contains a list of Tier 3 submetrics.

Table B-3: Tier 3 Submetrics

Item	SQM	
No	Ref	Submetric
1	<u>P-3</u>	Percent Missed Installation Appointments - Resale POTS
2	<u>P-3</u>	Percent Missed Installation Appointments - Resale Design
3	<u>P-3</u>	Percent Missed Installation Appointments - UNE Loop
4	<u>P-3</u>	Percent Missed Installation Appointments - UNE Loop & Port Combo
5	<u>P-3</u>	Percent Missed Installation Appointments - UNE xDSL (ADSL, HDSL, UCL)
6	<u>P-3</u>	Percent Missed Installation Appointments - UNE Line Sharing
7	<u>P-3</u>	Percent Missed Installation Appointments - <u>Local</u> Interconnection Trunks
8	<u>P-4</u>	Average Completion Interval (OCI) & Order Completion Interval Distribution - Resale POTS
9	<u>P-4</u>	Average Completion Interval (OCI) & Order Completion Interval Distribution - Resale Design
10	<u>P-4</u>	Average Completion Interval (OCI) & Order Completion Interval Distribution - UNE Loop & Port Combo
11	<u>P-4</u>	Average Completion Interval (OCI) & Order Completion Interval Distribution - UNE xDSL (ADSL, HDSL, UCL) - Without Conditioning
	<u>P-4</u>	Average Completion Interval (OCI) & Order Completion Interval Distribution - UNE xDSL With Conditioning
12	<u>P-4</u>	Average Completion Interval (OCI) & Order Completion Interval Distribution - UNE Line Sharing
13	<u>P-4</u>	Average Completion Interval (OCI) & Order Completion Interval Distribution - Interconnection Trunks
14	<u>M&R-1</u>	Missed Repair Appointments - Resale POTS
15	<u>M&R-1</u>	Missed Repair Appointments - Resale Design
16	M&R-1	Missed Repair Appointments - UNE Loop + Port Combo
17	<u>M&R-1</u>	Missed Repair Appointments - UNE Loops
18	M&R-1	Missed Repair Appointments - UNE xDSL
19	M&R-1	Missed Repair Appointments - UNE Line Sharing
20	M&R-1	Missed Repair Appointments - Local Interconnection Trunks
21	<u>B-1</u>	Invoice Accuracy
22	<u>B-2</u>	Mean Time To Deliver Invoices <u>- CRIS</u>
	<u>B-2</u>	Mean Time To Deliver Invoices - CABS
23	TGP-1	Trunk Group Performance - CLEC Aggregate
24	<u>C-3</u>	Collocation Percent of Due Dates Missed <u>- All Collocation Agreements</u>
25	<u>CM-1</u>	Timeliness of Change Management Notices - Region
26	<u>CM-3</u>	Timeliness of Documents Associated with Change - Region



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Appendix C: Statistical Properties and Definitions



Statistical Methods for BellSouth Performance Measure Analysis

1. Necessary Properties for a Test Methodology

The statistical process for testing if competing local exchange carriers (CLECs) customers are being treat equally with BellSouth (BST) customers involves more than just a mathematical formula. Three key elements need to be considered before an appropriate decision process can be developed. These are

- the type of data,
- the type of comparison, and
- the type of performance measure.

Once these elements are determined a test methodology should be developed that complies with the following properties.

- *Like-to-Like Comparisons* When possible, data should be compared at appropriate levels, e.g. wire center, time of month, dispatched, and residential, new orders. The testing process should:
 - Identify variables that may affect the performance measure.
 - Record these important confounding covariates.
 - Adjust for the observed covariates in order to remove potential biases and to make the CLEC and the ILEC units as comparable as possible.
- Aggregate Level Test Statistic Each performance measure of interest should be summarized by one overall test statistic giving the decision maker a rule that determines whether a statistically significant difference exists. The test statistic should have the following properties.
 - The method should provide a single overall index, on a standard scale.
 - If entries in comparison cells are exactly proportional over a covariate, the aggregated index should be very nearly the same as if comparisons on the covariate had not been done.
 - The contribution of each comparison cell should depend on the number of observations in the cell.
 - Cancellation between comparison cells should be limited.
 - The index should be a continuous function of the observations.
- Production Mode Process The decision system must be developed so that it does not require intermediate manual intervention, i.e. the process must be a "black box."
 - Calculations are well defined for possible eventualities.
 - The decision process is an algorithm that needs no manual intervention.
 - Results should be arrived at in a timely manner.
 - The system must recognize that resources are needed for other performance measure-related processes that also must be run in a timely manner.
 - The system should be auditable, and adjustable over time.
- Balancing The testing methodology should balance Type I and Type II Error probabilities.
 - P(Type I Error) = P(Type II Error) for well defined null and alternative hypotheses.
 - The formula for a test's balancing critical value should be simple enough to calculate using standard mathematical functions, i.e. one should avoid methods that require computationally intensive techniques.
 - Little to no information beyond the null hypothesis, the alternative hypothesis, and the number of observations should be required for calculating the balancing critical value.



- Trimming Removing extreme observations from BellSouth and CLEC distributions is needed in order to
 ensure that a fair comparison is made between performance measures. Three conditions are needed to
 accomplish this goal. These are:
 - Trimming should be based on a general rule that can be used in a production setting.
 - Trimmed observations should not simply be discarded; they need to be examined and possibly used in the final decision making process.
 - Trimming should only be used on performance measures that are sensitive to "outliers."

Measurement Types

The performance measures that will undergo testing are of four types:

- means
- proportions,
- rates, and
- ratio

While all four have similar characteristics, proportions and rates are derived from count data while means and ratios are derived from interval measurements.

2. Testing Methodology – The Truncated Z

Many covariates are chosen in order to provide deep comparison levels. In each comparison cell, a Z statistic is calculated. The form of the Z statistic may vary depending on the performance measure, but it should be distributed approximately as a standard normal, with mean zero and variance equal to one. Assuming that the test statistic is derived so that it is negative when the performance for the CLEC is worse than for the ILEC, a positive truncation is done – i.e. if the result is negative it is left alone, if the result is positive it is changed to zero. A weighted average of the truncated statistics is calculated where a cell weight depends on the volume of BST and CLEC orders in the cell. The weighted average is re-centered by the theoretical mean of a truncated distribution, and this is divided by the standard error of the weighted average. The standard error is computed assuming a fixed effects model.

Proportion Measures

For performance measures that are calculated as a proportion, in each adjustment cell, the truncated Z and the moments for the truncated Z can be calculated in a direct manner. In adjustment cells where proportions are not close to zero or one, and where the sample sizes are reasonably large, a normal approximation can be used. In this case, the moments for the truncated Z come directly from properties of the standard normal distribution. If the normal approximation is not appropriate, then the Z statistic is calculated from the hypergeometric distribution. In this case, the moments of the truncated Z are calculated exactly using the hypergeometric probabilities.

Rate Measures

The truncated Z methodology for rate measures has the same general structure for calculating the Z in each cell as proportion measures. For a rate measure, there are a fixed number of circuits or units for the CLEC, n_{2j} and a fixed number of units for BST, n_{1j} . Suppose that the performance measure is a "trouble rate." The modeling assumption is that the occurrence of a trouble is independent between units and the number of troubles in n circuits follows a Poisson distribution with mean λ_n where λ is the probability of a trouble in 1 circuit and n is the number of circuits.

In an adjustment cell, if the number of CLEC troubles is greater than 15 and the number of BST troubles is greater than 15, then the Z test is calculated using the normal approximation to the Poisson. In this case, the moments of the truncated Z come directly from properties of the standard normal distribution. Otherwise, if there are very few troubles, the number of CLEC troubles can be modeled using a binomial distribution with n equal to the total number of troubles (CLEC plus BST troubles.) In this case, the moments for the truncated Z are calculated explicitly using the binomial distribution.

Mean Measures

For mean measures, an adjusted "t" statistic is calculated for each like-to-like cell which has at least 7 BST and 7 CLEC transactions. A permutation test is used when one or both of the BST and CLEC sample sizes is less than 6. Both the adjusted "t" statistic and the permutation calculation are described in Appendix D, Statistical Formulas and Technical Description.

Ratio Measures

Rules will be given for computing a cell test statistic for a ratio measure, however, the current plan for measures in this category, namely billing accuracy, does not call for the use of a Z parity statistic.



Appendix D: Statistical Formulas and Technical Description



We start by assuming that any necessary trimming¹ of the data is complete, and that the data are disaggregated so that comparisons are made within appropriate classes or adjustment cells that define "like" observations.

1. Notation and Exact Testing Distributions

Below, we have detailed the basic notation for the construction of the truncated z statistic. In what follows the word "cell" should be taken to mean a like-to-like comparison cell that has both one (or more) ILEC observation and one (or more) CLEC observation.

L = the total number of occupied cells

j = 1,...,L; an index for the cells

 n_{1i} = the number of ILEC transactions in cell j

 n_{2j} = the number of CLEC transactions in cell j

 n_i = the total number transactions in cell j; n_{1j} + n_{2j}

 X_{1jk} = individual ILEC transactions in cell j; $k = 1,..., n_{1j}$

 X_{2jk} = individual CLEC transactions in cell j; k = 1,..., n_{2j}

 Y_{ik} = individual transaction (both ILEC and CLEC) in cell j

$$= \begin{cases} X_{1jk} & k = 1, ..., n_{1j} \\ X_{2jk} & k = n_{1j} + 1, ..., n_{j} \end{cases}$$

 $\Phi^{-1}(\cdot)$ = the inverse of the cumulative standard normal distribution function

^{1.} When it is determined that a measure should be trimmed, a trimming rule that is easy to implement in a production setting is:

Trim the ILEC observations to the largest CLEC value from all CLEC observations in the month under consideration.

That is, no CLEC values are removed; all ILEC observations greater than the largest CLEC observation are trimmed.

For Mean Performance Measures the following additional notation is needed.

$$\overline{X}_{ij}$$
 = The ILEC sample mean of cell j

$$\overline{X}_{j}$$
 = The CLEC sample mean of cell j

$$S_{1j}^2$$
 = The ILEC sample variance in cell j

$$S_{2i}^2$$
 = The CLEC sample variance in cell j

$$\{y_{jk}\} \hspace{1cm} = \hspace{1cm} \text{a random sample of size } n_{2j} \text{ from the set of } \hspace{1cm} Y_{_{j1}}, \ldots, Y_{_{jn_{_{j}}}} \hspace{1cm} ; \hspace{1cm} k = 1, \ldots, n_{2j}$$

$$M_i$$
 = The total number of distinct pairs of samples of size n_{1i} and n_{2i} ;

$$= \binom{n_j}{n_{1j}}$$

The exact parity test is the permutation test based on the "modified Z" statistic. For large samples, we can avoid permutation calculations since this statistic will be normal (or Student's t) to a good approximation. For small samples, where we cannot avoid permutation calculations, we have found that the difference between "modified Z" and the textbook "pooled Z" is negligible. We therefore propose to use the permutation test based on pooled Z for small samples. This decision speeds up the permutation computations considerably, because for each permutation we need only compute the sum of the CLEC sample values, and not the pooled statistic itself.

A permutation probability mass function distribution for cell j, based on the "pooled Z" can be written as

$$PM(t) = P(\sum_{k} y_{jk} = t) = \frac{\text{the number of samples that sum to t}}{M_{j}}$$

and the corresponding cumulative permutation distribution is

$$CPM(t) = P(\sum_{k} y_{jk} \le t) = \frac{\text{the number of samples with sum } \le t}{M_i}$$

For Proportion Performance Measures the following notation is defined

 a_{1i} = The number of ILEC cases possessing an attribute of interest in cell j

 a_{2j} = The number of CLEC cases possessing an attribute of interest in cell j

 a_i = The number of cases possessing an attribute of interest in cell j; $a_{1i} + a_{2i}$

The exact distribution for a parity test is the hypergeometric distribution. The hypergeometric probability mass function distribution for cell j is

$$HG(h) = P(H = h) = \begin{cases} \frac{\binom{n_{1j}}{h} \binom{n_{2j}}{a_j - h}}{\binom{n_j}{a_j}}, \max(0, a_j - n_{2j}) \le h \le \min(a_j, n_{1j}) \\ \binom{n_j}{a_j} \\ 0 & \text{otherwise} \end{cases}$$

and the cumulative hypergeometric distribution is

$$CHG(x) = P(H \le x) = \begin{cases} 0 & x < max(0, a_{j} - n_{2j}) \\ \sum_{h=max(0, a_{j} - n_{1j})}^{x} HG(h), & max(0, a_{j} - n_{2j}) \le x \le min(a_{j}, n_{1j}) \\ 1 & x > min(a_{j}, n_{1j}) \end{cases}$$

For Rate Measures, the notation needed is defined as

 b_{1i} = The number of ILEC base elements in cell j

 b_{2i} = The number of CLEC base elements in cell j

 b_i = The total number of base elements in cell j; $b_{1j} + b_{2j}$

 $\hat{\mathbf{r}}_{...}$ = The ILEC sample rate of cell j; $\mathbf{n}_{1j}/\mathbf{b}_{1j}$

 $\hat{\mathbf{f}}_{2j}$ = The CLEC sample rate of cell j; n_{2j}/b_{2j}

 q_i = The relative proportion of ILEC elements for cell j; b_{1j}/b_j

The exact distribution for a parity test is the binomial distribution. The binomial probability mass function distribution for cell j is

$$BN(k) = P(B = k) = \begin{cases} \binom{n_j}{k} q_j^k (1 - q_j)^{n_j - k}, & 0 \le k \le n_j \\ 0 & \text{otherwise} \end{cases}$$

and the cumulative binomial distribution is

$$CBN(x) = P(B \le x) = \begin{cases} 0 & x < 0 \\ \sum_{k=0}^{x} BN(k), & 0 \le x \le n_{j} \\ 1 & x > n_{j} \end{cases}$$

For Ratio Performance Measures the following additional notation is needed.

 U_{1jk} = additional quantity of interest of an individual ILEC transaction in cell j; k = 1,..., n_{1j}

 U_{2jk} = additional quantity of interest of an individual CLEC transaction in cell j; k = 1,..., n_{2j}

 $\hat{R}_{ij} = \text{the ILEC (I = 1) or CLEC (i = 2) ratio of the total additional quantity of interest to the base transaction total in cell j, i.e.,} \\ \sum_{k} U_{ijk} / \sum_{k} X_{ijk}$

2. Calculating the Truncated Z

The general methodology for calculating an aggregate level test statistic is outlined below.

Calculate Cell Weights (W_i)

A weight based on the number of transactions is used so that a cell, which has a larger number of transactions, has a larger weight. The actual weight formulae will depend on the type of measure.

Mean or Ratio Measure

$$W_j = \sqrt{\frac{n_{1j}n_{2j}}{n_j}}$$

Proportion Measure

$$W_{j} = \sqrt{\frac{n_{2j}n_{1j}}{n_{j}} \cdot \frac{a_{j}}{n_{j}} \cdot \left(1 - \frac{a_{j}}{n_{j}}\right)}$$

Rate Measure

$$W_{j} = \sqrt{\frac{b_{1j}b_{2j}}{b_{j}} \cdot \frac{n_{j}}{b_{j}}}$$



Calculate a Z Value (Z_i) for each Cell

A Z statistic with mean 0 and variance 1 is needed for each cell.

- If $W_i = 0$, set $Z_i = 0$.
- Otherwise, the actual Z statistic calculation depends on the type of performance measure.

Mean Measure

$$Z_i = \Phi^{-1}(\alpha)$$

where α is determined by the following algorithm.

If $min(n_{1i}, n_{2i}) > 6$, then determine α as

$$\alpha = P(t_{n_i - 1} \le T_i)$$

that is, α is the probability that a t random variable with n_{1i} - 1 degrees of freedom, is less than

$$T_{j} = \begin{cases} t_{j} + \frac{g}{6} \left(\frac{n_{1j} + 2n_{2j}}{\sqrt{n_{1j} n_{2j} (n_{1j} + n_{2j})}} \right) \left(t_{j}^{2} + \frac{n_{2j} - n_{1j}}{n_{1j} + 2n_{2j}} \right) & t_{j} \ge t_{minj} \end{cases}$$

$$t_{j} \ge t_{minj}$$

where

$$t_{j} = \frac{\overline{X}_{1j} - \overline{X}_{2j}}{s_{1j} \sqrt{\frac{1}{n_{1j}} + \frac{1}{n_{2j}}}}$$

$$t_{\min j} = \frac{-3\sqrt{n_{1j}n_{2j}n_{j}}}{g(n_{1j} + 2n_{2j})}$$

and g is the median value of all values of

$$\gamma_{1j} = \frac{n_{1j}}{(n_{1j} - 1)(n_{1j} - 2)} \sum_{k} \left(\frac{X_{1jk} - \overline{X}_{1j}}{s_{1j}} \right)^{3}$$

with $n_{1j} > n_{3q}$ for all values of j. n_{3q} is the 3 quartile of all values of n_{1j}

Note, that t_j is the "modified Z" statistic. The statistic T_j is a "modified Z" corrected for the skewness of the ILEC data.

If $min(n_{1i}, n_{2i}) \le 6$, and

- $M_1 \le 1,000$ (the total number of distinct pairs of samples of size n_{1j} and n_{2j} is 1,000 or less).
 - Calculate the sample sum for all possible samples of size n_{2j}.
 - Rank the sample sums from smallest to largest. Ties are dealt by using average ranks.
 - Let R₀ be the rank of the observed sample sum with respect all the sample sums.

$$\alpha = 1 - \frac{R_0 - 0.5}{M_i}$$

- b) $M_i > 1,000$
 - Draw a random sample of 1,000 sample sums from the permutation distribution.
 - Add the observed sample sum to the list. There are a total of 1001 sample sums. Rank the sample sums from smallest to largest. Ties are dealt by using average ranks.
 - Let R₀ be the rank of the observed sample sum with respect all the sample sums.

$$\alpha = 1 - \frac{R_0 - 0.5}{1001}$$

Proportion Measure

$$Z_{j} = \frac{n_{j} a_{1j} - n_{1j} a_{j}}{\sqrt{\frac{n_{1j} n_{2j} a_{j} (n_{j} - a_{j})}{n_{j} - 1}}}$$



Rate Measure

$$Z_{j} = \frac{n_{1j} - n_{j} q_{j}}{\sqrt{n_{j} q_{j} (1 - q_{j})}}$$

Ratio Measure

$$\begin{split} Z_{j} &= \frac{\hat{R}_{1j} - \hat{R}_{2j}}{\sqrt{V(\hat{R}_{1j}) \left(\frac{1}{n_{1j}} + \frac{1}{n_{2j}}\right)}} \\ V(\hat{R}_{1j}) &= \frac{\sum_{k} \left(U_{1jk} - \hat{R}_{1j} X_{1jk}\right)^{2}}{\overline{X}_{1j}^{2}(n_{1j} - 1)} = \frac{\sum_{k} U_{1jk}^{2} - 2\hat{R}_{1j} \sum_{k} \left(U_{1jk} X_{1jk}\right) + \hat{R}_{1j}^{2} \sum_{k} X_{1jk}^{2}}{\overline{X}_{1j}^{2}(n_{1j} - 1)} \end{split}$$

Obtain a Truncated Z Value for each Cell (Z_{j}^{*})

To limit the amount of cancellation that takes place between cell results during aggregation, cells whose results suggest possible favoritism are left alone. Otherwise the cell statistic is set to zero. This means that positive equivalent Z values are set to 0, and negative values are left alone. Mathematically, this is written as

$$Z_j^* = \min(0, Z_j)$$



Calculate the Theoretical Mean and Variance

Calculate the theoretical mean and variance of the truncated statistic under the null hypothesis of parity, $E(Z_j^*|H_0)$ and $Var(Z_j^*|H_0)$. To compensate for the truncation in step 3, an aggregated, weighted sum of the Z_j^* will need to be centered and scaled properly so that the final aggregate statistic follows a standard normal distribution.

- If $W_j=0$, then no evidence of favoritism is contained in the cell. The formulae for calculating $E(Z_j^*|H_0)$ and $Var(Z_j^*|H_0)$ cannot be used. Set both equal to 0.
- If $\min(n_{1j}, n_{2j}) > 6$ for a mean measure, $\min\{a_{ij}(1-\frac{a_{ij}}{a_{ij}}), a_{2j}(1-\frac{a_{2j}}{a_{2j}})\} > 9$ for a proportion measure, $\min(n_{ij}, n_{2j}) > 15$ and $n_{j}q_{j}(1-q_{j}) > 9$ for a rate measure, or n_{1j} and n_{2j} are large for a ratio measure then

$$E(Z_{j}^{*} | H_{0}) = -\frac{1}{\sqrt{2\pi}}$$

and

$$Var(Z_{j}^{*} | H_{0}) = \frac{1}{2} - \frac{1}{2\pi}$$

• Otherwise, determine the total number of values for Z_{j}^{*} . Let z_{ji} and θ_{ji} , denote the values of Z_{j}^{*} and the probabilities of observing each value, respectively.

$$E(Z_j^* \mid H_0) = \sum_i \theta_{ji} Z_{ji}$$

and

$$Var(Z_{j}^{*} | H_{0}) = \sum_{i} \theta_{ji} Z_{ji}^{2} - \left[E(Z_{j}^{*} | H_{0}) \right]^{2}$$

The actual values of the z's and θ 's depends on the type of measure.

Mean Measure

$$\begin{split} N_j &= \text{min}(M_j, 1,000), \ i = 1, \dots, N_j \\ z_{ji} &= \text{min}\Big\{0, \Phi^{-1}\Big(1 - \frac{R_i - 0.5}{N_j}\Big)\Big\} \quad \text{where } R_i \text{ is the rank of sample sum i} \\ \theta_j &= \frac{1}{N_i} \end{split}$$



Proportion Measure

$$z_{ji} = \min \left\{ 0, \frac{n_{j} i - n_{1j} a_{j}}{\sqrt{\frac{n_{1j} n_{2j} a_{j} (n_{j} - a_{j})}{n_{j} - 1}}} \right\}, \quad i = \max(0, a_{j} - n_{2j}), \dots, \min(a_{j}, n_{1j})$$

$$\theta_{ji} = HG(i)$$

Rate Measure

$$z_{ji} = \min \left\{ 0, \frac{i - n_{j} q_{j}}{\sqrt{n_{j} q_{j} (1 - q_{j})}} \right\}, \quad i = 0, ..., n_{j}$$

$$\theta_{ii} = BN(i)$$

Ratio Measure

The performance measure that is in this class is billing accuracy. If a parity test were used, the sample sizes for this measure are quite large, so there is no need for a small sample technique. If one does need a small sample technique, then a re-sampling method can be used.

Calculate the Aggregate Test Statistic (Z^T)

$$Z^{T} = \frac{\sum_{j} W_{j} Z_{j}^{*} - \sum_{j} W_{j} E(Z_{j}^{*} | H_{0})}{\sqrt{\sum_{j} W_{j}^{2} Var(Z_{j}^{*} | H_{0})}}$$



The Balancing Critical Value

There are four key elements of the statistical testing process:

- the null hypothesis, H₀, that parity exists between ILEC and CLEC services
- the alternative hypothesis, H_a, that the ILEC is giving better service to its own customers
- the Truncated Z test statistic, Z^{T} , and
- a critical value, c

The decision rule² is

 $\begin{array}{lll} \bullet \text{If} & Z^T \leq c & \text{then} & \text{accept H_a.} \\ \bullet \text{If} & Z^T \geq c & \text{then} & \text{accept H_0.} \end{array}$

There are two types of error possible when using such a decision rule:

• Type I Error: Deciding favoritism exists when there is, in fact, no favoritism.

• Type II Error: Deciding parity exists when there is, in fact, favoritism.

The probabilities of each type of each are:

• **Type I Error**: $\alpha = P(Z^T < c \mid H_0)$

• Type II Error: $\beta = P(Z^T \ge c \mid H_a)$

We want a balancing critical value, $c_{\rm B}$, so that $\alpha = \beta$.

It can be shown that.

$$c_{B} = \frac{\sum_{j} W_{j} M(m_{j}, se_{j}) - \sum_{j} W_{j} \frac{-1}{\sqrt{2\pi}}}{\sqrt{\sum_{j} W_{j}^{2} V(m_{j}, se_{j})} + \sqrt{\sum_{j} W_{j}^{2} \left(\frac{1}{2} - \frac{1}{2\pi}\right)}}$$

^{2.} This decision rule assumes that a negative test statistic indicates poor service for the CLEC customer. If the opposite is true, then reverse the decision rule.

where

$$M(\mu,\sigma) = \mu \, \Phi(\frac{-\mu}{\sigma}) - \sigma \, \phi(\frac{-\mu}{\sigma})$$

$$V(\mu,\sigma) = (\mu^2 + \sigma^2) \Phi(\tfrac{-\mu}{\sigma}) - \mu \, \sigma \, \phi(\tfrac{-\mu}{\sigma}) - M(\mu,\sigma)^2$$

 $\Phi(\cdot)$ is the cumulative standard normal distribution function, and $\phi(\cdot)$ is the standard normal density function.

This formula assumes that Z_j is approximately normally distributed within cell j. When the cell sample sizes, n_{1j} and n_{2j} , are small this may not be true. It is possible to determine the cell mean and variance under the null hypothesis when the cell sample sizes are small. It is much more difficult to determine these values under the alternative hypothesis. Since the cell weight, W_j will also be small (see calculate weights section above) for a cell with small volume, the cell mean and variance will not contribute much to the weighted sum. Therefore, the above formula provides a reasonable approximation to the balancing critical value.

The values of m_i and se_i will depend on the type of performance measure.

Mean Measure

For mean measures, one is concerned with two parameters in each cell, namely, the mean and variance. A possible lack of parity may be due to a difference in cell means, and/or a difference in cell variances. One possible set of hypotheses that capture this notion, and take into account the assumption that transaction are identically distributed within cells is:

$$\begin{split} &H_0 \! : \mu_{1j} = \mu_{2j}, \sigma_{1j}^{\ 2} = \sigma_{2j}^{\ 2} \\ &H_a \! : \mu_{2j} = \mu_{1j} + \delta_j \! \cdot \! \sigma_{1j}, \sigma_{2j}^{\ 2} = \lambda_j \! \cdot \! \sigma_{1j}^{\ 2} \\ & \delta_j \! > \! 0, \, \lambda_j \! \geq \! 1 \text{ and } j = 1, \dots, L. \end{split}$$

Under this form of alternative hypothesis, the cell test statistic Z_i has mean and standard error given by

$$m_{j} = \frac{-\delta_{j}}{\sqrt{\frac{1}{n_{1j}} + \frac{1}{n_{2j}}}}$$

and

$$se_{j} = \sqrt{\frac{\lambda_{j}n_{1j} + n_{2j}}{n_{1j} + n_{2j}}}$$



Proportion Measure

For a proportion measure there is only one parameter of interest in each cell, the proportion of transaction possessing an attribute of interest. A possible lack of parity may be due to a difference in cell proportions. A set of hypotheses that take into account the assumption that transaction are identically distributed within cells while allowing for an analytically tractable solution is:

$$\begin{split} &H_0\colon \ \frac{p_{2j}(1-p_{1j})}{(1-p_{2j})p_{1j}} = 1 \\ &H_a\colon \ \frac{p_{2j}(1-p_{1j})}{(1-p_{2j})p_{1j}} = \psi_j \qquad \qquad \psi_j \geq 1 \ \text{and} \ j = 1, \dots, L. \end{split}$$

These hypotheses are based on the "odds ratio." If the transaction attribute of interest is a missed trouble repair, then an interpretation of the alternative hypothesis is that a CLEC trouble repair appointment is ψ_j times more likely to be missed than an ILEC trouble.

Under this form of alternative hypothesis, the within cell asymptotic mean and variance of a_{1j} are given by

$$E(a_{1j}) = n_j \pi_j^{(1)}$$

$$var(a_{1j}) = \frac{n_j}{\frac{1}{\pi_i^{(1)}} + \frac{1}{\pi_i^{(2)}} + \frac{1}{\pi_i^{(3)}} + \frac{1}{\pi_i^{(4)}}}$$

where

$$\begin{split} &\pi_{\mathbf{j}}^{(1)} = f_{\mathbf{j}}^{(1)} \left(\mathbf{n}_{\mathbf{j}}^{2} + f_{\mathbf{j}}^{(2)} + f_{\mathbf{j}}^{(3)} - f_{\mathbf{j}}^{(4)} \right) \\ &\pi_{\mathbf{j}}^{(2)} = f_{\mathbf{j}}^{(1)} \left(-\mathbf{n}_{\mathbf{j}}^{2} - f_{\mathbf{j}}^{(2)} + f_{\mathbf{j}}^{(3)} + f_{\mathbf{j}}^{(4)} \right) \\ &\pi_{\mathbf{j}}^{(3)} = f_{\mathbf{j}}^{(1)} \left(-\mathbf{n}_{\mathbf{j}}^{2} + f_{\mathbf{j}}^{(2)} - f_{\mathbf{j}}^{(3)} + f_{\mathbf{j}}^{(4)} \right) \\ &\pi_{\mathbf{j}}^{(4)} = f_{\mathbf{j}}^{(1)} \left(\mathbf{n}_{\mathbf{j}}^{2} \left(\frac{2}{\psi_{\mathbf{j}}} - 1 \right) - f_{\mathbf{j}}^{(2)} - f_{\mathbf{j}}^{(3)} - f_{\mathbf{j}}^{(4)} \right) \\ &f_{\mathbf{j}}^{(1)} = \frac{1}{2\mathbf{n}_{\mathbf{j}}^{2} \left(\frac{1}{\psi_{\mathbf{j}}} - 1 \right)} \\ &f_{\mathbf{j}}^{(2)} = \mathbf{n}_{\mathbf{j}} \mathbf{n}_{\mathbf{l}\mathbf{j}} \left(\frac{1}{\psi_{\mathbf{j}}} - 1 \right) \\ &f_{\mathbf{j}}^{(3)} = \mathbf{n}_{\mathbf{j}} \mathbf{a}_{\mathbf{j}} \left(\frac{1}{\psi_{\mathbf{j}}} - 1 \right) \\ &f_{\mathbf{j}}^{(4)} = \sqrt{\mathbf{n}_{\mathbf{j}}^{2} \left[4\mathbf{n}_{\mathbf{l}\mathbf{j}} \left(\mathbf{n}_{\mathbf{j}} - \mathbf{a}_{\mathbf{j}} \right) \left(\frac{1}{\psi_{\mathbf{j}}} - 1 \right) + \left(\mathbf{n}_{\mathbf{j}} + \left(\mathbf{a}_{\mathbf{j}} - \mathbf{n}_{\mathbf{l}\mathbf{j}} \right) \left(\frac{1}{\psi_{\mathbf{j}}} - 1 \right) \right)^{2}} \right] \end{split}$$

^{3.} Stevens, W. L. (1951) Mean and Variance of an entry in a Contingency Table. *Biometrica*, 38, 468-470.

Recall that the cell test statistic is given by

$$Z_{j} = \frac{n_{j} a_{1j} - n_{1j} a_{j}}{\sqrt{\frac{n_{1j} n_{2j} a_{j} (n_{j} - a_{j})}{n_{j} - 1}}}$$

Using the equations above, we see that Z_i has mean and standard error given by

$$m_{j} = \frac{n_{j}^{2} \pi_{j}^{(1)} - n_{1j} a_{j}}{\sqrt{\frac{n_{1j} n_{2j} a_{j} (n_{j} - a_{j})}{n_{j} - 1}}}$$

and

$$se_{j} = \sqrt{\frac{n_{j}^{3}(n_{j} - 1)}{n_{1j} n_{2j} a_{j} (n_{j} - a_{j}) \left(\frac{1}{\pi_{j}^{(1)}} + \frac{1}{\pi_{j}^{(2)}} + \frac{1}{\pi_{j}^{(3)}} + \frac{1}{\pi_{j}^{(4)}}\right)}}$$

Rate Measure

A rate measure also has only one parameter of interest in each cell, the rate at which a phenomenon is observed relative to a base unit, e.g. the number of troubles per available line. A possible lack of parity may be due to a difference in cell rates. A set of hypotheses that take into account the assumption that transaction are identically distributed within cells is:

$$\begin{aligned} &H_0\colon r_{1j}=r_{2j}\\ &H_a\colon r_{2j}=\epsilon_j r_{1j} \end{aligned} \qquad \qquad \epsilon_j>1 \text{ and } j=1,\ldots,L.$$

Given the total number of ILEC and CLEC transactions in a cell, n_j , and the number of base elements, b_{1j} and b_{2j} , the number of ILEC transaction, n_{1j} , has a binomial distribution from n_j trials and a probability of

$$q_j^* = \frac{r_{1j}b_{1j}}{r_{1j}b_{1j} + r_{2j}b_{2j}}$$

Therefore, the mean and variance of n_{1j} , are given by

$$E(n_{1j}) = n_j q_j^*$$

$$var(n_{1j}) = n_j q_j^* (1 - q_j^*)$$

Under the null hypothesis

$$q_{j}^{*} = q_{j} = \frac{b_{1j}}{b_{j}}$$

but under the alternative hypothesis

$$q_{j}^{*} = q_{j}^{a} = \frac{b_{1j}}{b_{1j} + \varepsilon_{j}b_{2j}}$$

Recall that the cell test statistic is given by

$$Z_{j} = \frac{n_{1j} - n_{j} q_{j}}{\sqrt{n_{j} q_{j} (1 - q_{j})}}$$

Using the relationships above, we see that Z_i has mean and standard error given by

$$m_{j} = \frac{n_{j}(q_{j}^{a} - q_{j})}{\sqrt{n_{j}q_{j}(1 - q_{j})}} = (1 - \varepsilon_{j})\frac{\sqrt{n_{j}b_{1j}b_{2j}}}{b_{1j} + \varepsilon_{j}b_{2j}}$$

and

$$se_{j} = \sqrt{\frac{q_{j}^{a}(1-q_{j}^{a})}{q_{j}(1-q_{j})}} = \sqrt{\varepsilon_{j}} \frac{b_{j}}{b_{1j} + \varepsilon_{j}b_{2j}}$$

Ratio Measure

As with mean measures, one is concerned with two parameters in each cell, the mean and variance, when testing for parity of ratio measures. As long as sample sizes are large, as in the case of billing accuracy, the same method for finding m_i and se_i that is used for mean measures can be used for ratio measures.

Determining the Parameters of the Alternative Hypothesis

In this section we have indexed the alternative hypothesis of mean measures by two sets of parameters, λ_j and δ_j . Proportion and rate measures have been indexed by one set of parameters each, ψ_j and ϵ_j respectively. A major difficulty with this approach is that more than one alternative will be of interest; for example we may consider one alternative in which all the δ_j are set to a common non-zero value, and another set of alternatives in each of which just one δ_j is non-zero, while all the rest are zero. There are very many other possibilities. Each possibility leads to a single value for the balancing critical value; and each possible critical value corresponds to many sets of alternative hypotheses, for each of which it constitutes the correct balancing value.

The formulas we have presented can be used to evaluate the impact of different choices of the overall critical value. For each putative choice, we can evaluate the set of alternatives for which this is the correct balancing value. While statistical science can be used to evaluate the impact of different choices of these parameters, there is not much that an appeal to statistical principles can offer in directing specific choices. Specific choices are best left to telephony experts. Still, it is possible to comment on some aspects of these choices:

Parameter Choices for λ_j – The set of parameters λ_j index alternatives to the null hypothesis that arise because there might be greater unpredictability or variability in the delivery of service to a CLEC customer over that which would be achieved for an otherwise comparable ILEC customer. While concerns about differences in the variability of service are important, it turns out that the truncated Z testing which is being recommended here is relatively insensitive to all but very large values of the λ_j . Put another way, reasonable differences in the values chosen here could make very little difference in the balancing points chosen.

Parameter Choices for δ_j – The set of parameters δ_j are much more important in the choice of the balancing point than was true for the λ_j . The reason for this is that they directly index differences in average service. The truncated Z test is very sensitive to any such differences; hence, even small disagreements among experts in the choice of the δ_j could be very important. Sample size matters here too. For example, setting all the δ_j to a single value – δ_j = δ \angle might be fine for tests across individual CLECs where currently in Kentucky the CLEC customer bases are not too different. Using the same value of δ for the overall state testing does not seem sensible. At the state level we are aggregating over CLECs, so using the same δ as for an individual CLEC would be saying that a "meaningful" degree of disparity is one where the violation is the same (δ) for each CLEC. But the detection of disparity for any component CLEC is important, so the relevant "overall" δ should be smaller.

Parameter Choices for ψ_j or ϵ_j — The set of parameters ψ_j or ϵ_j are also important in the choice of the balancing point for tests of their respective measures. The reason for this is that they directly index increases in the proportion or rate of service performance. The truncated Z test is sensitive to such increases; but not as sensitive as the case of δ for mean measures. Sample size matters here too. As with mean measures, using the same value of ψ or ϵ for the overall state testing does not seem sensible.

The three parameters are related however. If a decision is made on the value of δ , it is possible to determine equivalent values of ψ and ϵ . The following equations, in conjunction with the definitions of ψ and ϵ , show the relationship with delta.

$$\delta = 2 \cdot \arcsin(\sqrt{\hat{p}_2}) - 2 \cdot \arcsin(\sqrt{\hat{p}_1})$$
$$\delta = 2\sqrt{\hat{r}_2} - 2\sqrt{\hat{r}_1}$$

The bottom line here is that beyond a few general considerations, like those given above, a principled approach to the choice of the alternative hypotheses to guard against must come from elsewhere.

Decision Process

Once Z^T has been calculated, it is compared to the balancing critical value to determine if the ILEC is favoring its own customers over a CLEC's customers.

This critical value changes as the ILEC and CLEC transaction volume change. One way to make this transparent to the decision-maker, is to report the difference between the test statistic and the critical value, $diff = Z^T - c_B$. If favoritism is concluded when $Z^T < c_B$, then the diff < 0 indicates favoritism.

This makes it very easy to determine favoritism: a positive *diff* suggests no favoritism, and a negative *diff* suggests favoritism.



Appendix E: BST SEEM Remedy Calculation Procedures



BST SEEM Remedy Procedure

1. Tier-1 Calculation For Retail Analogues

- 1. Calculate the overall test statistic for each CLEC; z^{T}_{CLEC-1} (Per Statistical Methodology by Dr. Mulrow)
- 2. Calculate the balancing critical value ($^{c}B_{CLEC-1}$) that is associated with the alternative hypothesis (for fixed parameters δ, Ψ , or ϵ)
- 3. If the overall test statistic is equal to or above the balancing critical value, stop here. That is, if ^cB _{CLEC-1} < z^T_{CLEC-1}, stop here. Otherwise, go to step 4.
- 4. Calculate the Parity Gap by subtracting the value of step 2 from that of step 1. ABS (z^{T}_{CLEC-1} ${}^{c}B_{CLEC-1}$)
- 5. Calculate the Volume Proportion using a linear distribution with slope of ¼. This can be accomplished by taking the absolute value of the Parity Gap from step 4 divided by 4; ABS ((z^{T}_{CLEC-1} ${}^{c}B_{CLEC-1}$) / 4). All parity gaps equal or greater to 4 will result in a volume proportion of 100%.
- 6. Calculate the Affected Volume by multiplying the Volume Proportion from step 5 by the Total Impacted CLEC- $_1$ Volume (I_c) in the negatively affected cell; where the cell value is negative.
- 7. Calculate the payment to CLEC-1 by multiplying the result of step 6 by the appropriate dollar amount from the fee schedule.
- 8. Then, CLEC-1 payment = Affected Volume_{CLEC1} * \$\$from Fee Schedule



Example: CLEC-1 Missed Installation Appointments (MIA) for Resale POTS

Note – the statistical results are only illustrative. They are not a result of a statistical test of this data.

	n _l	N _C	I _c	MIA	MIA _C	z ^T CLEC-1	СВ	Parity Gap	Volume Proportion	Affected Volume
State	50000	600	96	9%	16%	-1.92	-0.21	1.71	0.4275	
Cell						z _{CLEC-1}				
1		150	17	0.091	0.113	-1.994				8
2		75	8	0.176	0.107	0.734				
3		10	4	0.128	0.400	-2.619				2
4		50	17	0.158	0.340	-2.878				8
5		15	2	0.245	0.133	1.345				
6		200	26	0.156	0.130	0.021				
7		30	7	0.166	0.233	-0.600				3
8		20	3	0.106	0.150	-0.065				2
9		40	9	0.193	0.225	-0.918				4
10		10	3	0.160	0.300	-0.660				2

29

where n_I = ILEC observations and n_C = CLEC-1 observations Payout for CLEC-1 is (29 units) * (\$100/unit) = \$2,900



Example: CLEC-1 Order Completion Interval (OCI) for Resale POTS

	n _I	n _C	I _c	OCI	ocıc	z ^T CLEC-1	СВ	Parity Gap	Volume Proportion	Affected Volume
State	50000	600	600	5days	7days	-1.92	-0.21	1.71	0.4275	
Cell						z _{CLEC-1}				
1		150	150	5	7	-1.994				64
2		75	75	5	4	0.734				
3		10	10	2	3.8	-2.619				4
4		50	50	5	7	-2.878				21
5		15	15	4	2.6	1.345				
6		200	200	3.8	2.7	0.021				
7		30	30	6	7.2	-0.600				13
8		20	20	5.5	6	-0.065				9
9		40	40	8	10	-0.918				17
10		10	10	6	7.3	-0.660				4

133

where $n_I = ILEC$ observations and $n_C = CLEC-1$ observations

Payout for CLEC-1 is (133 units) * (\$100/unit) = \$13,300



2. Tier-2 Calculation For Retail Analogues

- 1. Tier-2 is triggered by three consecutive monthly failures of any Tier 2 Remedy Plan sub-metric.
- 2. Therefore, calculate monthly statistical results and affected volumes as outlined in steps 2 through 6 for the CLEC Aggregate performance. Determine average monthly affected volume for the rolling 3-month period.
- 3. Calculate the payment to State Designated Agency by multiplying average monthly volume by the appropriate dollar amount from the Tier-2 fee schedule.
- 4. Therefore, State Designated Agency payment = Average monthly volume * \$\$from Fee Schedule

Example: CLEC-A Missed Installation Appointments (MIA) for Resale POTS

State	n _l	n _C	I _c	MIA	MIA _C	z ^T CLEC-A	СВ	Parity Gap	Volume Proportion	Affected Volume
Month 1	180000	2100	336	9%	16%	-1.92	-0.21	1.71	0.4275	
Cell						z _{CLEC-A}				
1		500	56	0.091	0.112	-1.994				24
2		300	30	0.176	0.100	0.734				
3		80	27	0.128	0.338	-2.619				12
4		205	60	0.158	0.293	-2.878				26
5		45	4	0.245	0.089	1.345				
6		605	79	0.156	0.131	0.021				
7		80	19	0.166	0.238	-0.600				9
8		40	6	0.106	0.150	-0.065				3
9		165	36	0.193	0.218	-0.918				16
10		80	19	0.160	0.238	-0.660				9

99

where $n_I = ILEC$ observations and $n_C = CLEC$ -A observations

Assume Months 2 and 3 have the same affected volumes. Payout 99 units * \$300/unit = \$29,700.

If the above example represented performance for each of months 1 through 3, then



Example: CLEC-A Missed Installation Appointments for 1Q00

State	Miss	Remedy Dollars
Month 1	X	\$29,700
Month 2	X	\$29,700
Month 3	X	\$29,700
1Q00		\$89,100



3. **Tier-1 Calculation For Benchmarks**

- 1. For each CLEC, with five or more observations, calculate monthly performance results for the State.
- 2. CLECs having observations (sample sizes) between 5 and 30 will use Table I below. The only exception will be for Collocation Percent Missed Due Dates.

Table I - Small Sample Size Table (95% Confidence)	Table I -	Small Sam	ple Size Table	(95% (Confidence)
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Sample Size	Equivalent 90% Benchmark	Equivalent 95% Benchmark	
5	60.00%	80.00%	
6	66.67%	83.33%	
7	71.43%	85.71%	
8	75.00%	75.00%	
9	66.67%	77.78%	
10	70.00%	80.00%	
11	72.73%	81.82%	
12	75.00%	83.33%	
13	76.92%	84.62%	
14	78.57%	85.71%	
15	73.33%	86.67%	
16	75.00%	87.50%	
17	76.47%	82.35%	

Sample Size	Equivalent 90% Benchmark	Equivalent 95% Benchmark
18	77.78%	83.33%
19	78.95%	84.21%
20	80.00%	85.00%
21	76.19%	85.71%
22	77.27%	86.36%
23	78.26%	86.96%
24	79.17%	87.50%
25	80.00%	88.00%
26	80.77%	88.46%
27	81.48%	88.89%
28	78.57%	89.29%
29	79.31%	86.21%
30	80.00%	86.67%

- 3. If the percentage (or equivalent percentage for small samples) meets the benchmark standard, stop here. Otherwise, go to step 4.
- 4. Determine the Volume Proportion by taking the difference between the benchmark and the actual performance
- 5. Calculate the Affected Volume by multiplying the Volume Proportion from step 4 by the Total Impacted CLEC-1
- 6. Calculate the payment to CLEC-1 by multiplying the result of step 5 by the appropriate dollar amount from the
- 7. CLEC-1 payment = Affected Volume_{CLEC-1} * \$\$from Fee Schedule

Example: CLEC-1 Percent Missed Due Dates for Collocations

	n _C	Benchmark	MIA _C	Volume Proportion	Affected Volume
State	600	10%	13%	.03	18

Payout for CLEC-1 is (18 units) * (\$5000/unit) = \$90,000



4. Tier-1 Calculation For Benchmarks (In The Form Of A Target)

- 1. For each CLEC with five or more observations calculate monthly performance results for the State.
- 2. CLECs having observations (sample sizes) between 5 and 30 will use Table I above.
- 3. Calculate the interval distribution based on the same data set used in step 1.
- 4. If the 'percent within' (or equivalent percentage for small samples) meets the benchmark standard, stop here. Otherwise, go to step 5.
- 5. Determine the Volume Proportion by taking the difference between benchmark and the actual performance result
- 6. Calculate the Affected Volume by multiplying the Volume Proportion from step 5 by the Total CLEC-1 Volume.
- 7. Calculate the payment to CLEC-1 by multiplying the result of step 6 by the appropriate dollar amount from the fee schedule.

CLEC-1 payment = Affected Volume_{CLEC1} * \$\$from Fee Schedule

Example: CLEC-1 Reject Timeliness

	n _C	Benchmark	Reject Timeliness	Volume Proportion	Affected Volume
State	600	95% within 1 hour	93% within 1 hour	.02	12

Payout for CLEC-1 is (12 units) * (\$100/unit) = \$1,200



5. Tier-2 Calculations For Benchmarks

Tier-2 calculations for benchmark measures are the same as the Tier-1 benchmark calculations, except the CLEC Aggregate data having failed for three months.